

# Comprehensive treatment of correlations at different energy scales in nuclei using Green's functions

- |                         |   |
|-------------------------|---|
| Lecture 1: 8/28/07      | Propagator description of single-particle motion and the link with experimental data    |
| Lecture 2: 8/29/07      | From Hartree-Fock to spectroscopic factors $< 1$ : inclusion of long-range correlations |
| Lecture 3: 8/29/07      | Role of short-range and tensor correlations associated with realistic interactions      |
| Lecture 4: 8/30/07      | Dispersive optical model and predictions for nuclei towards the dripline                |
| Adv. Lecture 1: 8/30/07 | Saturation problem of nuclear matter & pairing in nuclear and neutron matter            |
| Adv. Lecture 2: 8/31/07 | Quasi-particle density functional theory  |

Wim Dickhoff  
Washington University in St. Louis

# The two "most elusive" numbers in nuclear physics

- What are these numbers?
- In what sense are they elusive?
- What is the history?
- Three-body forces? Relativity? Give up?
- What has been learned from  $(e, e' p)$ ?
- What really decides the saturation density?
- Nuclear Matter with SRC? No LRC?
- Conclusions

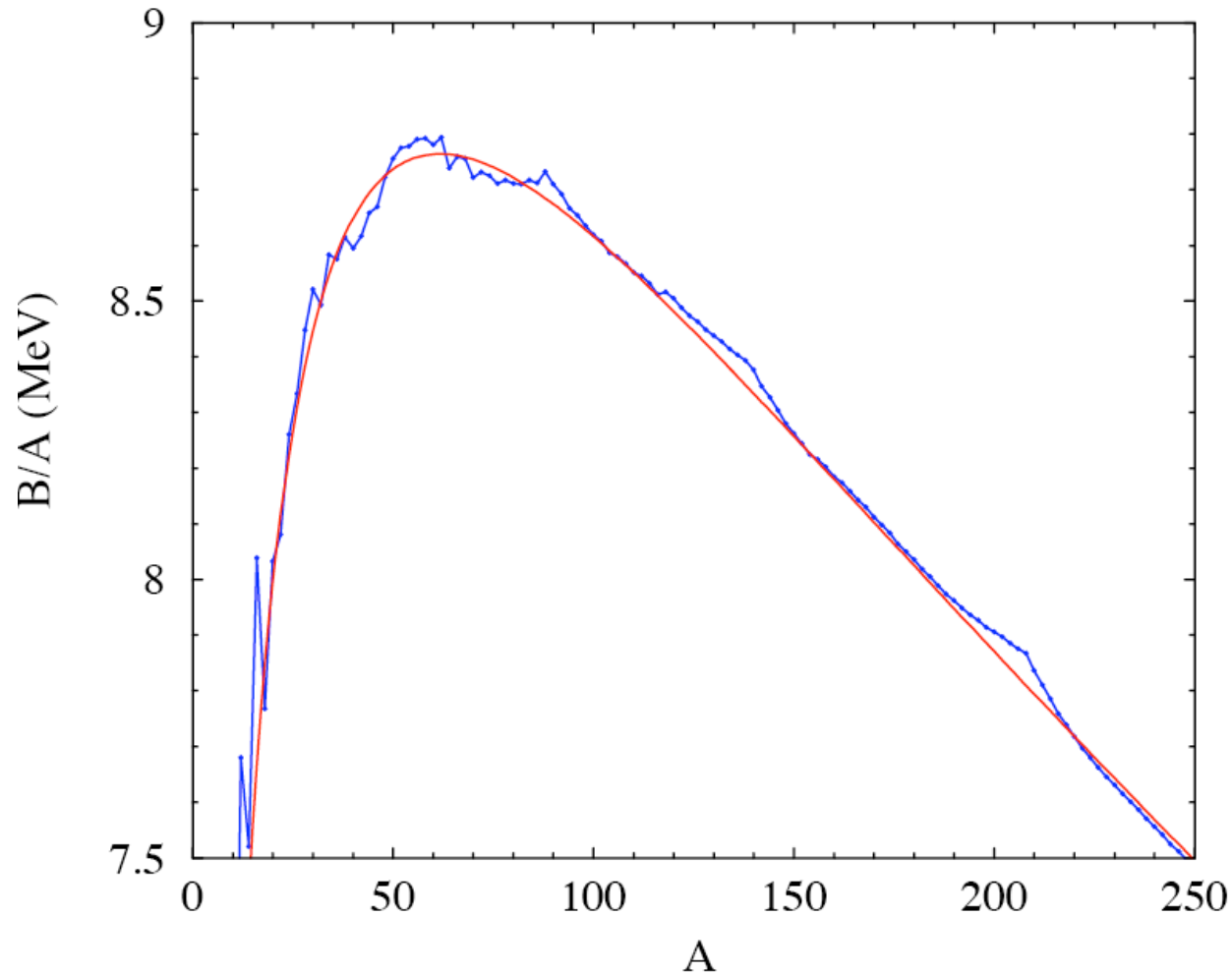
# Empirical Mass Formula

Global representation of nuclear masses (Bohr & Mottelson)

$$B = b_{vol}A - b_{surf}A^{2/3} - \frac{1}{2}b_{sym}\frac{(N-Z)^2}{A} - \frac{3}{5}\frac{Z^2e^2}{R_c}$$

- Volume term  $b_{vol} = 15.56 \text{ MeV}$
- Surface term  $b_{surf} = 17.23 \text{ MeV}$
- Symmetry energy  $b_{sym} = 46.57 \text{ MeV}$
- Coulomb energy  $R_c = 1.24 A^{1/3} \text{ fm}$
- Pairing term must also be considered

# Empirical Mass Formula



Plotted: most stable nucleus for a given  $A$

Green's function V 4

# Central density of nuclei

Multiply charge density at the origin by  $A/Z$

⇒ Empirical density = 0.16 nucleons / fm<sup>3</sup>

⇒ Equivalent to  $k_F = 1.33 \text{ fm}^{-1}$

## *Nuclear Matter*

$$N = Z$$

No Coulomb

$A \Rightarrow \infty, V \Rightarrow \infty$  but  $A/V = \rho$  fixed

“Two most important numbers”

$$b_{vol} = 15.56 \text{ MeV and } k_F = 1.33 \text{ fm}^{-1}$$

# Historical Perspective

- First attempt using scattering in the medium
  - Formal development (linked cluster expansion)
  - Low-density expansion
  - Reorganized perturbation expansion (60s)  
involving ordering in the number of hole lines
  - Variational Theory vs. Lowest Order *BBG* (70s)
  - Variational results & next hole-line terms (80s)
  - Three-body forces? Relativity? (80s)
  - Confirmation of three hole-line results (90s)
  - New insights from experiment  
about what nucleons are up to in the nucleus (90s & 00s)
- Brueckner 1954*  
*Goldstone 1956*  
*Galitskii 1958*  
*Bethe & students*  
*BBG-expansion*  
*Clark, Pandharipande*  
*Day, Wiringa*  
*Urbana, CUNY*  
*Baldo et al.*  
**NIKHEF Amsterdam**  
*JLab*

# Old pain and suffering!

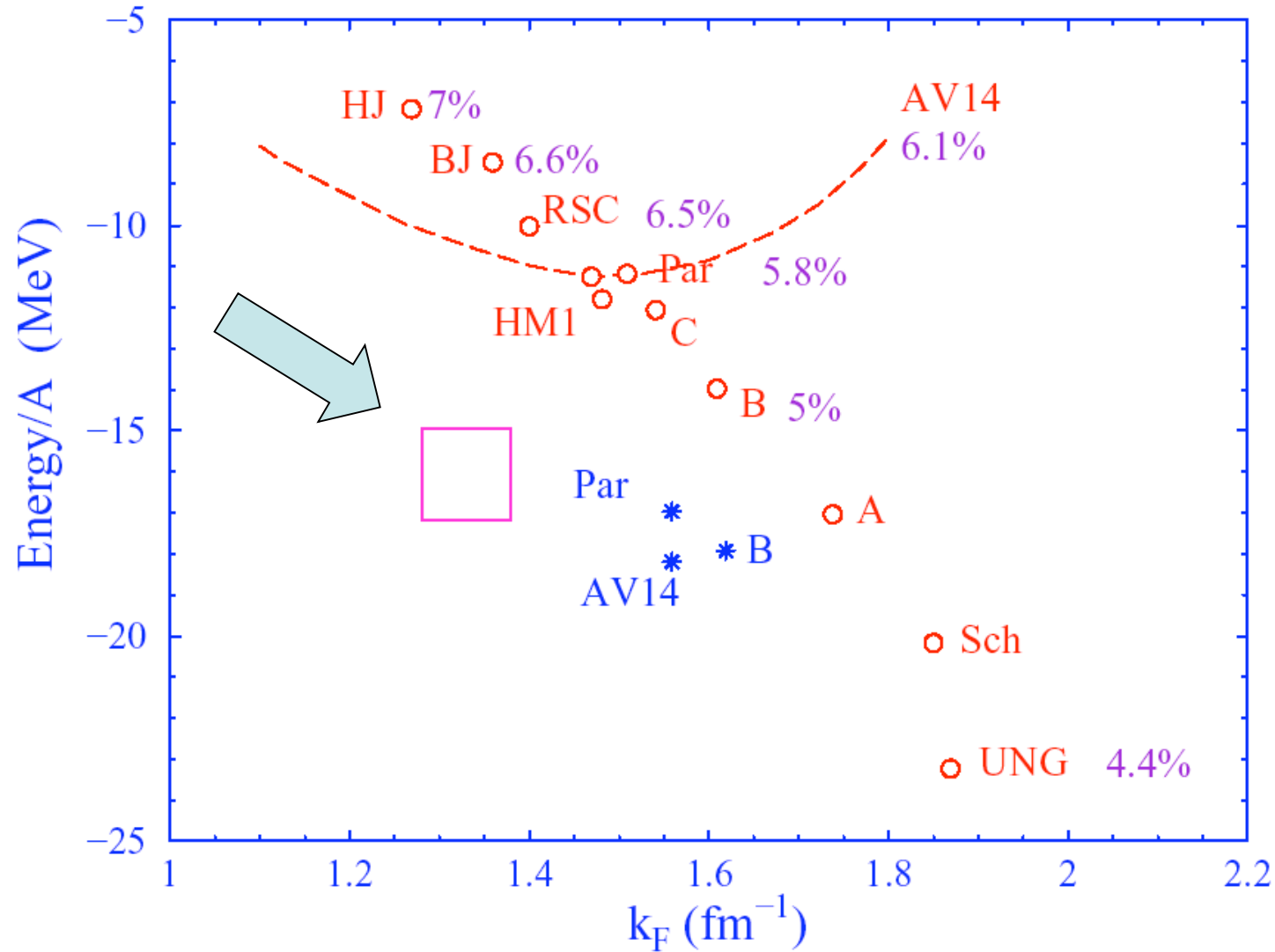
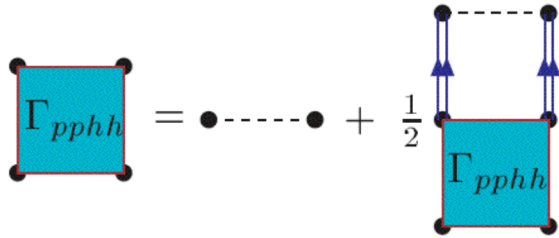


Figure adapted from Marcello Baldo (Catania)

# Lowest-order Brueckner theory (two hole lines)



$G_{BG}^f$  angle-average of

$$G_{BG}^f(k_1, k_2; E) = \frac{\theta(k_1 - k_F)\theta(k_2 - k_F)}{E - \varepsilon(k_1) - \varepsilon(k_2) + i\eta}$$

$$\langle k\ell | G^{JST}(K, E) | k'\ell' \rangle = \langle k\ell | V^{JST} | k'\ell' \rangle + \frac{1}{2} \sum_{\ell''} \int_0^\infty \frac{dq}{(2\pi)^3} q^2 \langle k\ell | V^{JST} | q\ell'' \rangle G_{BG}^f(q, K, E) \langle q\ell'' | G^{JST}(K, E) | k'\ell' \rangle$$

**Spectrum**  $\varepsilon_{BHF}(k) = \frac{\hbar^2 k^2}{2m} + \Sigma_{BHF}(k; \varepsilon_{BHF}(k))$   $k < k_F \Rightarrow$  standard choice  
 $\text{all } k \Rightarrow$  continuous choice

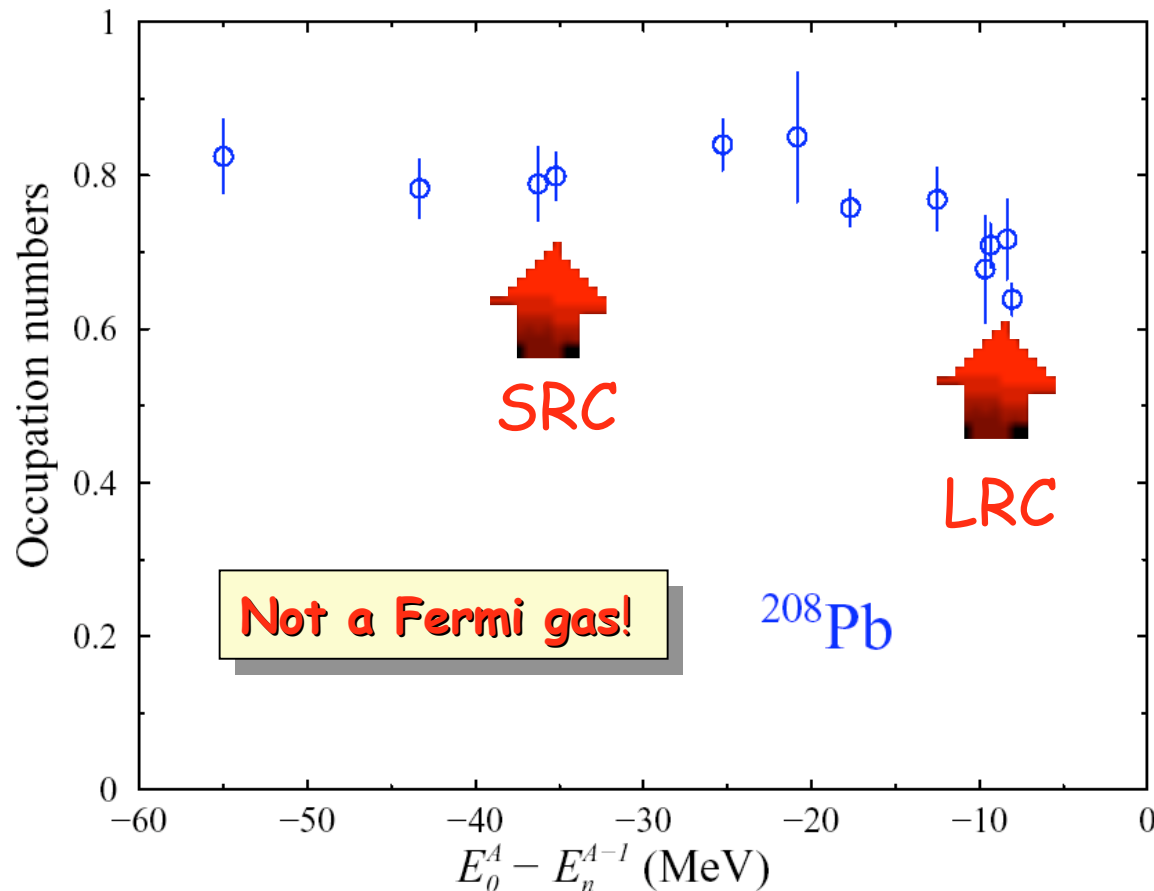
**Self-energy**  $\Sigma_{BHF}(k; E) = \frac{1}{v} \sum_{m, m'} \int \frac{d^3 k'}{(2\pi)^3} \theta(k_F - k') \langle \vec{k}\vec{k}' mm' | G(\vec{k} + \vec{k}'; E + \varepsilon_{BHF}(k')) | \vec{k}\vec{k}' mm' \rangle$

**Energy**  $\frac{E}{A} = \frac{4}{\rho} \int \frac{d^3 k}{(2\pi)^3} \theta(k_F - k) \frac{\hbar^2 k^2}{2m}$   
 $+ \frac{1}{2\rho} \sum_{m, m'} \int \frac{d^3 k}{(2\pi)^3} \theta(k_F - k) \int \frac{d^3 k'}{(2\pi)^3} \theta(k_F - k') \langle \vec{k}\vec{k}' mm' | G(\vec{k} + \vec{k}'; \varepsilon_{BHF}(k) + \varepsilon_{BHF}(k')) | \vec{k}\vec{k}' mm' \rangle$



M. van Batenburg (thesis, 2001) & L. Lapikás from  $^{208}\text{Pb} (e, e' p) ^{207}\text{Tl}$

## Occupation of deeply-bound proton levels from EXPERIMENT



Up to 100 MeV  
missing energy  
and  
270 MeV/c  
missing momentum

Covers the whole  
mean-field domain  
for the FIRST time!!

Confirmation of theory

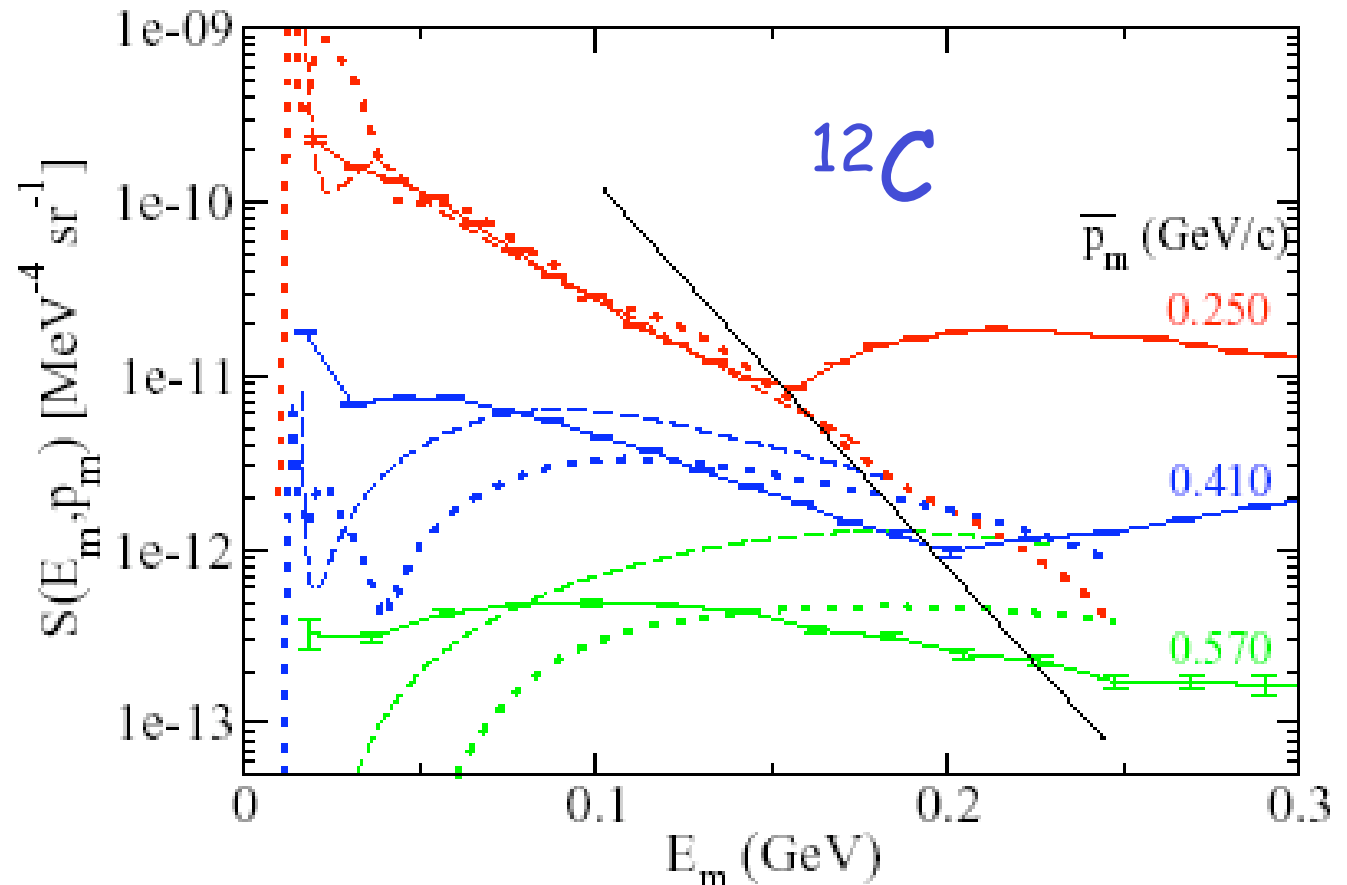
Green's function V 9

# Where are the last protons? Answer is coming!

Jlab data  
PRL93,182501 (2004)  
Rohe et al.

Location of high-momentum component

integrated strength OK!



There are high-momentum components  
in the nuclear ground state!

Green's function V 10

## Energy Sum Rule (Migdal, Galitskii, Koltun ...)

Finite nuclei

$$E_0^A = \langle \Psi_0^A | \hat{H} | \Psi_0^A \rangle = \frac{1}{2} \sum_{\alpha\beta} \langle \alpha | T | \beta \rangle n_{\alpha\beta} + \frac{1}{2} \sum_{\alpha} \int_{-\infty}^{\varepsilon_F} dE E S_h(\alpha; E)$$

$$n_{\alpha\beta} = \langle \Psi_0^A | a_{\alpha}^+ a_{\beta} | \Psi_0^A \rangle = \frac{1}{\pi} \int_{-\infty}^{\varepsilon_F} dE \operatorname{Im} G(\beta, \alpha; E)$$

$$S_h(\alpha; E) = \sum_n \left| \langle \Psi_n^{A-1} | a_{\alpha} | \Psi_0^A \rangle \right|^2 \delta(E - (E_0^A - E_n^{A-1})) = \frac{1}{\pi} \operatorname{Im} G(\alpha, \alpha; E)$$

Nuclear matter

$$\frac{E}{A} = \frac{1}{2} \left\{ \frac{4}{\rho} \int \frac{d^3k}{(2\pi)^3} \int_{-\infty}^{\varepsilon_F} dE \left( \frac{\hbar^2 k^2}{2m} + E \right) S_h(k; E) \right\}$$

- Presumes only two-body interactions!
- Correct description of experimental spectral function should yield good  $E/A$ !!

# Where does binding come from (really)?

$^{16}\text{O}$  PRC51,3040(1995)

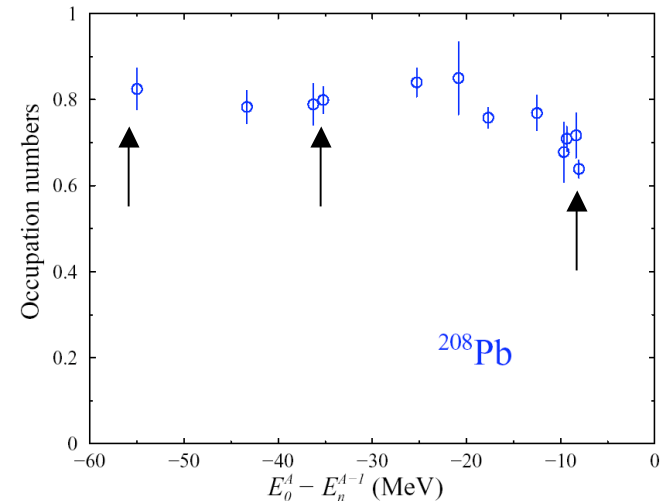
$lj$	"BHF"			Total			
	$\epsilon$	$t$	$\Delta E$	$\epsilon$	$t$	$\Delta E$	
$s_{\frac{1}{2}} \text{ qh}$	-36.9	11.8	-50.3	-34.3	11.2	-36.0	
$s_{\frac{1}{2}} \text{ c}$				-90.4	17.1	-22.9	←
$p_{\frac{3}{2}} \text{ qh}$	-15.4	17.6	9.1	-17.9	18.1	0.4	
$p_{\frac{3}{2}} \text{ c}$				-95.2	35.2	-10.0	←
$p_{\frac{1}{2}} \text{ qh}$	-11.5	16.6	10.3	-14.1	17.2	5.5	
$p_{\frac{1}{2}} \text{ c}$				-103.6	35.9	-5.8	←
$\ell > 1 \text{ c}$				-98.9	63.2	-12.3	←
$E/A(\text{MeV})$		-1.9			-5.1		
$\langle r \rangle(\text{fm})$		2.59			2.55		

Quasiholes contribute 37% to the total energy  
 High-momentum nucleons (continuum) contribute 63%  
 but represent only about 10% of the particles!!

Green's function V 12

# Saturation density and SRC

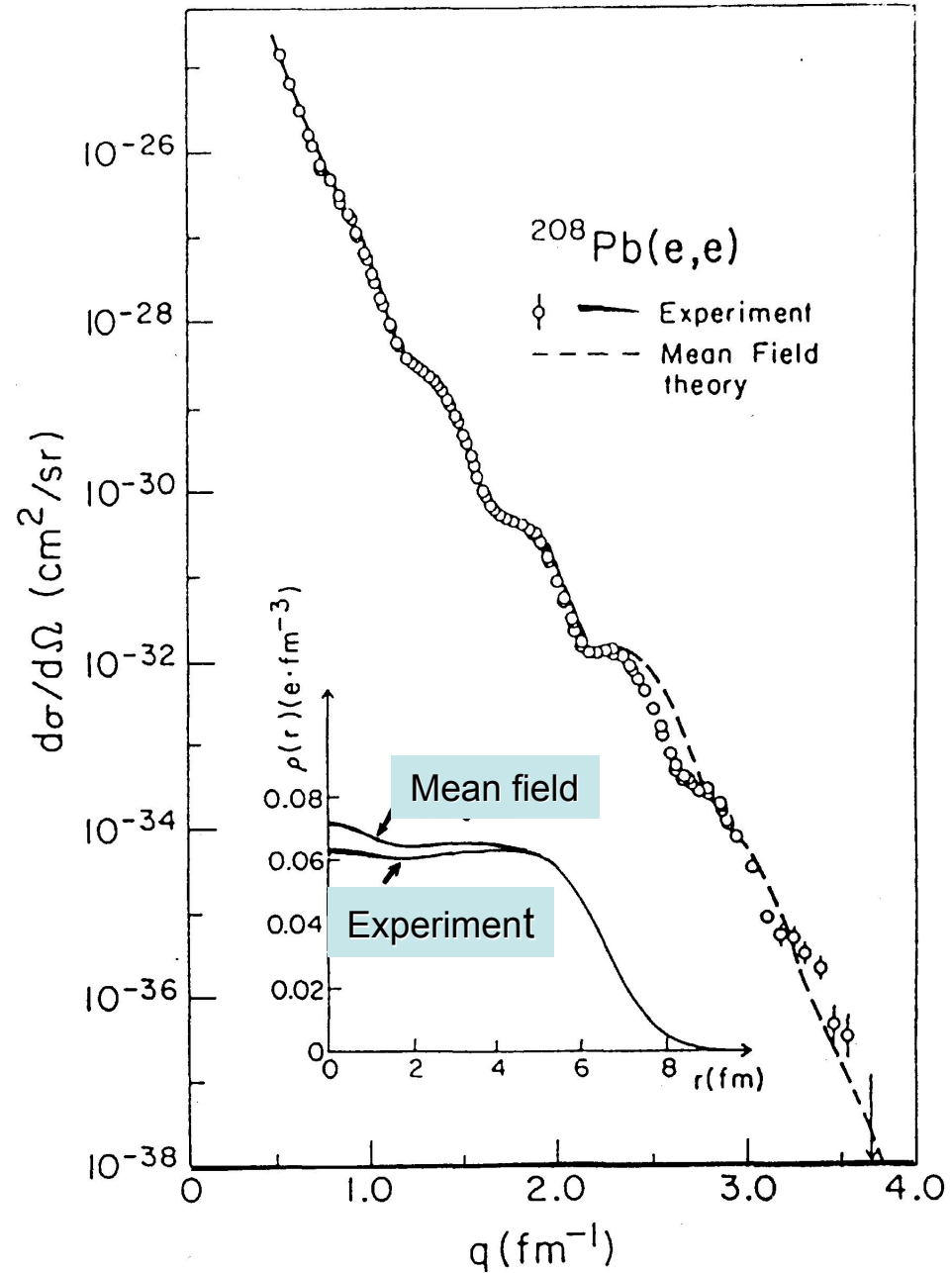
- Saturation density related to nuclear charge density at the origin. Data for  $^{208}\text{Pb} \Rightarrow A/Z * \rho_{\text{ch}}(0) = 0.16 \text{ fm}^{-3}$
- Charge at the origin determined by protons in  $s$  states
- Occupation of  $0s$  and  $1s$  totally dominated by SRC as can be concluded from recent analysis of  $^{208}\text{Pb}(e, e' p)$  data and theoretical calculations of occupation numbers in nuclei and nuclear matter.
- Depletion of  $2s$  proton also dominated by SRC: 15% of the total depletion of 25% ( $n_{2s} = 0.75$ )



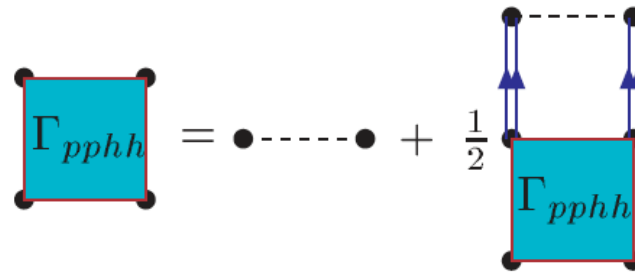
- **Conclusion: Nuclear saturation dominated by SRC  
and therefore high-momentum components**

# Elastic electron scattering from $^{208}\text{Pb}$

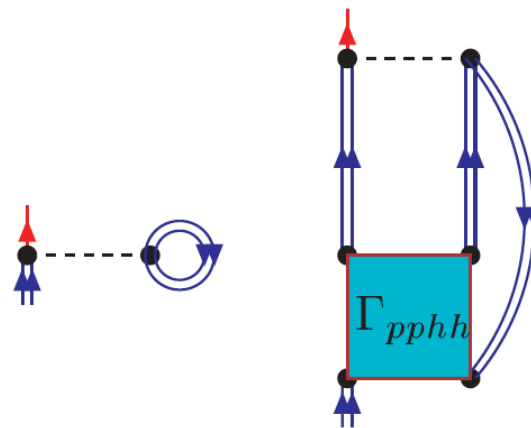
B. Frois *et al.*  
Phys. Rev. Lett. **38**, 152 (1977)



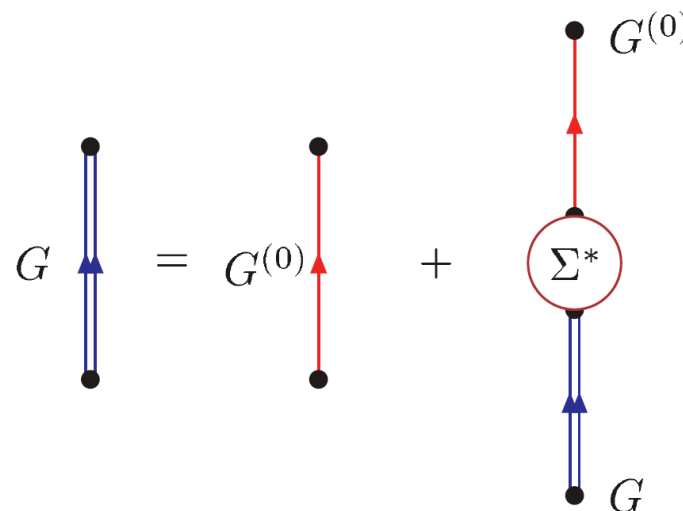
Self-consistent  
treatment of  
SRC  
in nuclear matter



Interaction



Self-energy

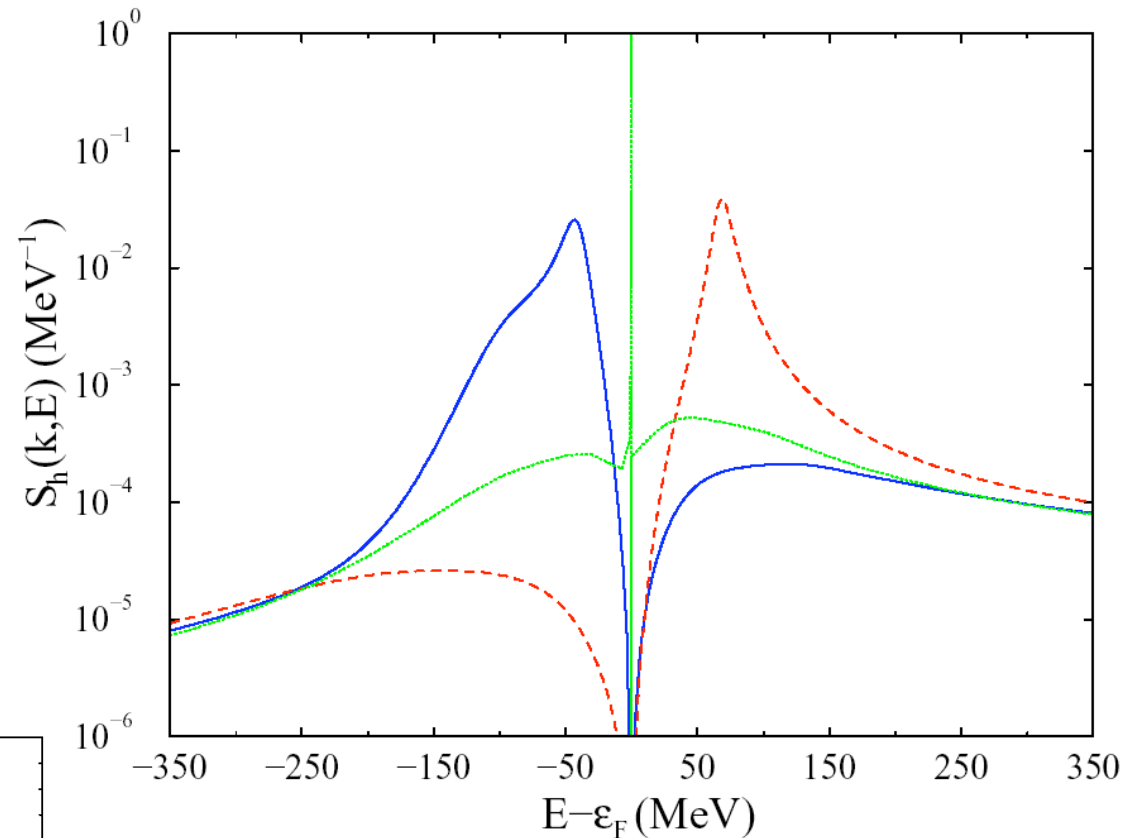
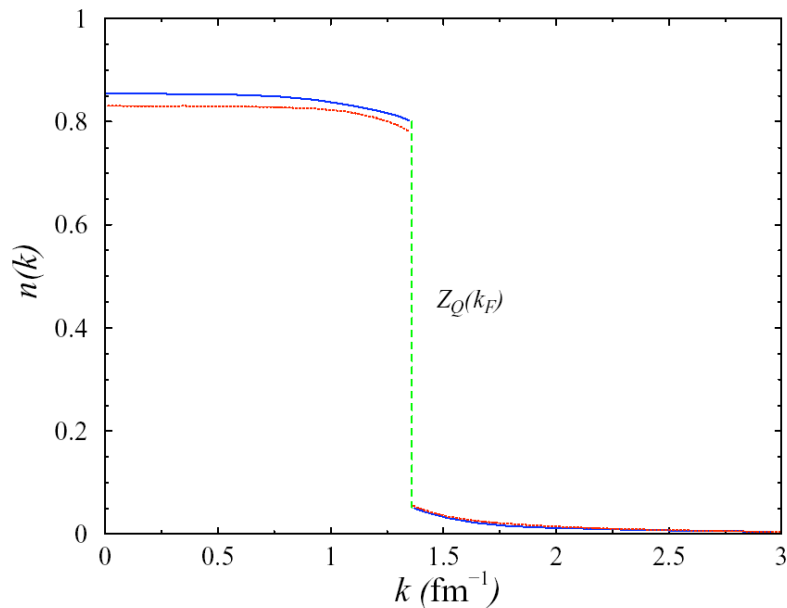


Dyson equation

Green's function V 15

# Results from Nuclear Matter 2nd generation (2000)

- Spectral functions for  $k = 0, 1.36, \text{ \& } 2.1 \text{ fm}^{-1}$
- Common tails on both sides of  $\varepsilon_F$



Momentum distribution :

only minor changes

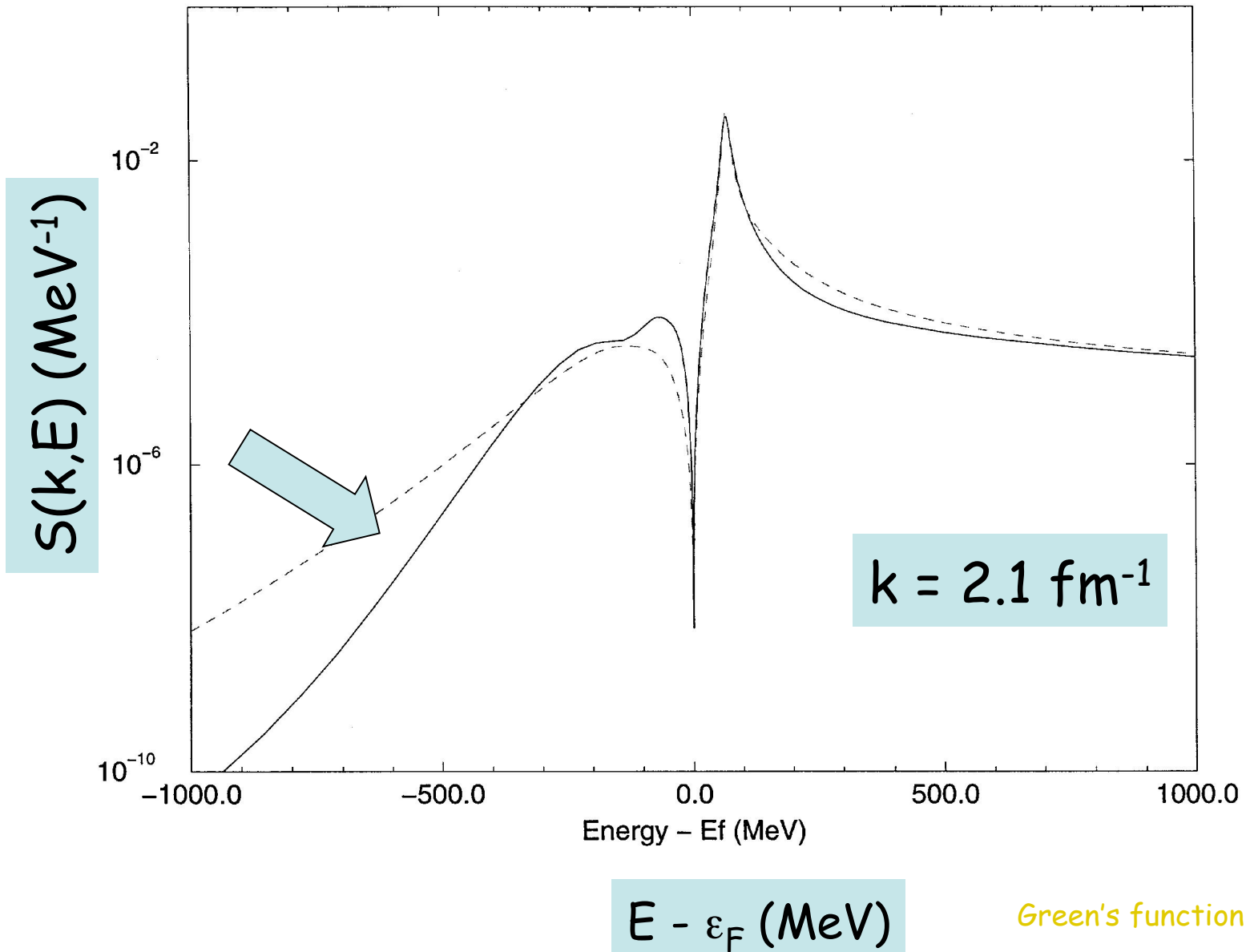
occupation in nuclei

depleted similarly!?!

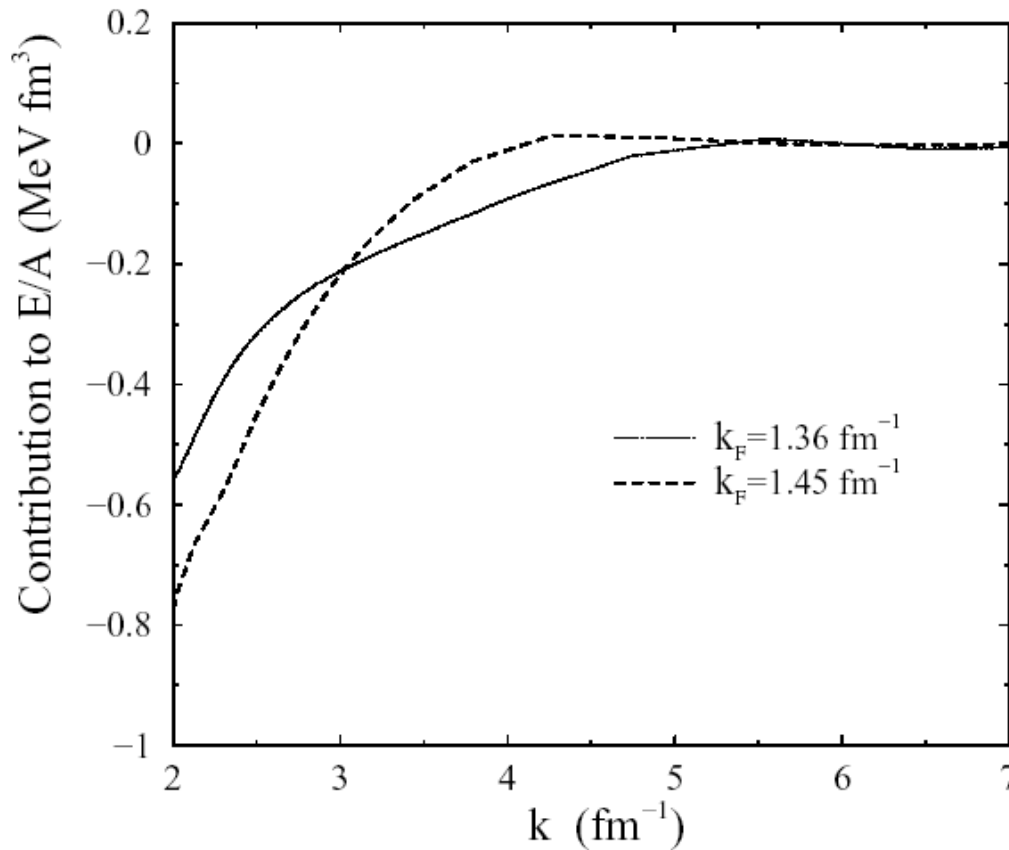
Green's function V 16



# Self-consistent spectral functions



Saturation with self-consistent spectral functions  
in nuclear matter  $\Rightarrow$  reasonable saturation properties



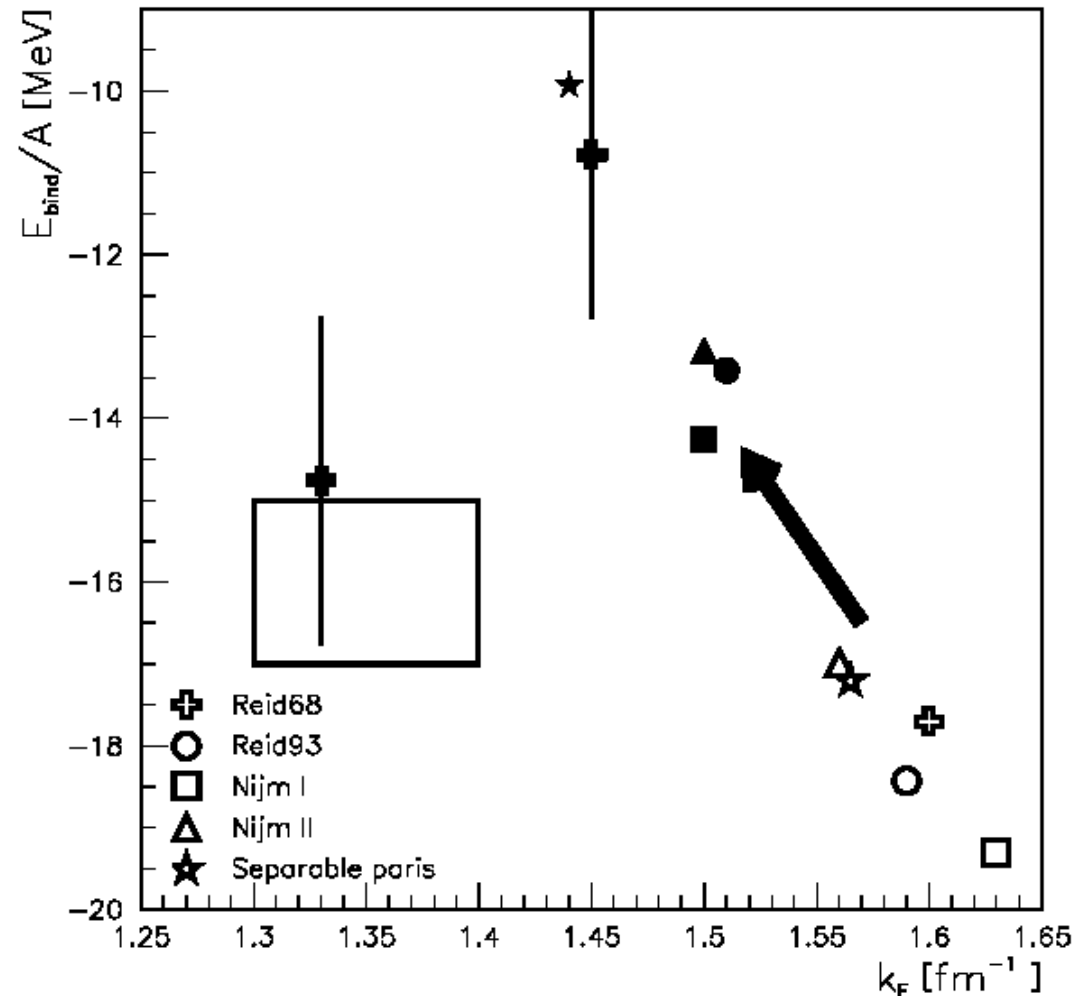
Contribution to the energy per particle before integration over the  
single-particle momentum at high momentum for two densities

Green's function V 18

# Saturation of Nuclear Matter

## Ladders and self-consistency for Nuclear Matter

- Ghent group  
Dewulf, Van Neck &  
Waroquier
- St. Louis  
Stoddard, WD



Phys. Rev. Lett. 90, 152501 (2003)

Green's function V 19

# Self-consistent spectral functions

- Distribution below  $\varepsilon_F$  broadens for high momenta and develops a common tail at high missing energy
- Slight increase in occupation  $k < k_F$  to 85% at  $k_F = 1.36 \text{ fm}^{-1}$  compared to Phys. Rev. **C44**, R1265 (1991) & Nucl. Phys. **A555**, 1 (1993)
- Self-consistent treatment of Pauli principle
- Interaction between dressed particles weaker (reduced cross sections for both pn and nn)
- Pairing instabilities disappear in all channels
- Saturation with lower density than before and reasonable binding
- **Contribution of long-range correlations excluded**

# Self-consistent Green's functions and the energy of the ground state of the electron gas



GW approximation

$G$  self-consistent sp propagator

$W$  screened Coulomb interaction

$\Rightarrow$  RPA with dressed sp propagators

Electron gas : -XC energies (Hartrees)

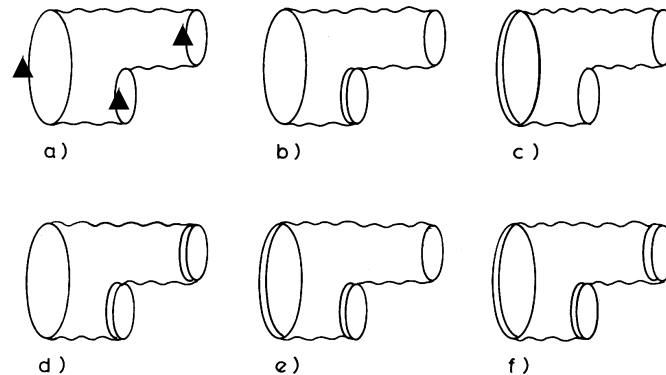
<u>Method</u>	$r_s = 1$	$r_s = 2$	$r_s = 4$	$r_s = 5$	$r_s = 10$	$r_s = 20$	Reference
QMC	0.5180	0.2742	0.1464	0.1197	0.0644	0.0344	CA80
	0.5144	0.2729	0.1474	0.1199	0.0641	0.0344	OB94;OHB99
GW	0.5160	0.2727	0.1450	0.1185	0.0620	0.032	GG01
		0.2741	0.1465				HB98
RPA	0.5370	0.2909	0.1613	0.1340	0.0764	0.0543	Green's function V 21

# What about long-range correlations in nuclear matter?

- Collective excitations in nuclei very different from those in nuclear matter
- Long-range correlations normally associated with small  $q$
- Contribution to the energy like  $dq q^2 \Rightarrow$  very small (except for e-gas)
- Contributions of collective excitations to the binding energy of nuclear matter dominated by pion-exchange induced excitations?!?

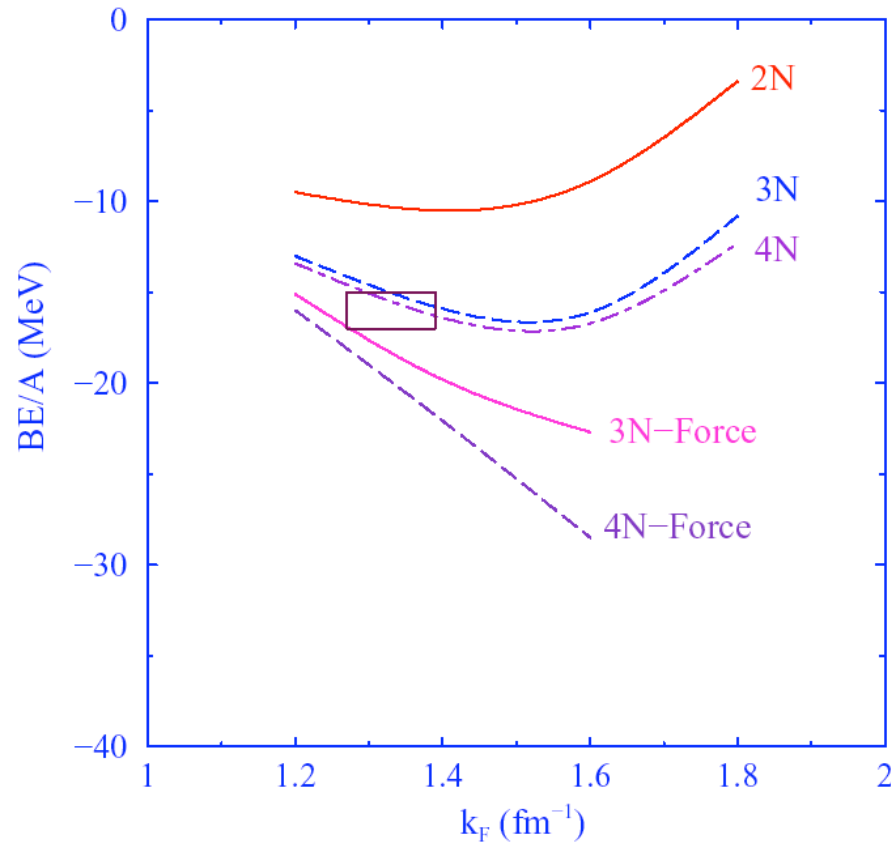
# Inclusion of $\Delta$ -isobars as "3N-" and "4N-force"

Nucl. Phys. A389, 492 (1982)



$k_F$ [fm <sup>-1</sup> ]	1.0	1.2	1.4	1.6
third order				
a)	-0.303	-1.269	-3.019	-5.384
b)	-0.654	-1.506	-2.932	-5.038
c)	-0.047	-0.164	-0.484	-1.175
d)	0.033	0.095	0.220	0.447
e)	-0.104	-0.264	-0.589	-1.187
f)	0.041	0.137	0.385	0.962
Sum	-1.034	-2.971	-6.419	-11.375

# Inclusion of $\Delta$ -isobars as 3N- and 4N-force



2N,3N, and 4N from  
B.D.Day, PRC24,1203(81)

Rings with  $\Delta$ -isobars :

Nucl. Phys. A389, 492 (1982)

PPNPhys 12, 529 (1983)

**$\Rightarrow$  No sensible convergence with  $\Delta$ -isobars**



# Nuclear Saturation without $\pi$ -collectivity

- Variational calculations treat LRC (on average) and SRC simultaneously (Parquet equivalence) so **difficult** to separate LRC and SRC
- Remove 3-body ring diagram from Catania hole-line expansion calculation  $\Rightarrow$  about the correct saturation density
- Hole-line expansion doesn't treat Pauli principle very well
- Present results improve treatment of Pauli principle by self-consistency of spectral functions  $\Rightarrow$  more reasonable saturation density and binding energy acceptable
- Neutron matter: pionic contributions must be included ( $\Delta$ )

# Pion collectivity: nuclei vs. nuclear matter

- Pion collectivity leads to pion condensation at higher density in nuclear matter (including  $\Delta$ -isobars)  $\Rightarrow$  Migdal ...
- No such collectivity observed in nuclei  $\Rightarrow$  LAMPF / Osaka data
- Momentum conservation in nuclear matter dramatically favors amplification of  $\pi$ -exchange interaction at fixed  $q$
- In nuclei the same interaction is sampled over all momenta Phys. Lett. **B146**, 1(1984)

$$V_{\pi}(q) = -\frac{f_{\pi}^2}{m_{\pi}^2} \frac{q^2}{m_{\pi}^2 + q^2}$$

Needs further study

$\Rightarrow$  Exclude collective pionic contributions to nuclear matter binding energy

# Two Nuclear Matter Problems

## The usual one

- With  $\pi$ -collectivity and only nucleons
- Variational + CBF and three hole-line results presumed OK (for  $E/A$ ) but not directly relevant for comparison with nuclei!
- **NOT OK** if  $\Delta$ -isobars are included
- Relevant for neutron matter

## The relevant one?!

- Without  $\pi$ -collectivity
- Treat only SRC
- But at a sophisticated level by using self-consistency
- Confirmation from Ghent results  $\Rightarrow$  Phys. Rev. Lett. **90**, 152501 (2003)
- 3N-forces difficult  $\Rightarrow \pi \dots$
- Relativity?

# Comments

## Relativity

- Saturation depends on  $NN\sigma$ -coupling in medium but underlying correlated two-pion exchange behaves differently in medium
- $m^* \rightarrow 0$  with increasing  $\rho$  opposite in liquid  ${}^3\text{He}$  appears unphysical
- Dirac sea under control?
- $sp$  strength overestimated too many nucleons for  $k < k_F$

## Three-body forces

- Microscopic models yield only attraction in matter and more so with increasing  $\rho$
- Microscopic background of phenomenological repulsion in 3N-force (if it exists)?
- 4N-, etc. forces yield increasing attraction with  $\rho$
- Needed in light nuclei and attractive!
- Mediated by  $\pi$ -exchange
- Argonne group can't get nuclear matter right with new 3N-force

Green's function V 28

# Conclusions

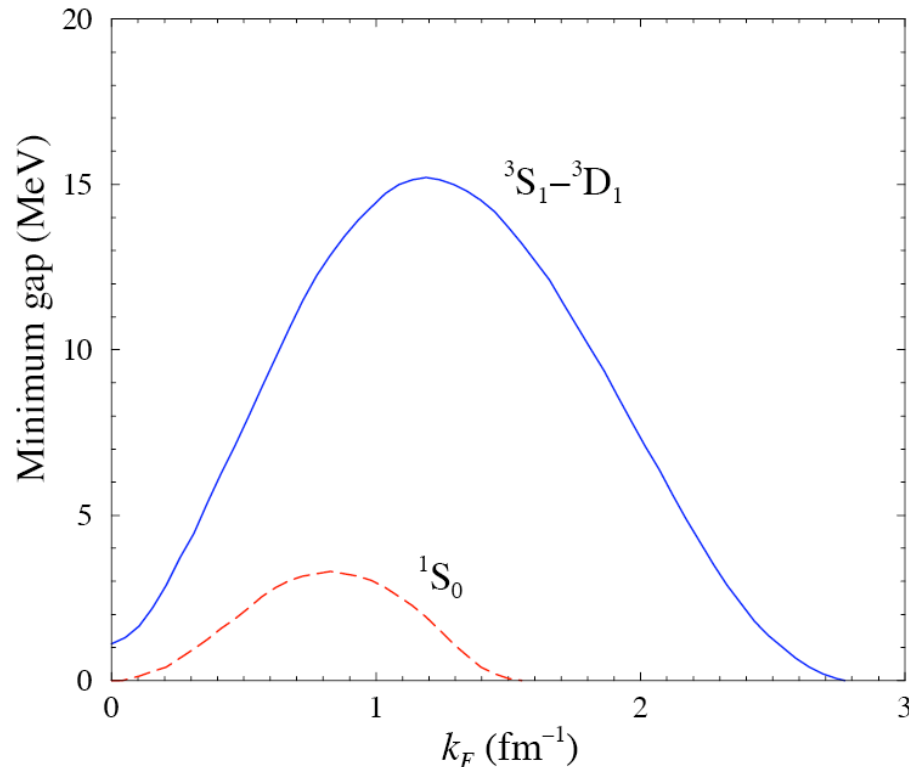
- Good understanding of role of short-range correlations
  - Depletion of Fermi sea: nuclear matter OK for nuclei
    - **Confirmed by experiment**
    - High-momentum components
      - **# of protons experimentally confirmed**
- Long-range correlations crucial for distribution of  $sp$  strength
- Energy per particle from self-consistent Green's functions
- Better understanding of nuclear matter saturation  
⇒ SRC dominate (don't treat LRC from pions)
- **We know what protons are up to in nuclei!!**

# Some pairing issues in infinite matter

- Gap size in nuclear matter & neutron matter
- Density & temperature range of superfluidity
- Resolution of  ${}^3S_1$ - ${}^3D_1$  puzzle (size of pn pairing gap)
- Influence of short-range correlations (SRC)
- Influence of polarization contributions
- Relation of infinite matter results & finite nuclei

Review: e.g. Dean & Hjorth-Jensen, RMP75, 607 (2003)

# Puzzle related to gap size in ${}^3S_1$ - ${}^3D_1$ channel



Mean-field particles

Early nineties: BCS gaps  $\sim 10$  MeV

Alm et al. Z.Phys.A337,355 (1990)

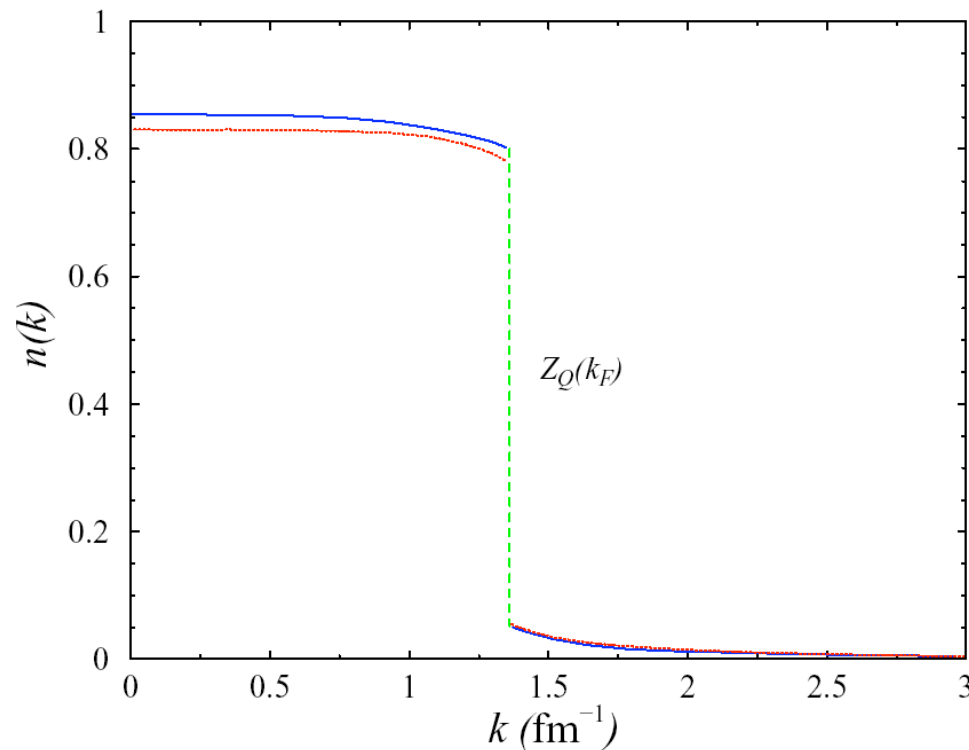
Vonderfecht et al. PLB253,1 (1991)

Baldo et al. PLB283, 8 (1992)

Dressing nucleons is expected to reduce pairing strength as suggested by in-medium scattering

# Results from Nuclear Matter (N=Z)

2nd generation (2000)



Momentum distribution: only minor changes  
when self-consistency is included

Occupation in nuclei: Depleted similarly!

Thesis Libby Roth Stoddard (2000)

Green's function V 32

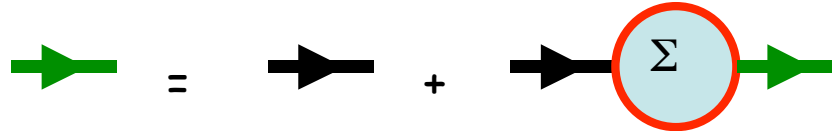


# Green's function and $\Gamma$ -matrix approach (ladders)

Single-particle Green's function

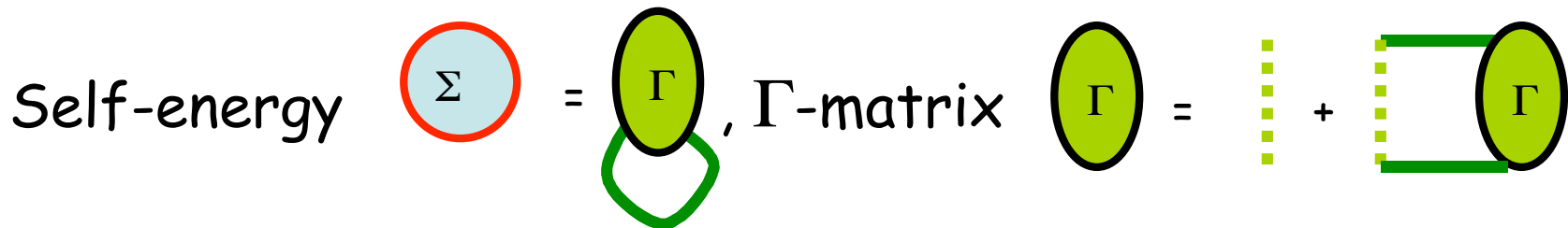
$$G(k, t_1, t_2) = -i \langle T c_k(t_1) c_k^\dagger(t_2) \rangle$$

Dyson equation:



$$G(k, \omega) = G^{(0)}(k, \omega) + G^{(0)}(k, \omega) \Sigma(k, \omega) G(k, \omega)$$

$$G(k, \omega) = \frac{1}{\omega - k^2 / 2m - \Sigma(k, \omega)} \Rightarrow S(k, \omega) = -2 \text{Im} G(k, \omega)$$

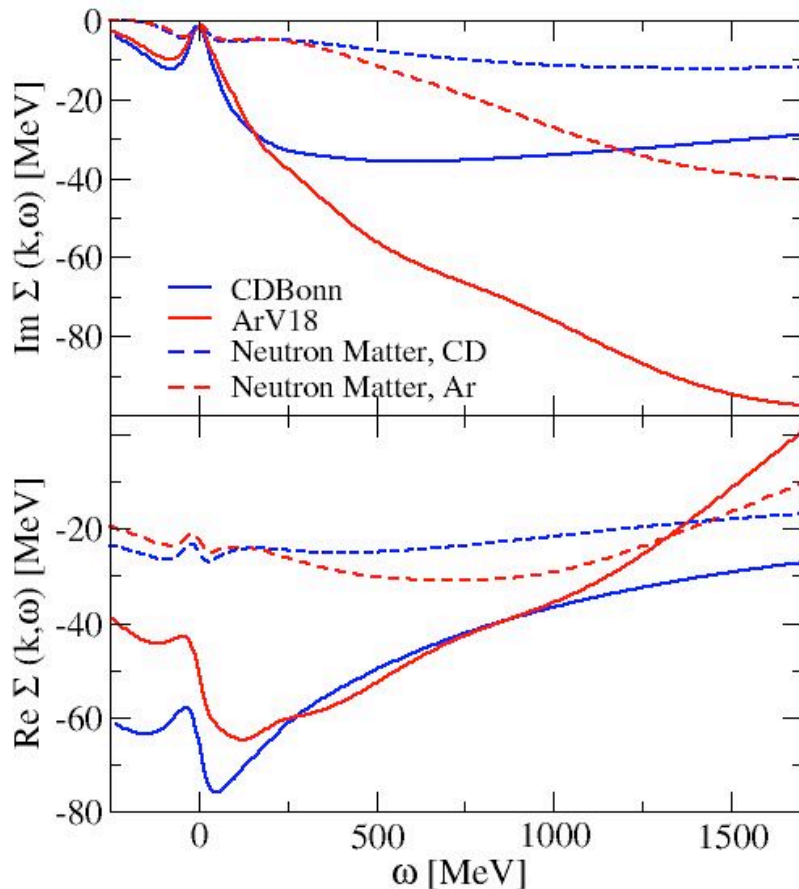


- Pairing instability possible
- Finite temperature calculation can avoid this

# Self-energy

$$G(k, \omega) = \frac{1}{\omega - k^2/2m - \Sigma(k, \omega)}$$

$$\Rightarrow S(k, \omega) = -2\text{Im}G(k, \omega)$$



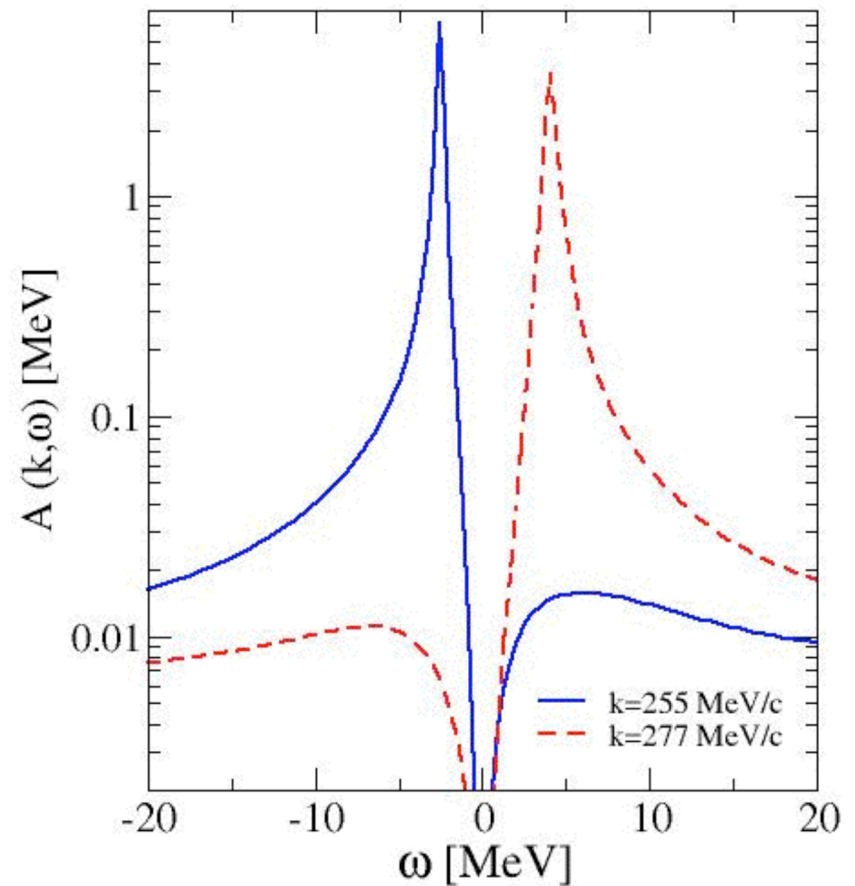
Real and imaginary part of the retarded self-energy

- $k_F = 1.35 \text{ fm}^{-1}$
- $T = 5 \text{ MeV}$
- $k = 1.14 \text{ fm}^{-1}$

Note differences due to NN interaction

# Spectral functions

- Strength above and below the Fermi energy as in BCS
- But broad distribution in energy
- BCS not just a cartoon of SCGF but both features must be considered in a consistent way
- CDBonn interaction at "T=0"



# BCS: a reminder

NN correlations on top of Hartree-Fock:  $\epsilon_k, c_k^+$

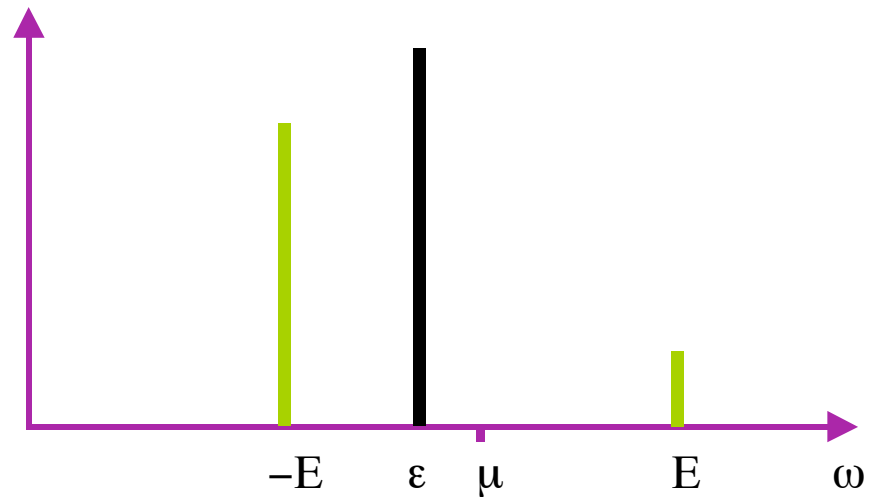
Bogoliubov transformation  $a_k^+ = u_k c_k^+ + v_k c_{\bar{k}}$

with 
$$\begin{matrix} u_k^2 \\ v_k^2 \end{matrix} = \frac{1}{2} \left[ 1 \pm \frac{\epsilon_k - \mu}{\sqrt{(\epsilon_k - \mu)^2 + \Delta(k)^2}} \right], \quad E(k) = \sqrt{(\epsilon_k - \mu)^2 + \Delta(k)^2}$$

Gap equation

$$\Delta(k) = \int k'^2 dk' \langle k, \bar{k} | V | k', \bar{k}' \rangle \frac{\Delta(k')}{-2E(k)}$$

Spectral function  $S(k, \omega)$



# Solution of the gap equation

$$\Delta(k) = \sum_{k'} \langle k, \bar{k} | V | k', \bar{k}' \rangle \frac{\Delta(k')}{\omega - 2E(k)} \quad \text{with} \quad E(k) = \sqrt{(\epsilon_k - \mu)^2 + \Delta(k)^2} \quad \text{and} \quad \omega=0$$

Define: 
$$\delta(k) = \frac{\Delta(k)}{\omega - 2E(k)}$$

$$\begin{pmatrix} 2E(k) + \langle k | V | k \rangle, & \dots, & \langle k | V | k' \rangle \\ \vdots & \ddots & \vdots \\ \langle k' | V | k \rangle, & \dots, & 2E(k') + \langle k' | V | k' \rangle \end{pmatrix} \begin{pmatrix} \delta(k) \\ \vdots \\ \delta(k') \end{pmatrix} = \omega \begin{pmatrix} \delta(k) \\ \vdots \\ \delta(k') \end{pmatrix}$$

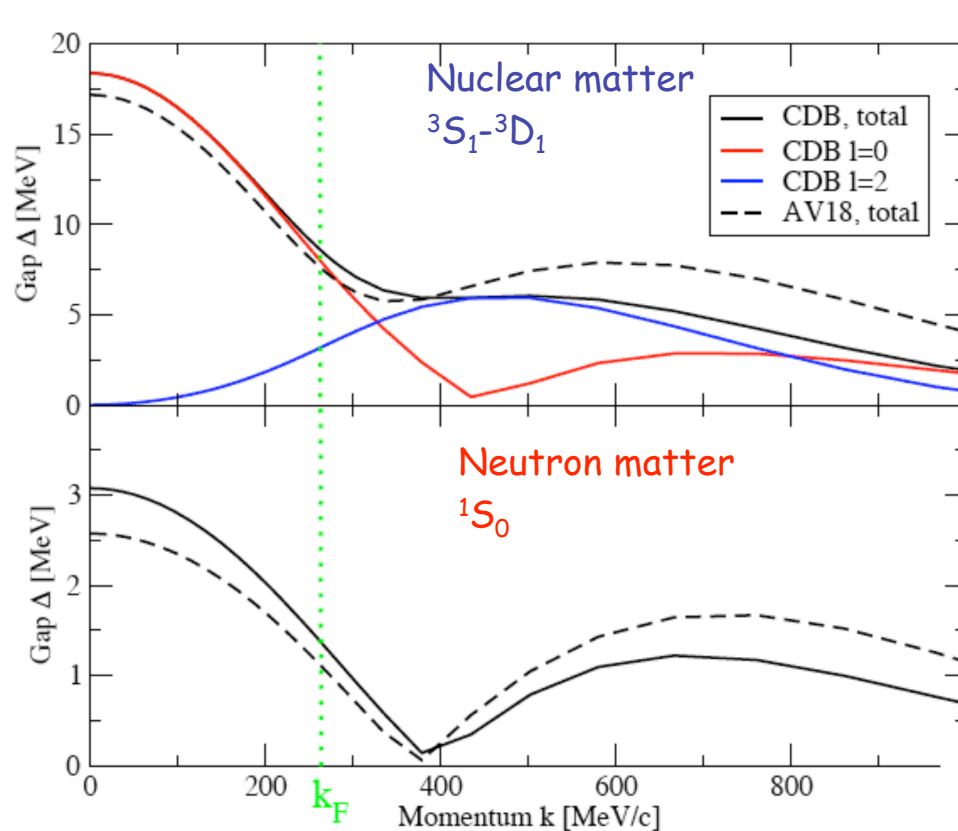
*Eigenvalue problem for a pair of nucleons at  $\omega=0$*

Steps of the calculation:

- \* Assume  $\Delta(k)$  and determine  $E(k)$
- \* Solve eigenvalue equation and evaluate new  $\Delta(k)$ 
  - If lowest eigenvalue  $\omega < 0$  enhance  $\Delta(k)$  (resp.  $\delta(k)$ )
  - If lowest eigenvalue  $\omega > 0$  reduce  $\Delta(k)$

\* Repeat until convergence

# Gaps from BCS for realistic interactions



$T = 0$

Mean-field particles

- momentum dependence  $\Delta(k)$
- different NN interactions
- very similar to pairing gaps in finite nuclei for like particles...!?
- for np pairing no strong empirical evidence...?!

Early nineties: BCS gaps  $\sim 10$  MeV

Alm et al. Z.Phys.A337,355 (1990)  
 Vonderfecht et al. PLB253,1 (1991)  
 Baldo et al. PLB283, 8 (1992)

# Beyond BCS in the framework of SCGF

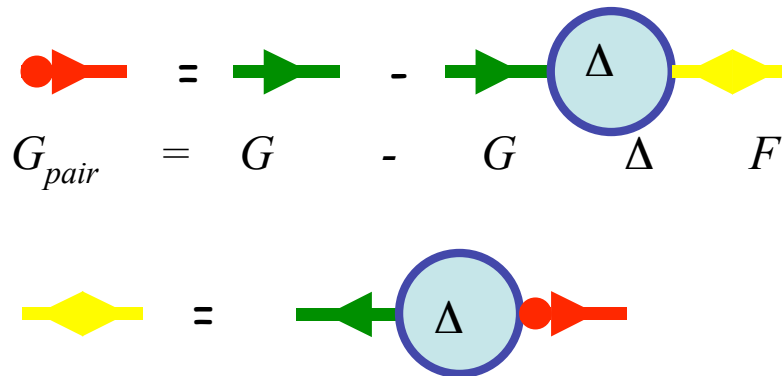
Generalized Green's functions: Extend  $G(k, t_1, t_2) = -i \langle T c_k(t_1) c_k^+(t_2) \rangle$

Anomalous propagators  $G(k, t_1, t_2) = \begin{pmatrix} -i \langle T c c^+ \rangle & -i \langle T c c \rangle \\ i \langle T c^+ c^+ \rangle & i \langle T c^+ c \rangle \end{pmatrix} = \begin{pmatrix} G & F \\ F^+ & \bar{G} \end{pmatrix}$

Generalized Dyson equation: Gorkov equations

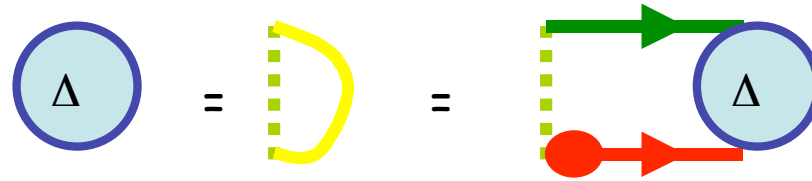
$$\begin{pmatrix} \omega - t_k - \Sigma(k, \omega) & -\Delta(k, \omega) \\ -\Delta^+(k, \omega) & \omega + t_k + \Sigma(k, \omega) \end{pmatrix} \begin{pmatrix} G_{pair}(k, \omega) & F(k, \omega) \\ F^+(k, \omega) & \bar{G}_{pair}(k, \omega) \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$$

Leads to e.g.



$G$  includes all normal self-energy terms

# Anomalous self-energy: $\Delta$ & generalized Gap equation



$$\Delta(k) = \int k'^2 dk' \langle k|V|k' \rangle \int d\omega \int d\omega' \frac{1 - f(\omega) - f(\omega')}{-\omega - \omega'} S(k', \omega) S_{pair}(k', \omega') \Delta(k')$$

$$f(\omega) = \frac{1}{e^{\beta\omega} + 1}$$

Fermi function

If we replace  $S(k, \omega)$  by "HF" approx. and  $S_{pair}(k, \omega)$  by BCS:

⇒ Usual Gap equation

If we take  $S_{pair}(k, \omega) = S(k, \omega)$ :

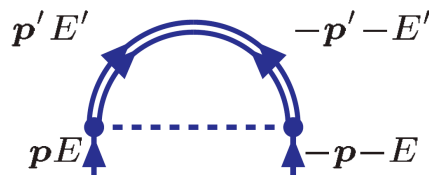
⇒ Corresponds to the homogeneous solution of  $\Gamma$ -matrix eq.

With  $S_{pair}(k, \omega)$ :

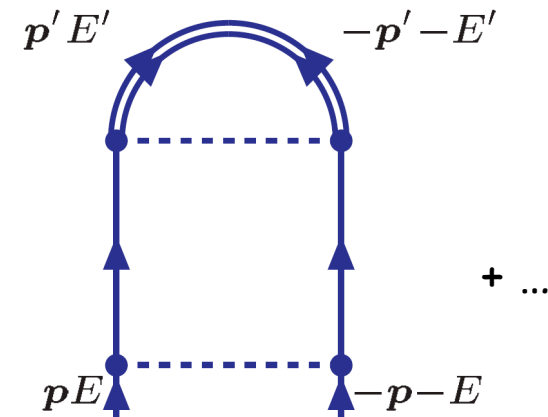
⇒ The above and self-consistency Green's function V 40



# Consistency of Gap equation (anomalous self-energy) and Ladder diagrams



Iteration of Gorkov equations for anomalous propagator generates



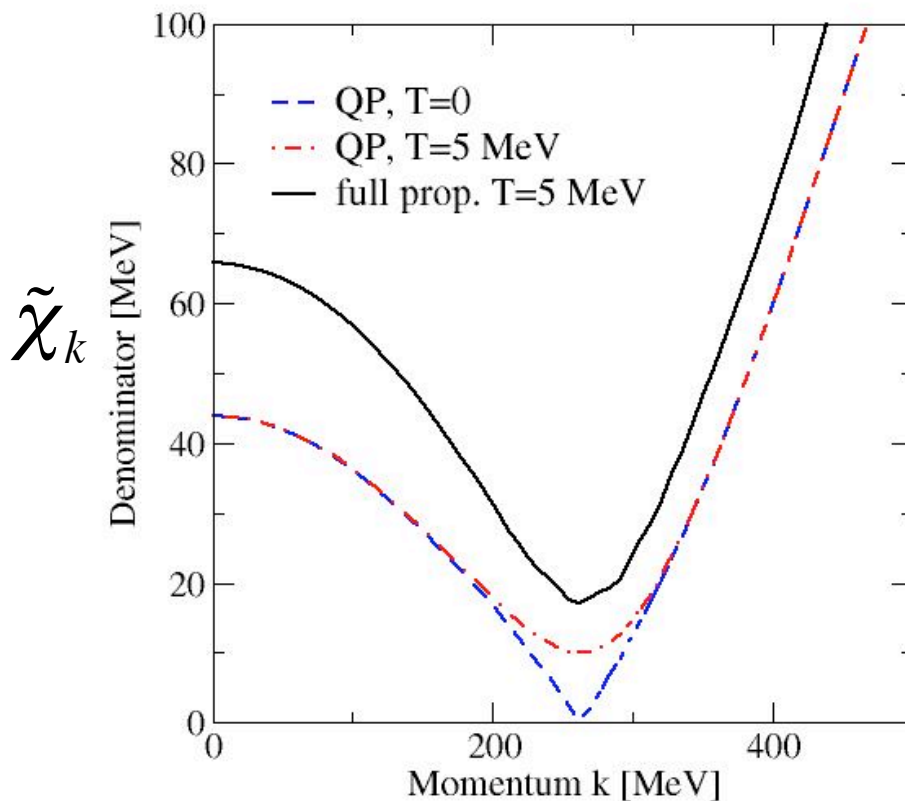
... and all other ladder diagrams at total momentum and energy zero (w.r.t.  $2\mu$ ) plus anomalous self-energy terms in normal part of propagator

So truly consistent with inclusion of ladder diagrams at other total momenta and energies

# Features of generalized gap equation

$$\Delta(k) = \int k'^2 dk' \langle k|V|k' \rangle \int d\omega \int d\omega' \frac{1 - f(\omega) - f(\omega')}{-\omega - \omega'} S(k', \omega) S_{\cancel{pair}}(k', \omega') \Delta(k')$$

$$-\frac{1}{2\tilde{\chi}_{k'}}$$



Dashed:

Spectral strength only at 1 energy

Dashed-dot:

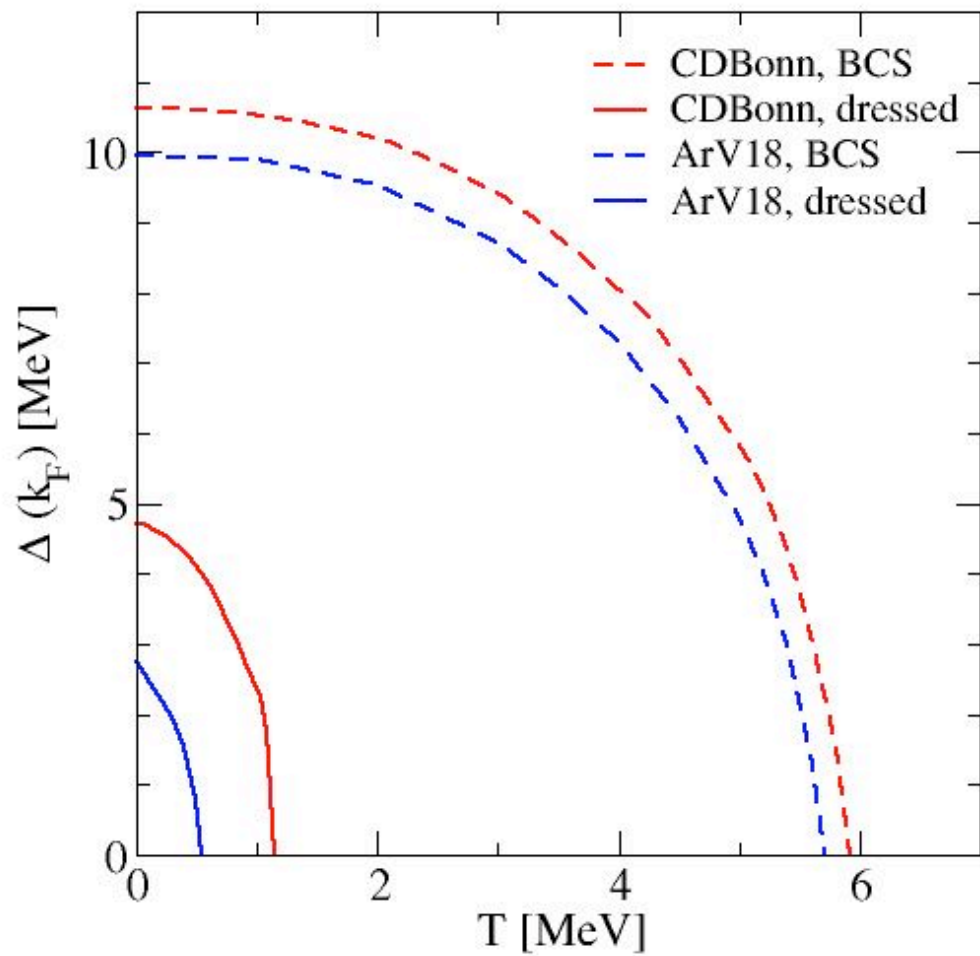
Effect of temperature (5 MeV)

Solid:

Includes complete strength distribution due to SRC

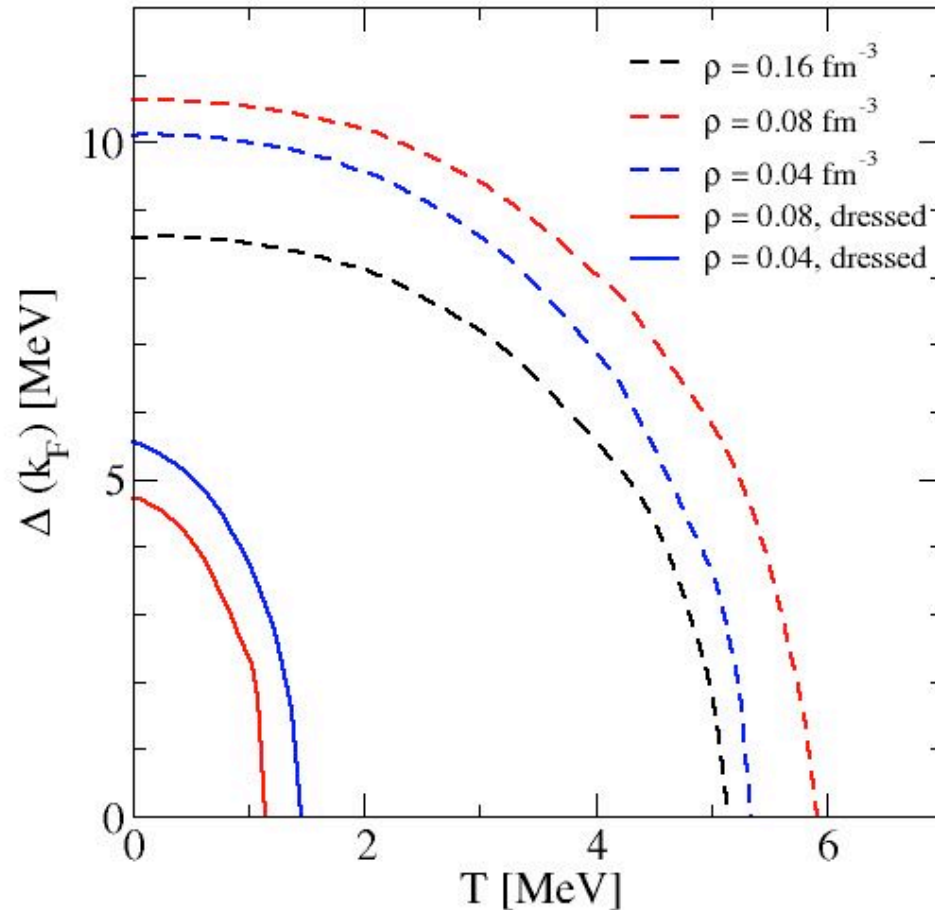
Related studies by

Baldo, Lombardo, Schuck et al.  
use BHF self-energy



*CDBonn yields stronger pairing than ArV18*

# Proton-neutron pairing in symmetric nuclear matter



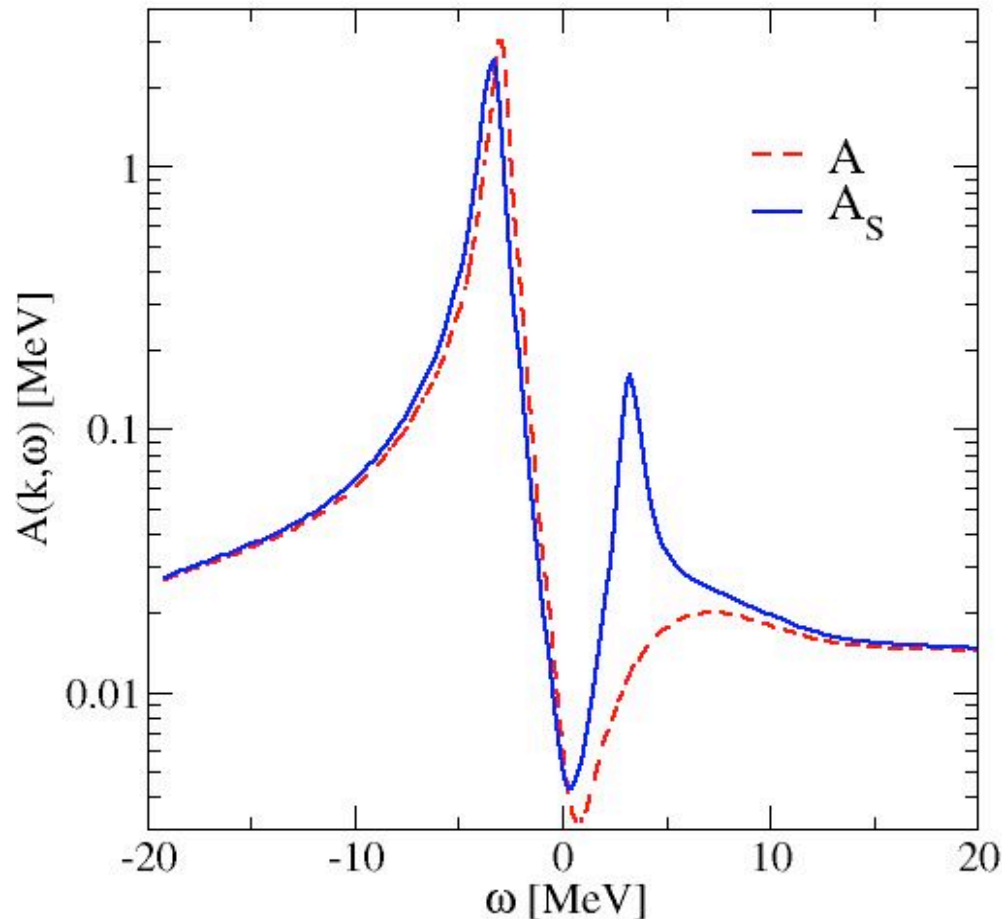
Using CDBonn

Dashed lines:  
quasiparticle poles

Solid lines:  
dressed nucleons

No pairing at saturation  
density!

# Pairing and spectral functions



Spectral functions

$S(k, \omega)$  dashed =  $A(k, \omega)$

$S_{\text{pair}}(k, \omega)$  solid =  $A_S(k, \omega)$

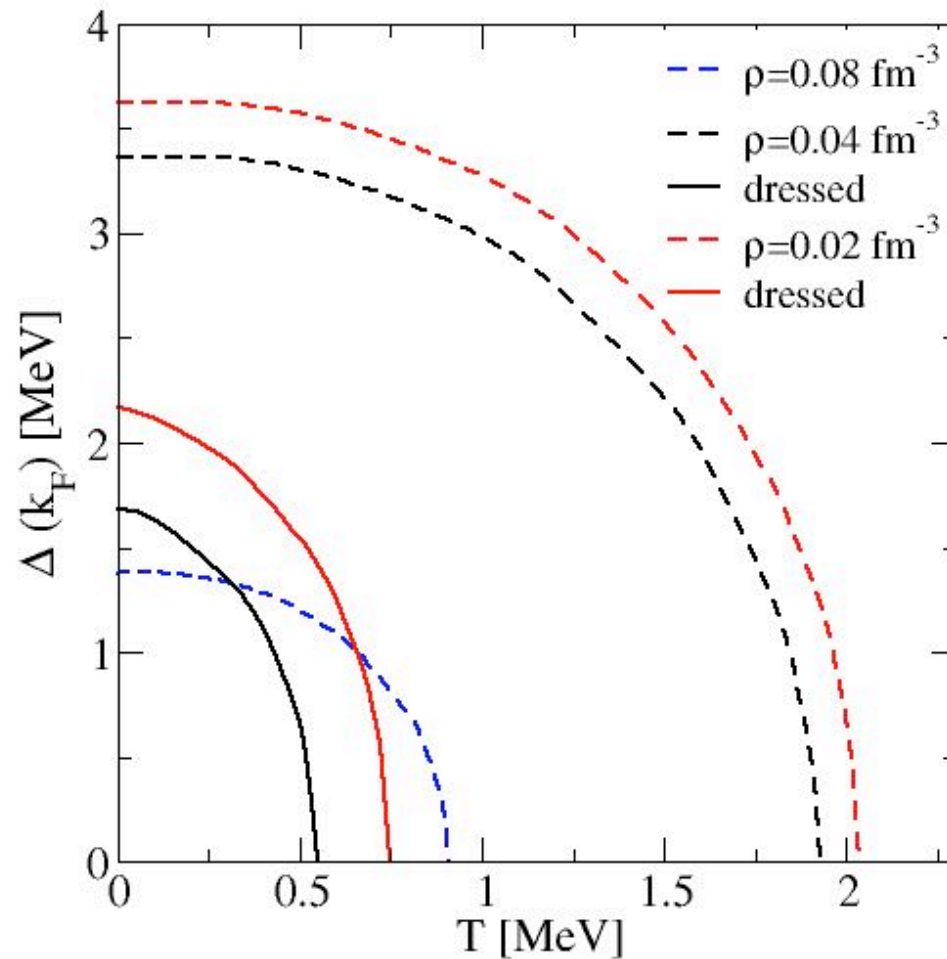
$\rho = 0.08 \text{ fm}^{-3}$

$T = 0.5 \text{ MeV}$

$k = 193 \text{ MeV}/c$   $0.9 k_F$

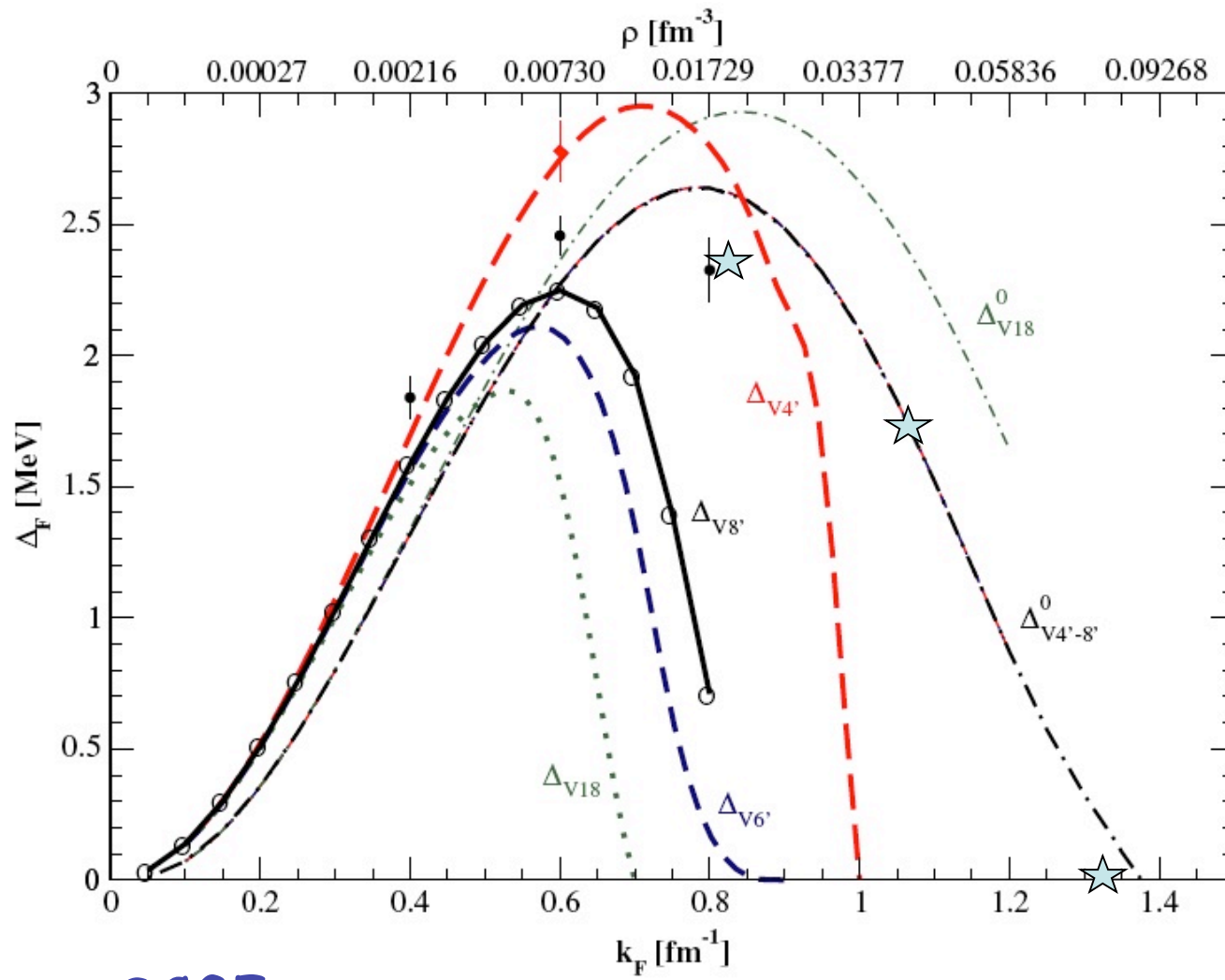
Expected effect

# Pairing in neutron matter



*Dressing effects weaker,  
but non-negligible  
CDBonn*

# Comparison for neutron matter with CBF & Monte Carlo PRL95,192501(2005)



★ ⇒ SCGF