

# Structure change in light neutron-rich nuclei via nucleon transfer reaction

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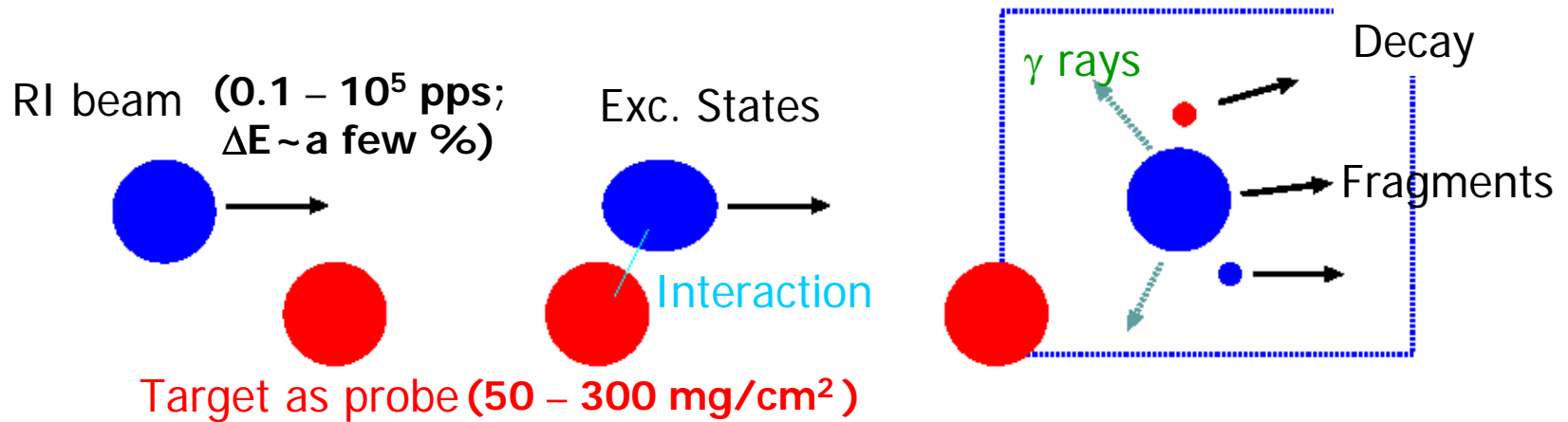
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# Inverse Kinematics w/ RI beam (30-100 MeV/u)



- **Formation** of Excited States of Exotic Nuclei
  - Direct reactions and their selectivities
- **In-beam spectroscopy** measuring decay products
  - Invariant-mass/ $\gamma$ -ray spectroscopy
    - Particle detectors at forward angles (kinematical focus)
    - Gamma detectors surrounding target (Doppler shift)

# Probes for direct reactions (30-100 MeV/u)

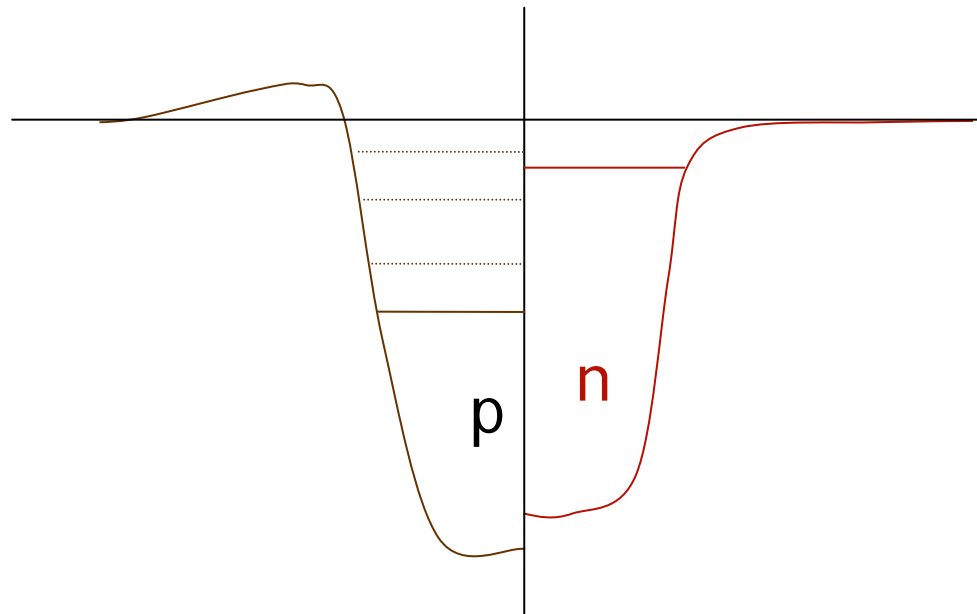
- Heavy Nuclei: Strong Coulomb Field
  - Coulomb Excitation, Coulomb Dissociation
    - E1, E2, (M1) / Isovector
- H, D,  $^4\text{He}$  [Liquid targets]
  - Inelastic Scattering
    - Collective / single-particle states (odd nuclei)
    - Isovector (H) / Isoscalar(H, D,  $^4\text{He}$ )
    - Spin-Flip (H, D) / Spin-Non-Flip (H, D,  $^4\text{He}$ )
  - Charge Exchange
    - Fermi type (H) / Gamow-Teller type (H, D)
  - Nucleon Transfer
    - $(\alpha, t)$ ,  $(\alpha, ^3\text{He})$  Reaction
  - Knockout
    - Hole states
- ◆ Other (Be, C, etc.)
  - Inelastic Scattering
  - Knockout / Fragmentation

# Motivation for transfer reactions

Structure information of nuclei as functions of **N** and **Z**

## Shell Evolution : Single particle states

- Spectroscopy of proton (unoccupied) single particle states in neutron-rich nuclei



# Nucleon (Proton) Transfer

- (d,n), ( $^3\text{He}$ ,d), ( $\alpha$ ,t), ...

Incident energy higher than 30 MeV/u

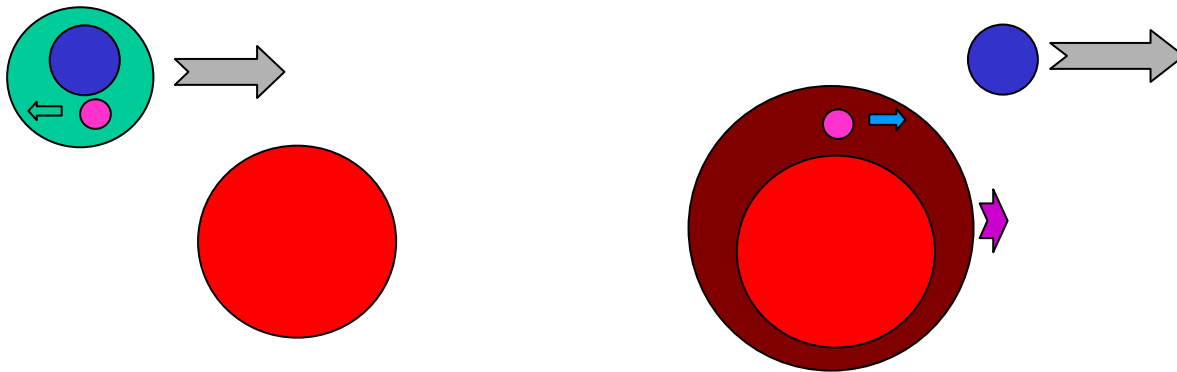
- ✓ Thicker target (100~200 mg/cm<sup>2</sup>)
- ✓ Less distortion effect
- ✓ Less multi-step process
- ✓ Same optical potential as inelastic excitation
- ✓ Identification by comparing with other direct reactions

But

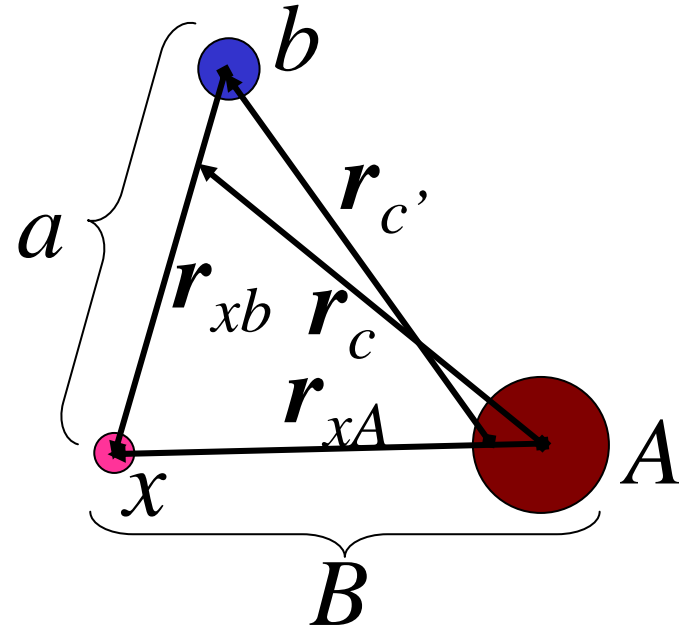
x Momentum mismatch

# Momentum Matching Condition

- As if “Getting off from the moving train (projectile) to platform (target)”
  - Internal motion in the train (Fermi motion in the projectile) along the opposite direction of the train (target)
  - Motion on the platform (Fermi motion of the nucleon on the target) along the direction of the train



$$\begin{aligned}
 [c] & \quad [c'] \\
 a + A & \rightarrow b + B \\
 a & = (b + x) \\
 B & = (A + x)
 \end{aligned}$$



### Plane Wave Born Approx.

$$T_{PW}^{\text{Post}} = \langle \phi_{c'} | V_{xb} + V_{bA} | \phi_c \rangle$$

$$T_{PW}^{\text{Prior}} = \langle \phi_{c'} | V_{xA} + V_{bA} | \phi_c \rangle$$

$$\begin{aligned}
 \langle \phi_{c'} | V_{xb} | \phi_c \rangle &= -\frac{1}{(2\pi)^3} \frac{\hbar^2}{2\mu_{xb}} (k_{xb}^2 + \kappa_a^2) \int d^3 r_{xb} \psi_a(\vec{r}_{xb}) e^{i\vec{k}_{xb} \cdot \vec{r}_{xb}} \int d^3 r_{xA} \psi_B^*(\vec{r}_{xA}) e^{-i\vec{k}_{xA} \cdot \vec{r}_{xA}} \\
 \langle \phi_{c'} | V_{xA} | \phi_c \rangle &= -\frac{1}{(2\pi)^3} \frac{\hbar^2}{2\mu_{xA}} (k_{xA}^2 + \kappa_B^2) \int d^3 r_{xb} \psi_a(\vec{r}_{xb}) e^{i\vec{k}_{xb} \cdot \vec{r}_{xb}} \int d^3 r_{xA} \psi_B^*(\vec{r}_{xA}) e^{-i\vec{k}_{xA} \cdot \vec{r}_{xA}}
 \end{aligned}$$

$$\vec{k}_{xb} = \frac{b}{a} \vec{k}_c - \vec{k}_{c'}; \quad \vec{k}_{xA} = \vec{k}_c - \frac{A}{B} \vec{k}_{c'}$$

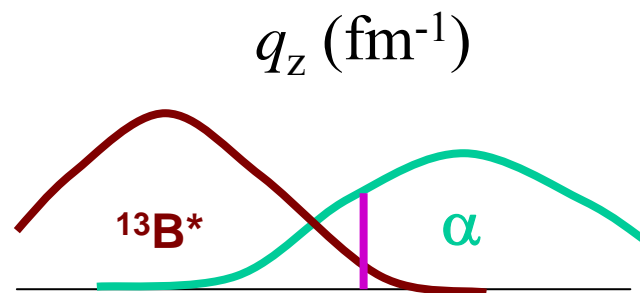
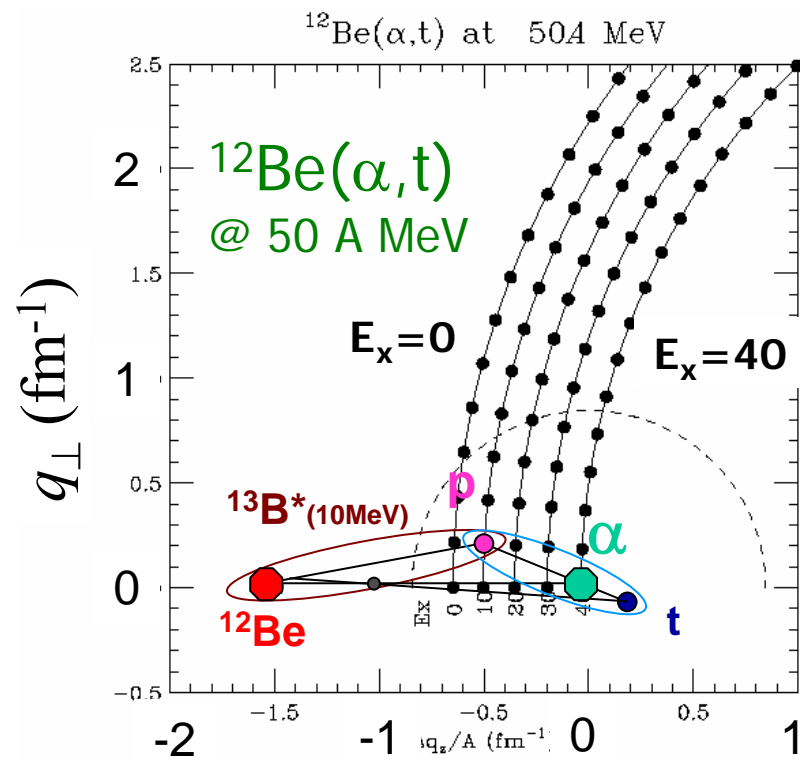
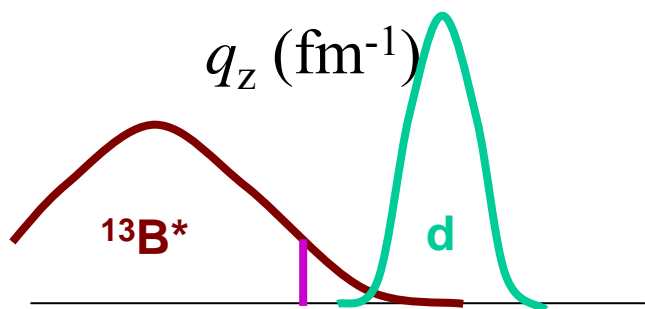
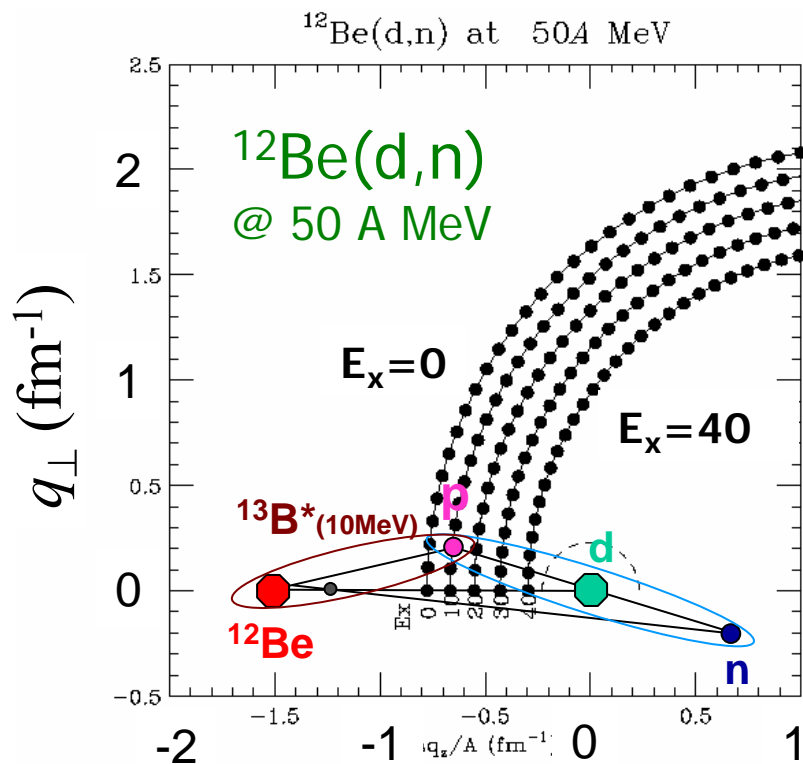
Fourier Transforms of wave functions of nucleon (x) in *a* and *B*

Same value but different expressions

$$\frac{\hbar^2 \kappa_a^2}{2\mu_{xb}} = \varepsilon_a; \quad \frac{\hbar^2 \kappa_B^2}{2\mu_{xA}} = \varepsilon_B \quad \text{Binding energies of } a \text{ and } B$$

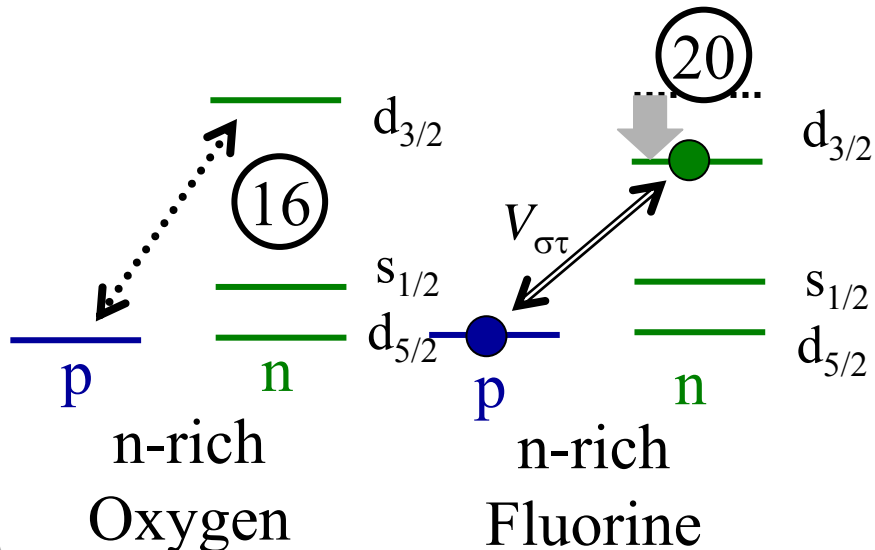


# Proton Transfer in Momentum Space

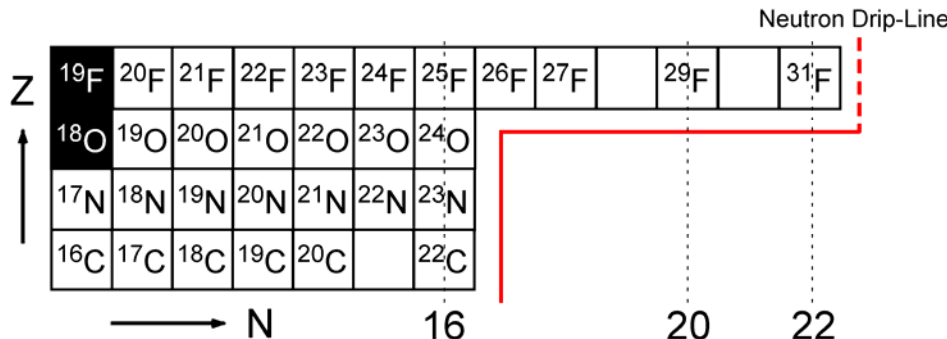


# Exotic Magic Number at N=16 (Z~8)

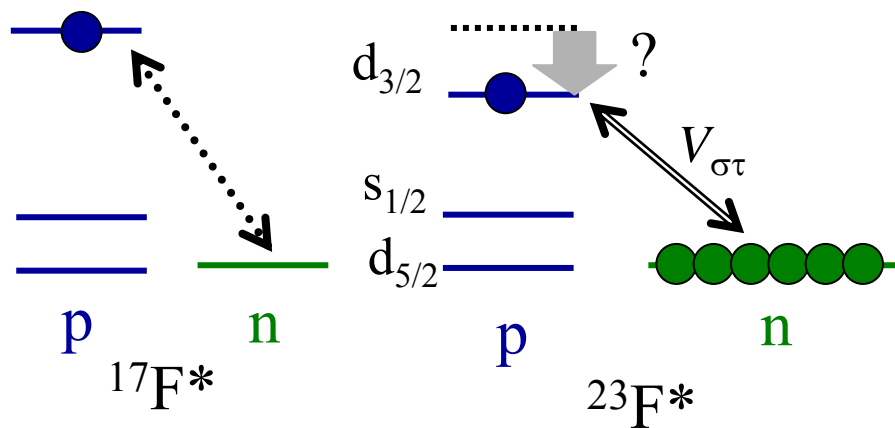
Spin-orbit splitting between  $vd_{3/2}$  &  $vd_{5/2}$  depend on the number of protons in  $d_{5/2}$  orbit attracting  $vd_{3/2}$  orbit by  $V_{\sigma\tau}$



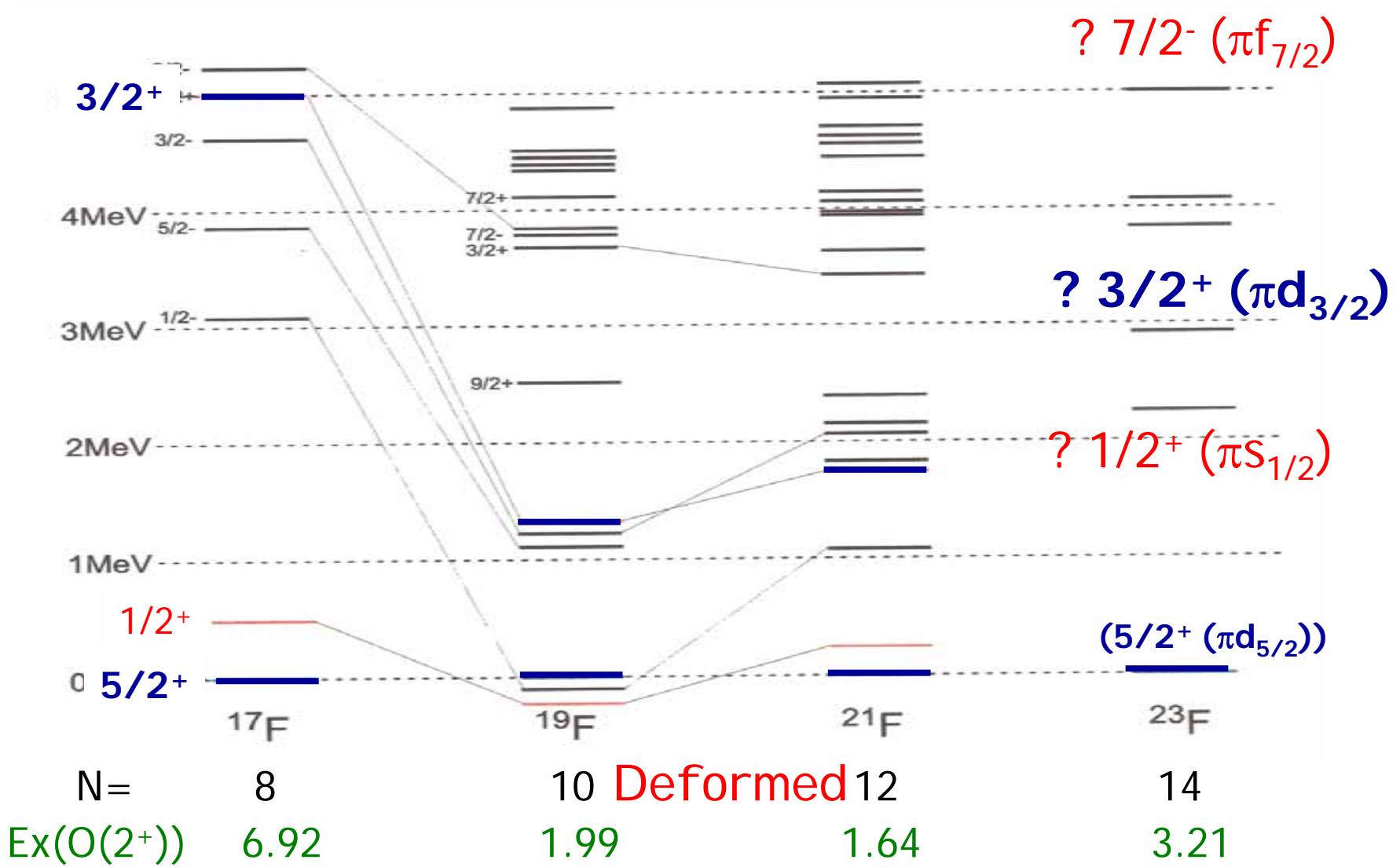
**Excitation energy of  $3/2^+$  S.P. state in  $^{17}\text{F}$  &  $^{23}\text{F}$  ?**



Change of Fluorine **Proton** Shell as a function of **Neutron** number



# Known Energy Levels of Fluorine Isotopes



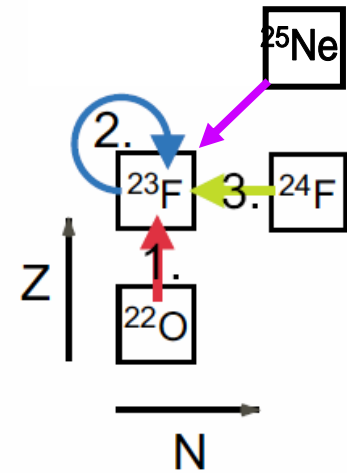
${}^4\text{He}({}^{22}\text{O}, {}^{23}\text{F}\gamma)$ ,  ${}^4\text{He}({}^{23}\text{F}, {}^{23}\text{F}\gamma)$ ,  ${}^4\text{He}({}^{24}\text{F}, {}^{23}\text{F}\gamma)$ ,  ${}^4\text{He}({}^{25}\text{Ne}, {}^{23}\text{F}\gamma)$

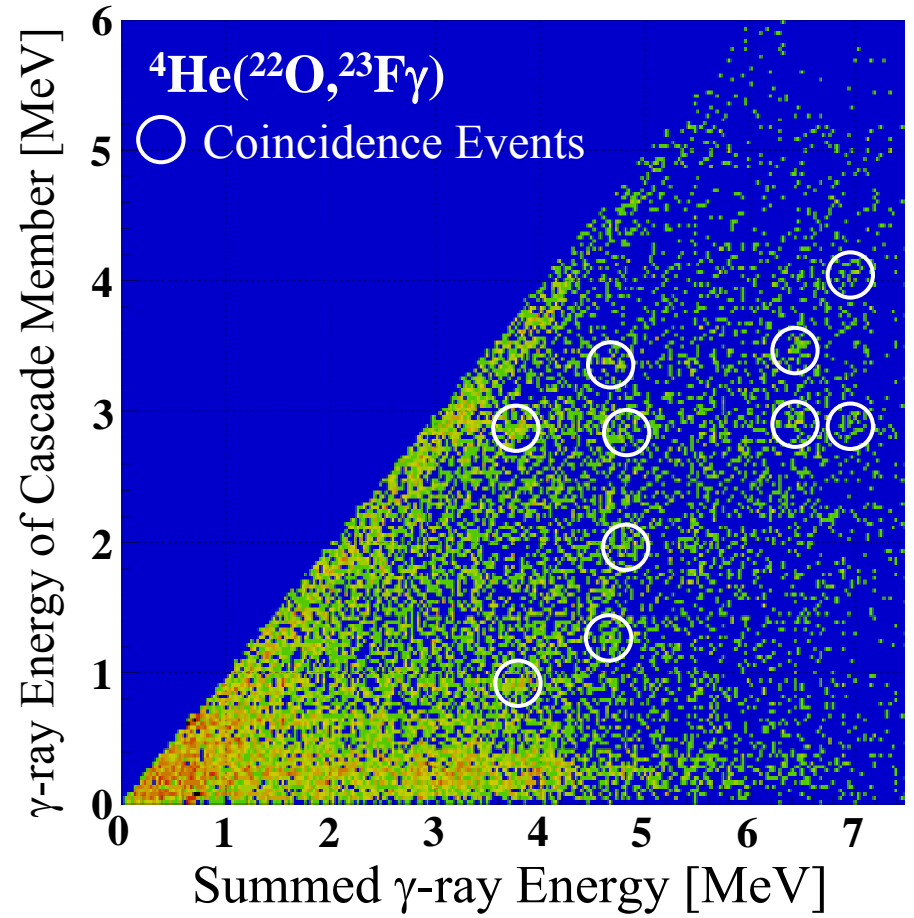
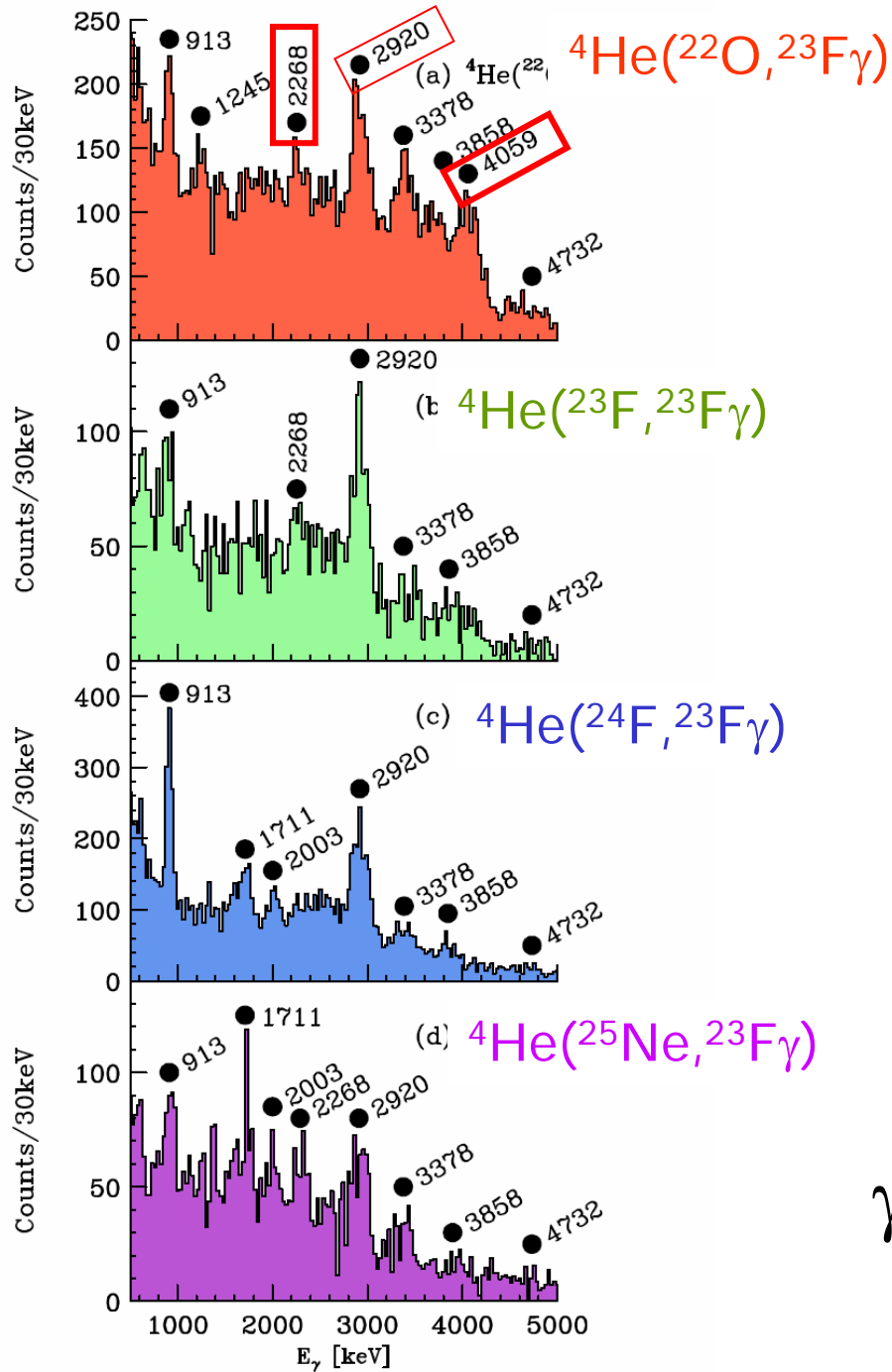
- Use of Cocktail beam ( ${}^{22}\text{O}$ ,  ${}^{23}\text{F}$ ,  ${}^{24}\text{F}$ ,  ${}^{25}\text{Ne}$ )
- Gamma ray measurement coincident with  ${}^{23}\text{F}$  ejectile

### Three Different Reactions Approaching ${}^{23}\text{F}$

1.  ${}^4\text{He}({}^{22}\text{O}, {}^{23}\text{F}\gamma)$ : Proton Pickup Reaction
2.  ${}^4\text{He}({}^{23}\text{F}, {}^{23}\text{F}\gamma)$ : Inelastic Scattering
3.  ${}^4\text{He}({}^{24}\text{F}, {}^{23}\text{F}\gamma)$ : Knockout
4.  ${}^4\text{He}({}^{25}\text{Ne}, {}^{23}\text{F}\gamma)$ :

1. Proton S.P. states ( $5/2^+$ ,  $1/2^+$ ,  $3/2^+$ )
2. Collective states; Non-spin-flip states  
([core 2+]  $\otimes$  S.P. state, etc)
3. Neutron hole states

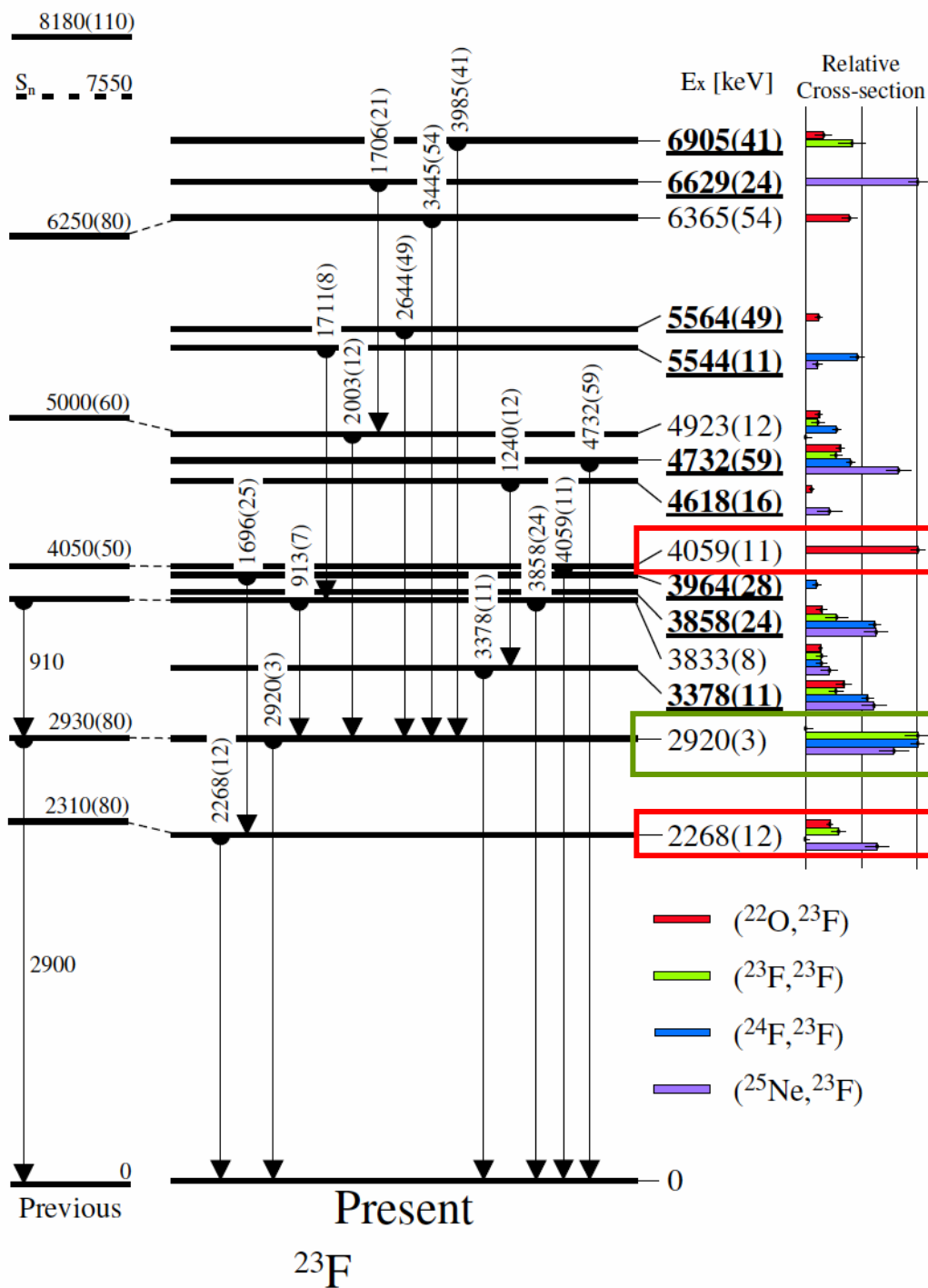
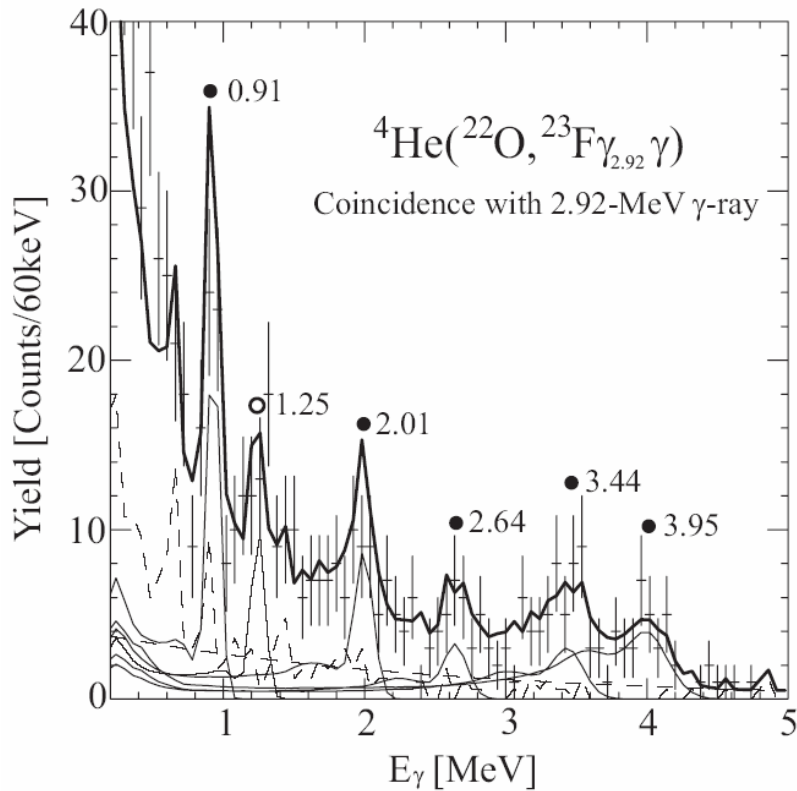




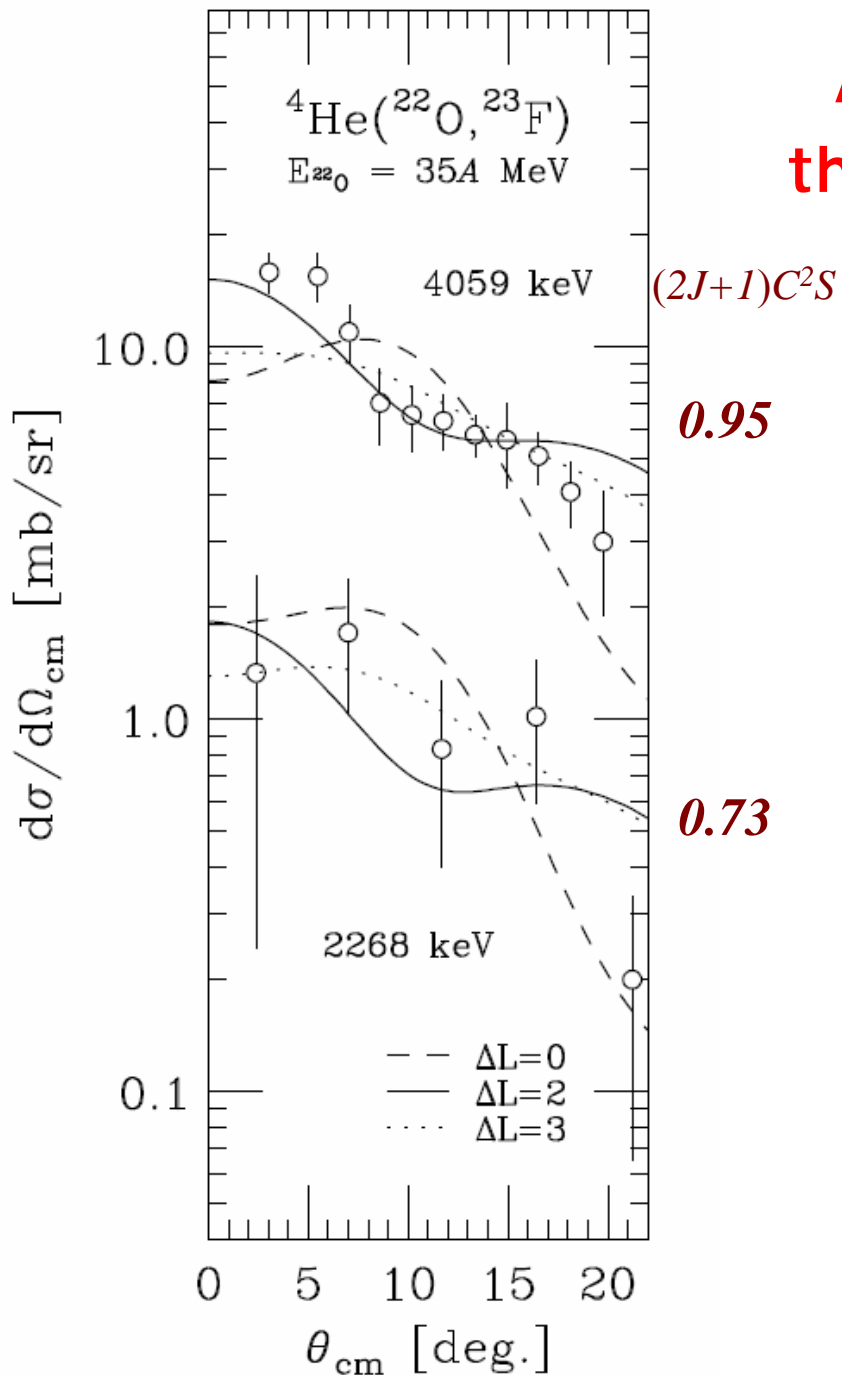
$\gamma$  ray spectra

# Level Scheme of $^{23}\text{F}$

Fitting using response functions by GEANT3 simulations



# Angular Distributions for the 4.06- and 2.37-MeV state

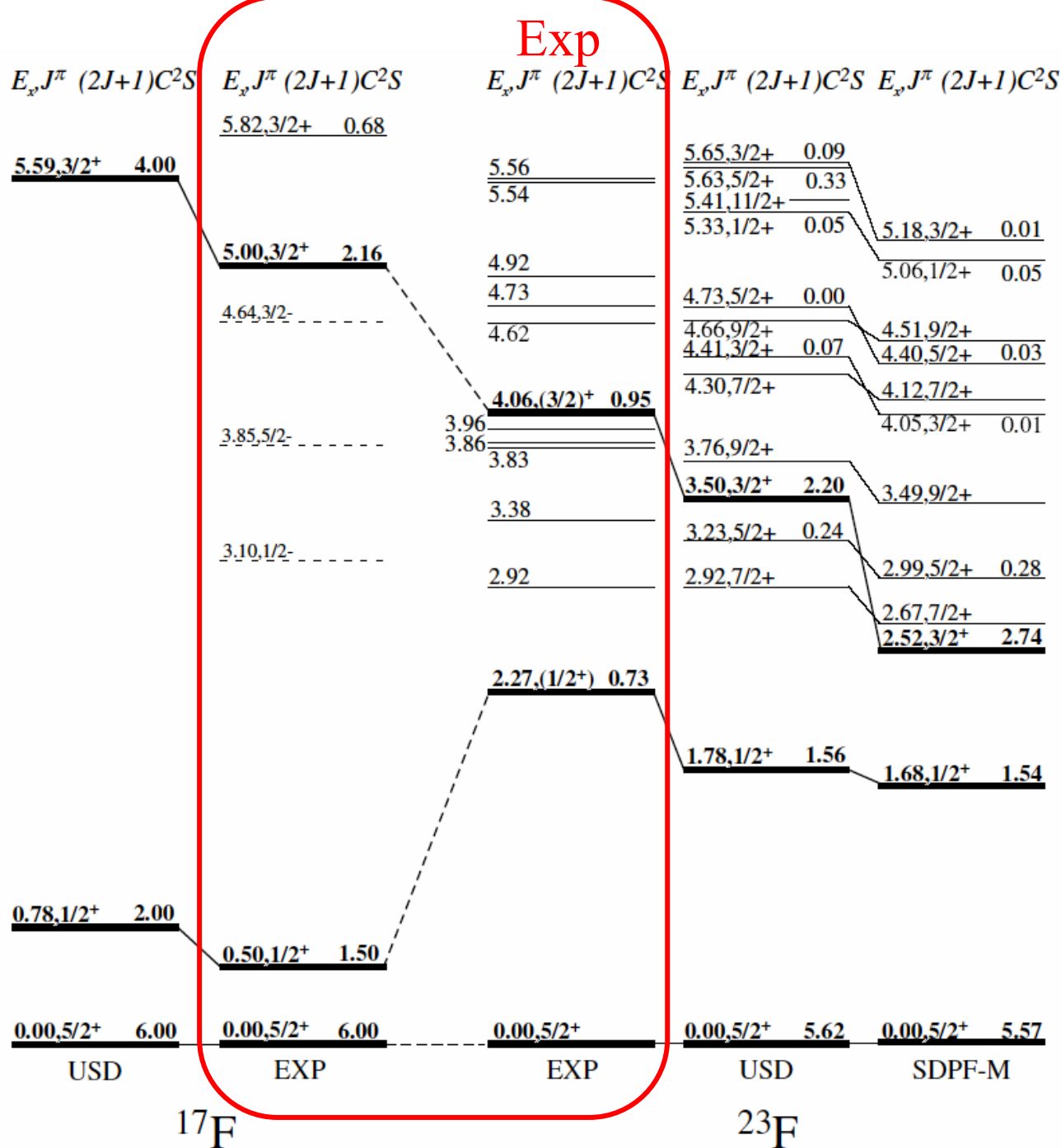


$J^\pi$  and spectroscopic factors of excited states by DWBA analysis.

- Optical Potentials of the  ${}^{22}\text{O}+\alpha$  and the  ${}^{23}\text{F}+t$  channels deduce from angular distributions for  ${}^{22}\text{O}(\alpha, \alpha')$  and  ${}^{23}\text{F}(\alpha, \alpha')$

The 4.06-MeV state :  
 Single particle state in  $d$ .

The 2.27-MeV state : consistent with  
 Single particle state in the  $s$ .



## Comparison with Shell Model Calculations

LS splitting of proton single particle energy may be larger than stable nuclei because of neutron-richness

$$V_{LS} \propto \frac{1}{r} \frac{d}{dr} V(r) (\vec{l} \cdot \vec{s})$$

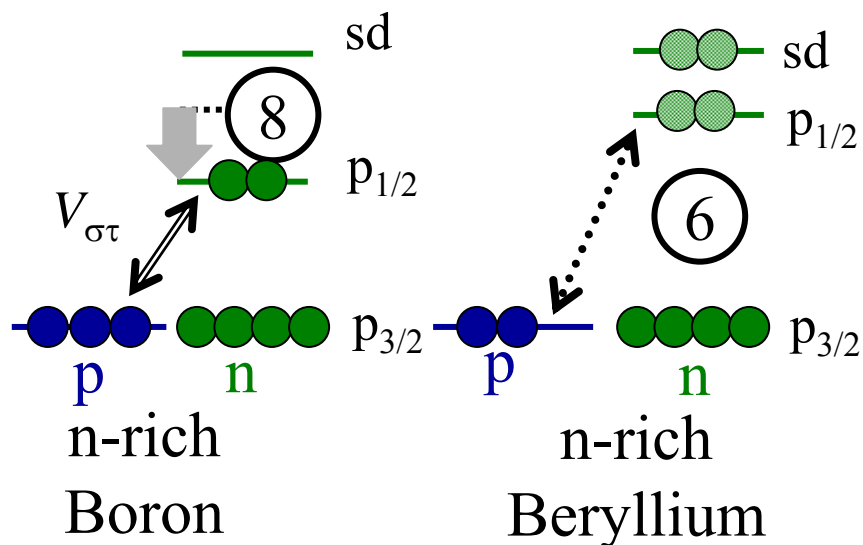
[1] B.A.Brown,  
<http://www.nsl.msu.edu/~brown/resources/SDE.HTM>

[2] T.Otsuka, *private communication*.: predicts N=16 magic number



## N-rich N=8 Nuclei

Spin-orbit splitting between  $vp_{1/2}$  &  $vp_{3/2}$  depend on the number of protons in  $dp_{1/2}$  orbit attracting  $vp_{1/2}$  orbit



## $^{13}\text{B}$

- Spherical ground state
- How about excited states?
  - Deformed core + proton?

## $^{12}\text{Be}$

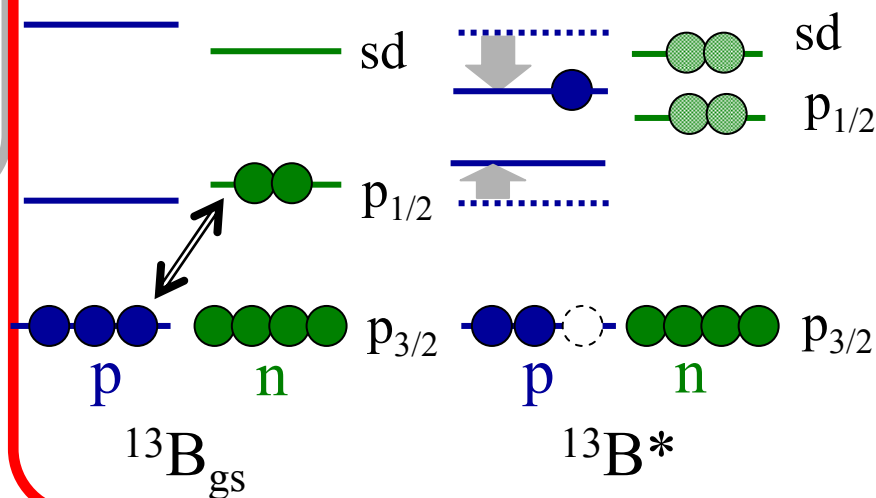
- Low-lying  $2^+$  state
- Low-lying  $1^-$  state
- Low-lying  $0^+_2$  state

Magicity loss in N=8

Deformed ground state

Change of Boron Proton Shell as a function of configuration

Deformed mean field?



# ${}^4\text{He}({}^{12}\text{Be}, {}^{13}\text{B}\gamma) @ 50 \text{ A MeV}$

Deformed  ${}^{12}\text{Be}$  core + 1 proton ?

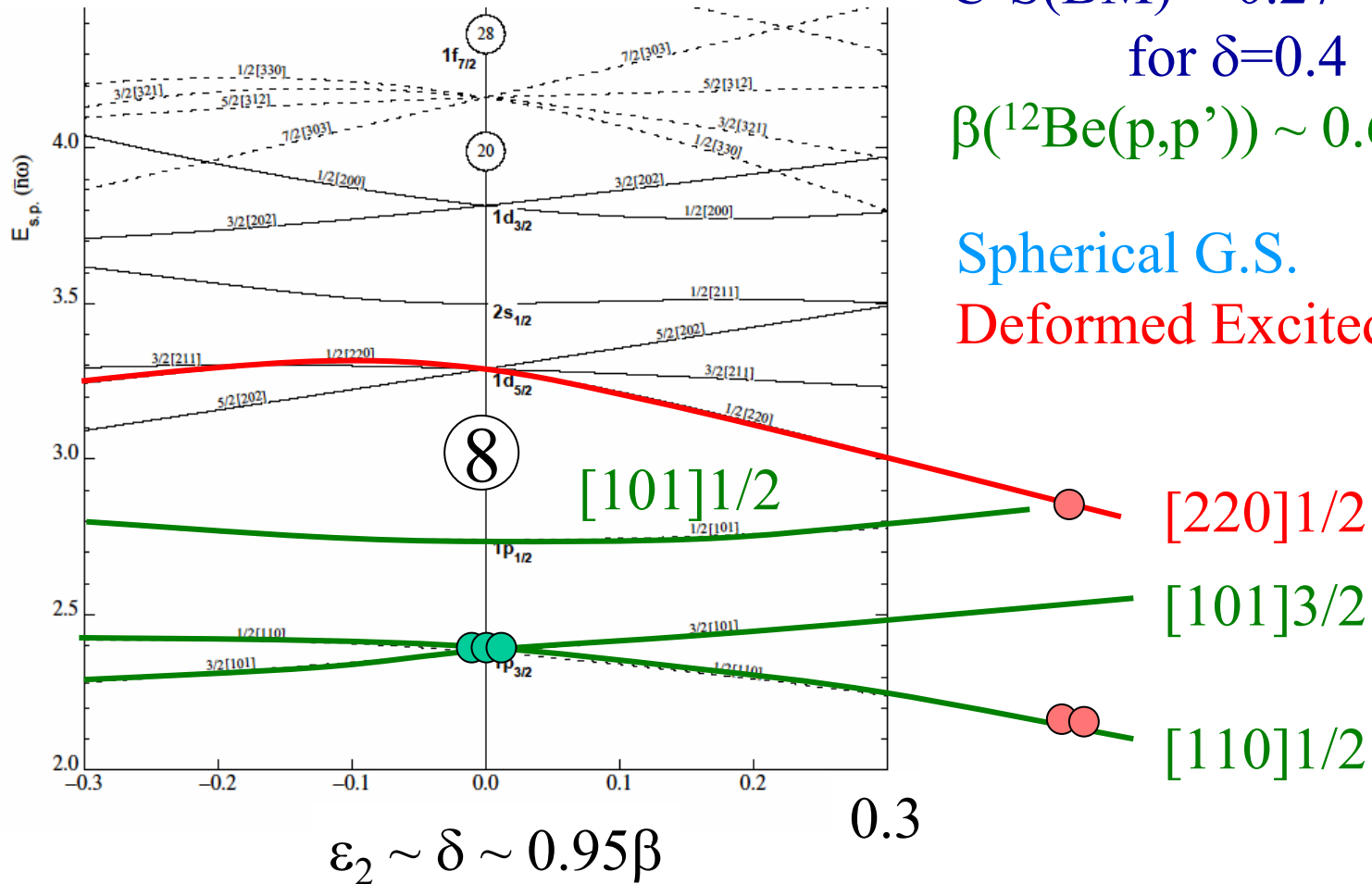
$C^2S(\text{BM}) \sim 0.27$

for  $\delta=0.4$

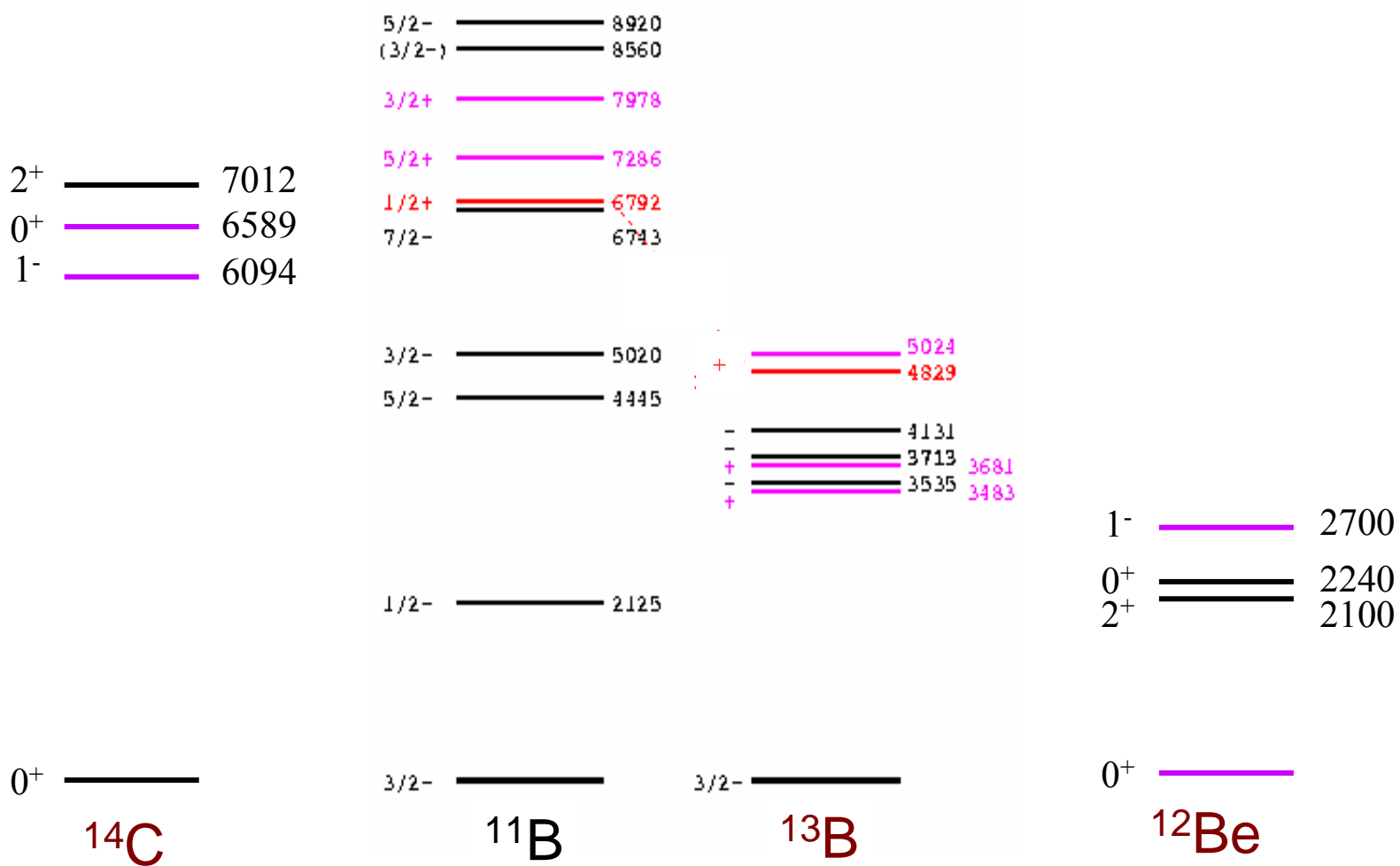
$\beta({}^{12}\text{Be}(p,p')) \sim 0.6-0.7$

Spherical G.S.

Deformed Excited  $1/2^+$  ?



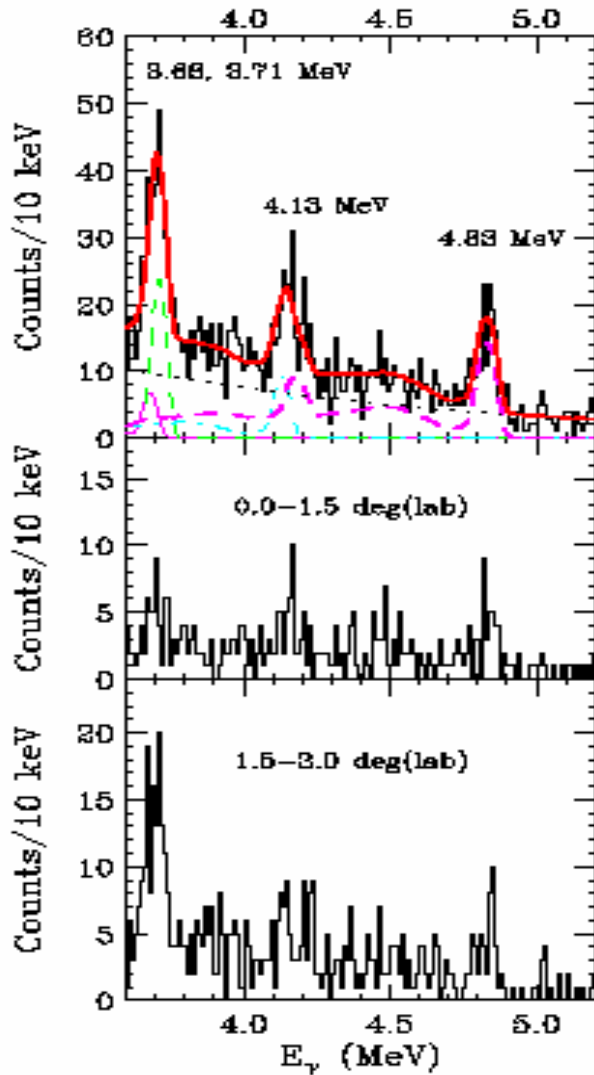
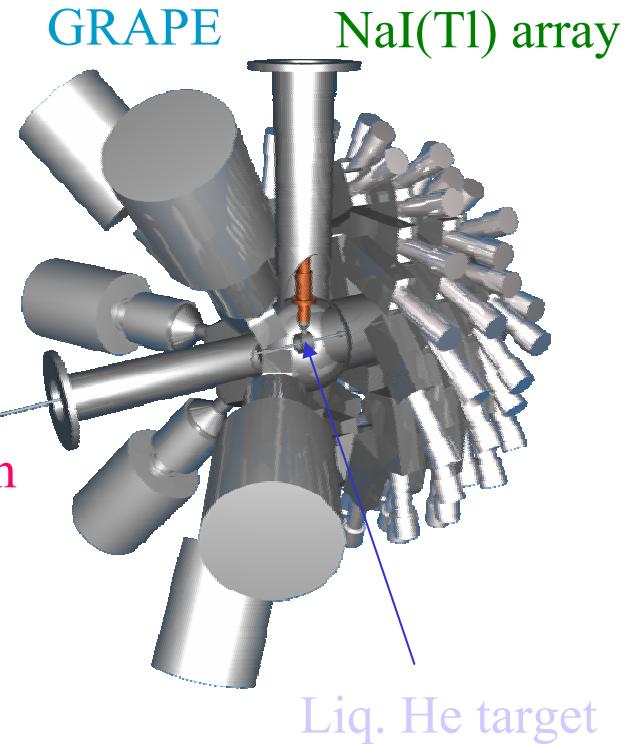
# Spectra of $^{14}\text{C}$ , $^{12}\text{Be}$ , $^{11}\text{B}$ , and $^{13}\text{B}$



# $^4\text{He}(^{12}\text{Be}, ^{13}\text{B}_\gamma) @ 50 \text{ A MeV}$

3.71 & 4.83 MeV states strongly excited by  $(\alpha, t)$

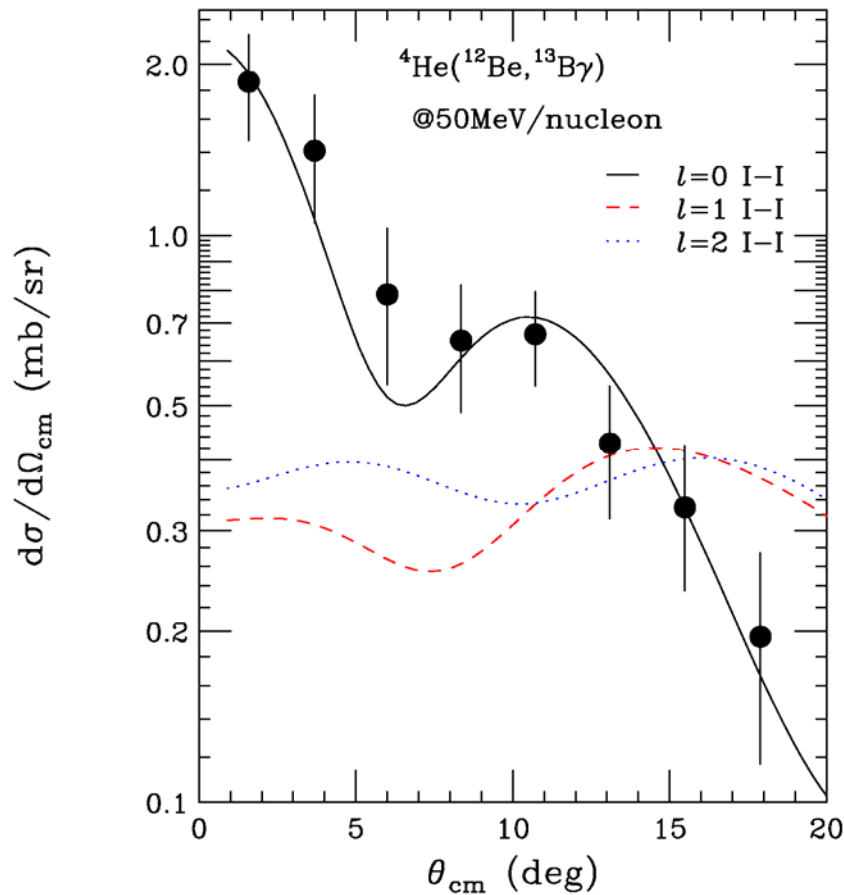
Different transferred  $L$



[keV]	$^4\text{He}(^{12}\text{Be}, ^{13}\text{B}_\gamma)$	$^{11}\text{B}(t,p)$	$^{13}\text{B}^9\text{Be}(^{14}\text{B}, ^{13}\text{B})$	$^{14}\text{Be}(n)$	$^{16}\text{O}(^{14}\text{N}, ^{17}\text{F})$	$^{13}\text{B}^{12}\text{C}(^{14}\text{C}, ^{13}\text{N})$	$^{13}\text{B}^{12}\text{C}(^{13}\text{C}, ^{12}\text{N})$	$^{13}\text{B}^{12}\text{C}(^{15}\text{N}, ^{14}\text{O})$
4829	1.00	0.03			1.00	0.34		
4131	0.59(13)	1.00	0.40			0.23	0.78	0.39
3713	0.95(18)	0.25				1.00	1.00	1.00
3681	0.48(16)	0.38	1.00					
3534	0.31(12)	0.19		1.00				
3482	0.06(13)	0.06	0.60					

# $^4\text{He}(^{12}\text{Be}, ^{13}\text{B}\gamma) @ 50 \text{ A MeV}$

Angular Distribution of  $^{13}\text{B}$  coin. with **4829** keV  $\gamma$



FR-DWBA (DWUCK5)

Optical Potential:

$^{12}\text{C} + ^4\text{He}$  (entrance)

$^{12}\text{C} + ^3\text{He}$  (exit)

$L=0 \rightarrow J^\pi = 1/2^+$

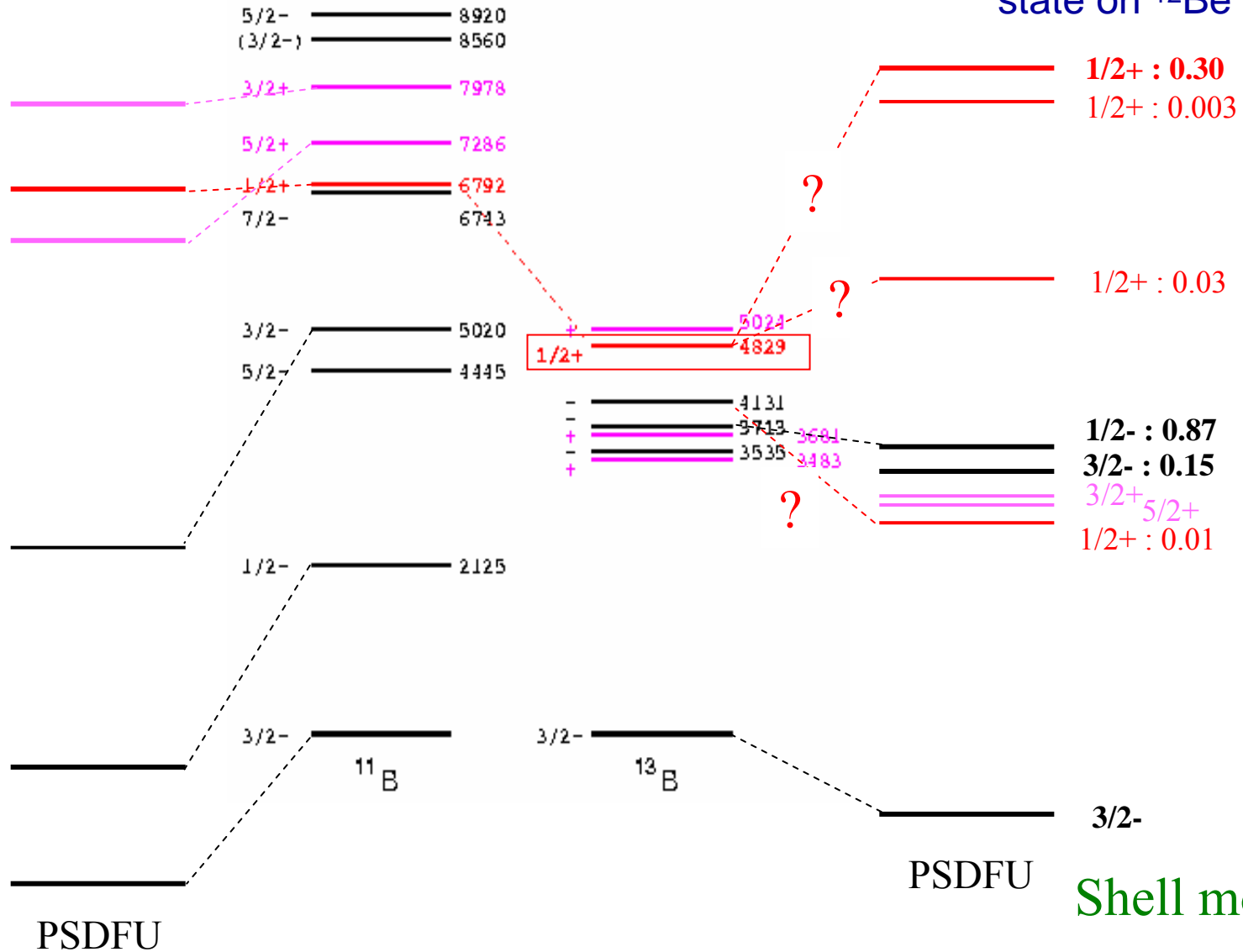
$C^2S = 0.1 - 0.2$

dep. on Potentials

$\rightarrow$  Proton "single particle" state on  $^{12}\text{Be}$

# ${}^4\text{He}({}^{12}\text{Be}, {}^{13}\text{B}\gamma) @ 50 \text{ A MeV}$

Proton "single particle" state on  ${}^{12}\text{Be}$



# 1/2<sup>+</sup> state in <sup>13</sup>B\* Configuration

$$|^{12}\text{Be}_{\text{gs}}\rangle = \alpha |(\pi p)^2 (vp)^6\rangle_{0\hbar\omega} + \beta |(\pi p)^2 (vp)^4 (vsd)^2\rangle_{2\hbar\omega} + \dots$$

$$|\alpha|^2 \sim |\beta|^2 \sim 0.5$$

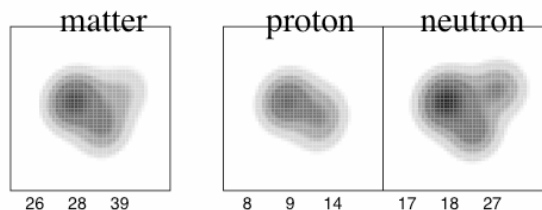
deformation

Deformed <sup>12</sup>Be core + 1 proton

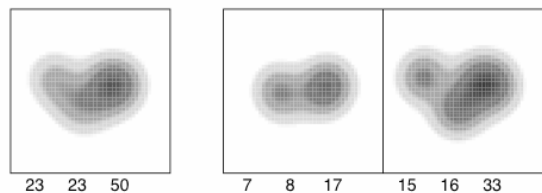
$$|^{13}\text{B}^*(1/2^+)\rangle = \alpha' |(\pi p)^2 (\pi sd)(vp)^6\rangle_{1\hbar\omega} + \beta' |(\pi p)^2 (\pi sd)(vp)^4 (vsd)^2\rangle_{3\hbar\omega} + \gamma' |(\pi p)^2 (vp)^6 (vsd)\rangle + \delta' |(\pi p)^2 (vp)^4 (vsd)^3\rangle + \dots$$

$$C^2S = \langle ^{13}\text{B}^*(1/2^+) | ^{12}\text{Be}_{\text{gs}} + p(\ell=0) \rangle \approx \alpha\alpha' + \beta\beta'$$

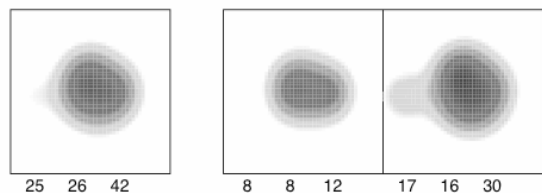
# 1/2<sup>+</sup> state in <sup>13</sup>B\* by AMD Kanada-Enyo prelim.



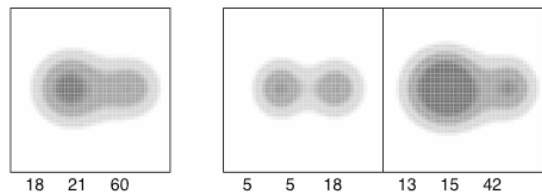
13B(3/2-)



13B(1/2+)



second  
13B(1/2+)



12Be(0+)

- 1/2<sup>+</sup><sub>1</sub> : 変形した状態
  - 70% 1h
  - 30% 1h + 2h
    - 陽子の励起状態
  - <sup>12</sup>Beの基底状態の配位混合を反映した状態
- 1/2<sup>+</sup><sub>2</sub> : 球形の状態
  - 1h + 0h
- 本実験では、1/2<sup>+</sup><sub>1</sub>状態が励起?



# Summary

- $(\alpha, t)$  and  $(\alpha, {}^3\text{He})$  reactions at intermediate energy can be used for spectroscopy of single-particle states in exotic nuclei.
- Spectroscopy of  ${}^{23}\text{F}$  was also performed by  $(\alpha, t)$  reaction combined with inelastic and knock-out reactions
- Level scheme was constructed for  ${}^{23}\text{F}$
- Spin-orbit splitting of  $3/2^+$  and  $5/2^+$  was not so small as predictions of shell models.
- $\gamma$ -ray spectroscopy of  ${}^{13}\text{B}$  excited by Proton Transfer ( ${}^{12}\text{Be}, {}^{13}\text{B}\gamma$ ) reaction was measured.
- The 4.8-MeV state have  $J^\pi$  of  $1/2^+$  and an proton  $S$ -factor of  $\approx 0.1\sim 0.2$  by DWBA analysis
  - Differs from standard shell-model prediction
  - It might be contain  $[220]1/2^+$  configuration on the deformed  ${}^{12}\text{Be}$  core.
  - $1/2^+_1$  state in AMD calculation
- $(\alpha, t)$ ,  $(\alpha, {}^3\text{He})$  reaction on  ${}^{32}\text{Mg}$  and  ${}^{34}\text{Si}$  was measured recently by using position-sensitive Ge array, GRAPE. N-rich nuclei around  $N\sim 20$