

DF



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# FACETS OF ( $d, ^2\text{He}$ ) CHARGE-EXCHANGE REACTIONS: From nucleon-nucleon physics to the mysteries of supernova explosions and the double-beta decay

astrophysics !

double-beta decay

NN-studies

halo nuclei

stretched states

# Albert Singlestane & John Doe ----Questions and Answers

THERE ARE SOME THINGS I'VE ALWAYS WONDERED ABOUT ...

LIKE WHAT ..?

LIKE, HOW CAN YOU TELL WHEN IT'S EXACTLY MIDNIGHT ?

EASY .. THE DARKNESS IS DIRECTLY OVERHEAD

GEE, AND WHY DO DAYS GET LONGER IN THE SUMMER ?

BECAUSE HEAT MAKES THINGS EXPAND !!!

AND WHY IS AIR SPEED DIFFERENT FROM GROUND SPEED??

SIMPLE ! BECAUSE THE EARTH IS ROUND AND THE AIR IS FLAT

AND WHAT HOLDS THINGS TOGETHER ?

VELCRO !! NEUTRONS AND PROTONS ARE HELD TOGETHER BY VELCRO !!!!

THANK YOU

DON'T MENTION IT. I HAVE A NATURAL TALENT FOR SCIENCE

# Nucleosynthesis

**Question:**

- When did it start ??
  - what elements were produced and can we understand the isotopic composition ??
  - do parameters of the Early Universe have an influence ??
- 

1945: G. Gamow's hypothesis  
*"all of todays elements were made during the early BIG BANG phase of the Universe"*

**wrong!**

# Nucleosynthesis

**wrong** for 3 simple reasons!!!

- Binding energy of deuteron (2.22 MeV) is too small !!
- Binding energy of  ${}^4\text{He}$  is too large (28.3MeV) !!
- There are no stable isotopes with  $A=5$  and  $A=8$  !!

*deuterons are being dissociated until the Universe  
has cooled down to 80 keV !!!*  $N_\gamma \sim 10^{10} N_N$

*for further fusion the train has  
long left the station!!*

**Universe composition:**  
**~76% H and ~23%  ${}^4\text{He}$**

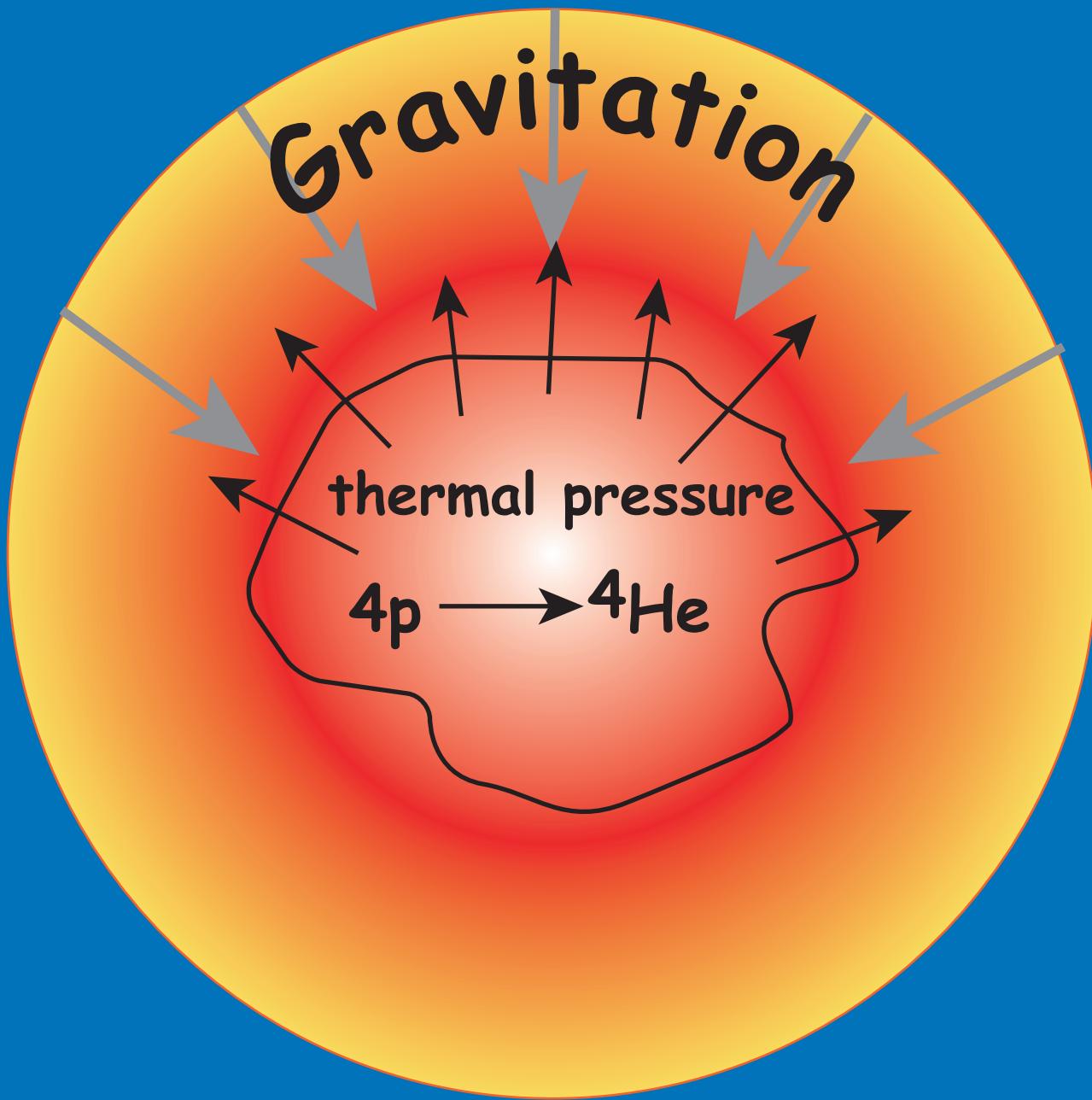
Elements are made in stars  
but  
stars have to be big



and  
they have to explode

Supernovae  
Cassiopeia A  
Chandra

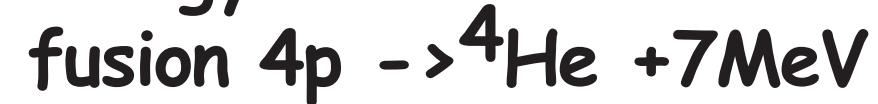
# Nuclear processes and energy household of supernovae



initial condition:

$$M > 10 M_{\odot}$$

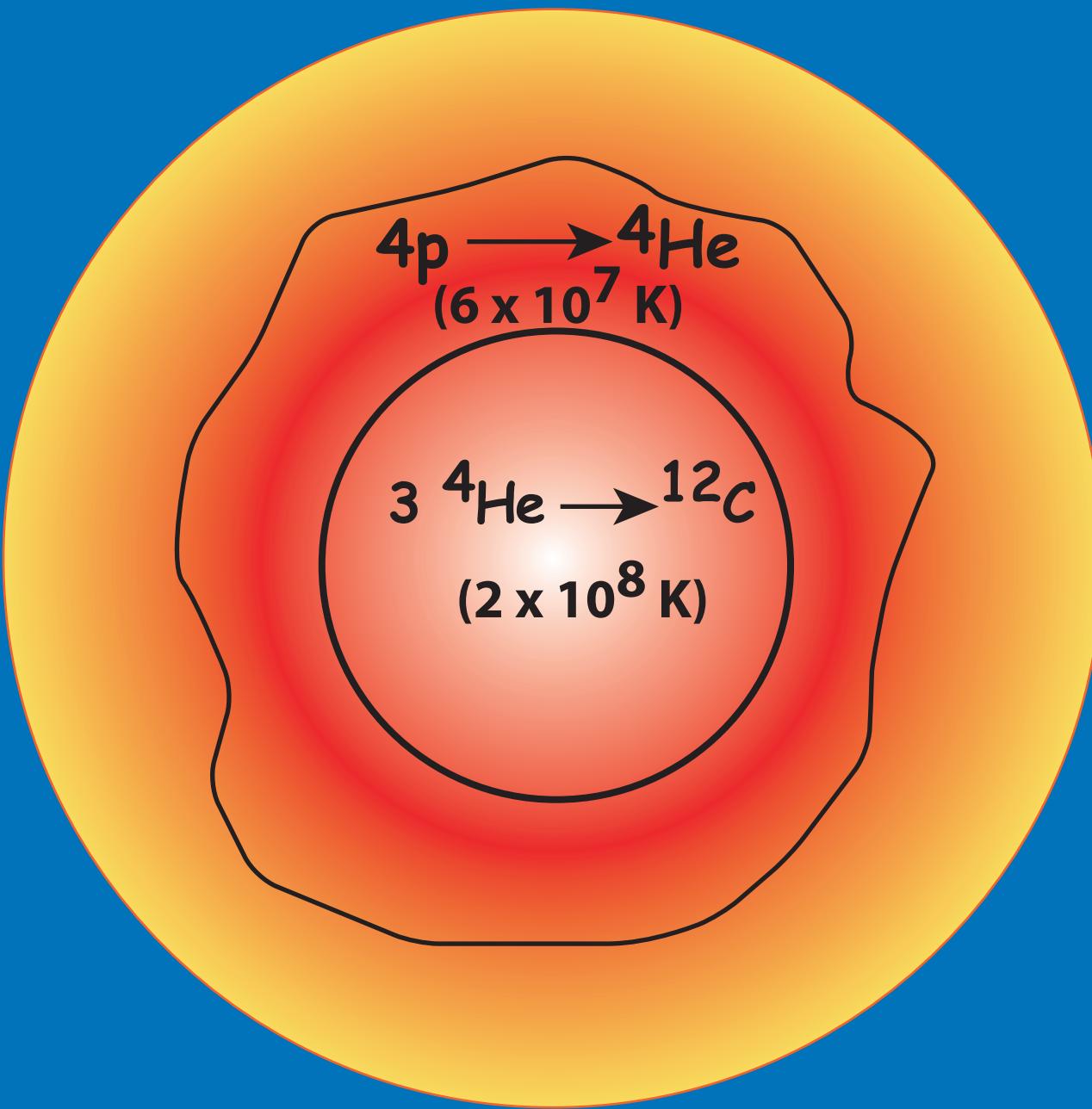
energy:



at:  $T \sim 10^7 - 10^8 \text{ K}$

lifetime:  $10^6 - 10^7 \text{ y}$

after  $10^6$  -  $10^7$  y



end of H-burning

contraction of star

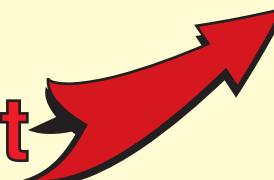
temperature increase

Red Giant (Super-Giant)

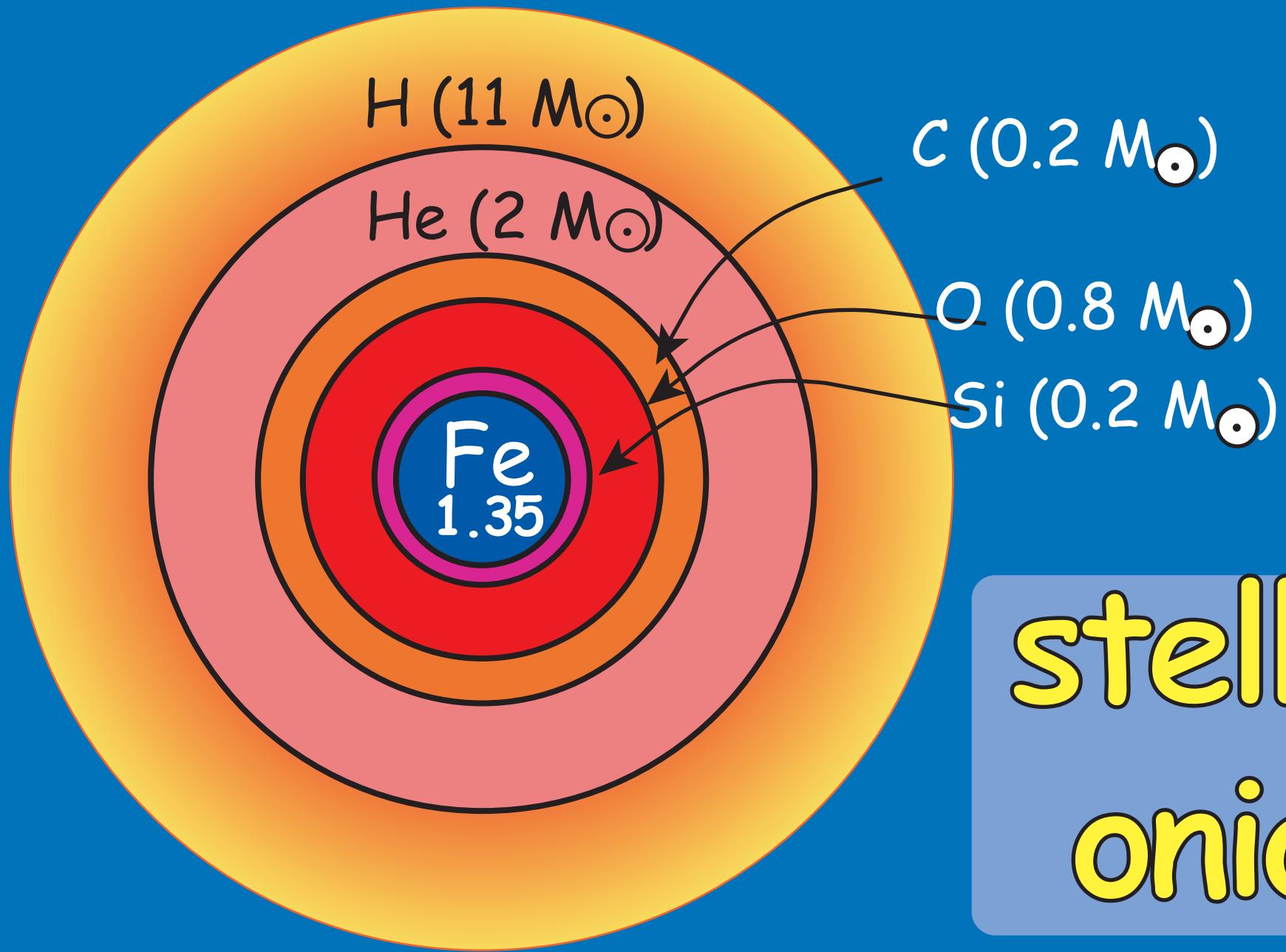
lifetime:  $5 \times 10^5$  y

## THEN

- 600y**  $^{12}\text{C}$  burning ( $^{12}\text{C} + ^{12}\text{C} \rightarrow ^{20}\text{Ne} + \alpha + 4 \text{ MeV}$ )  
 $T = 10^9 \text{ K}$
- 1y**  $^{20}\text{Ne}$  burning (many paths)  $T = 2 \times 10^9 \text{ K}$   
(ashes mainly  $^{16}\text{O}$ )
- 0.5 y**  $^{16}\text{O}$  burning  $T = 2-3 \times 10^9 \text{ K}$   
(ashes mainly  $^{28}\text{Si}$  (Fe))
- ~1 day**  $^{28}\text{Si}$  burning  $T = 4 \times 10^9 \text{ K}$   
(ashes mainly Fe)  $\rho = 2 \times 10^7 \text{ g/cm}^3$
- then** core collapse (~ sec)  $T = 10^{11} \text{ K}$   
core bounce & explosion (~ msec)  $\rho = 10^{14} \text{ g/cm}^3$   
nucleosynthesis (0.1 - 10 sec)

entering physics at 

end of stellar evolution  $M_{\text{star}} \sim 15 M_{\odot}$

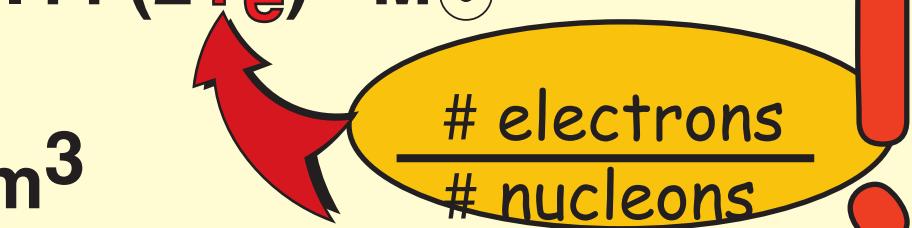


stellar  
onion

## SN-explosion scenario

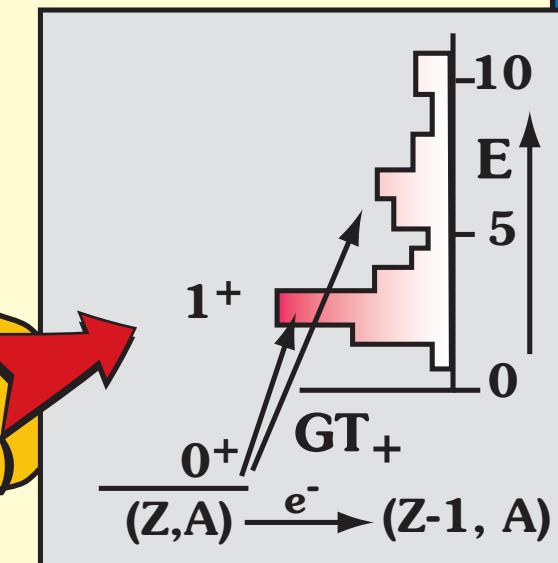
- interior of star gets enriched with Fe
- gravitational pressure increases balanced by degenerate electron gas up to Chandrasekhar limit:  $M_{\text{ch}} = 1.44 (2Y_e)^2 M_{\odot}$

- start of collapse at  $T = 10^9 \text{ K}$  and  $\rho = 3 \times 10^9 \text{ g/cm}^3$  accelerated by neutronization (de-leptonization)



- loss of pressure
- accelerated collapse
- reduction of  $Y_e$  and loss of energy!!

rate determined by GT-strength  
( $\Delta S = 1, \Delta T = 1, \Delta L = 0$ )



$Y_e$  at freeze-out determines the explosive energy!!

## SN-explosion scenario (cont.)

### neutrino trapping and $Y_e$ freeze-out

$R_{\text{core}} \sim 30\text{km}$

$\lambda_{\text{mfp}}(\nu) \sim 0.4\text{km}$

core decouples ( $Y_e$  freezes out --- but what is its value?)



conversion of gravitational energy into neutrinos

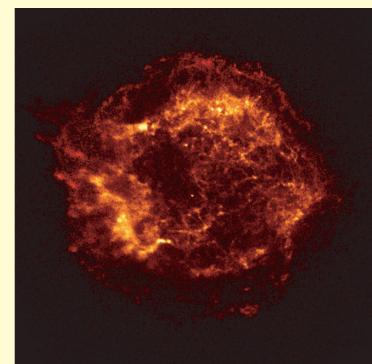
imploding core reaches nuclear matter density  
( $\rho \sim 10^{15}\text{g/cm}^3$ ) and **rebounds**

rebounding shock wave meets infalling material

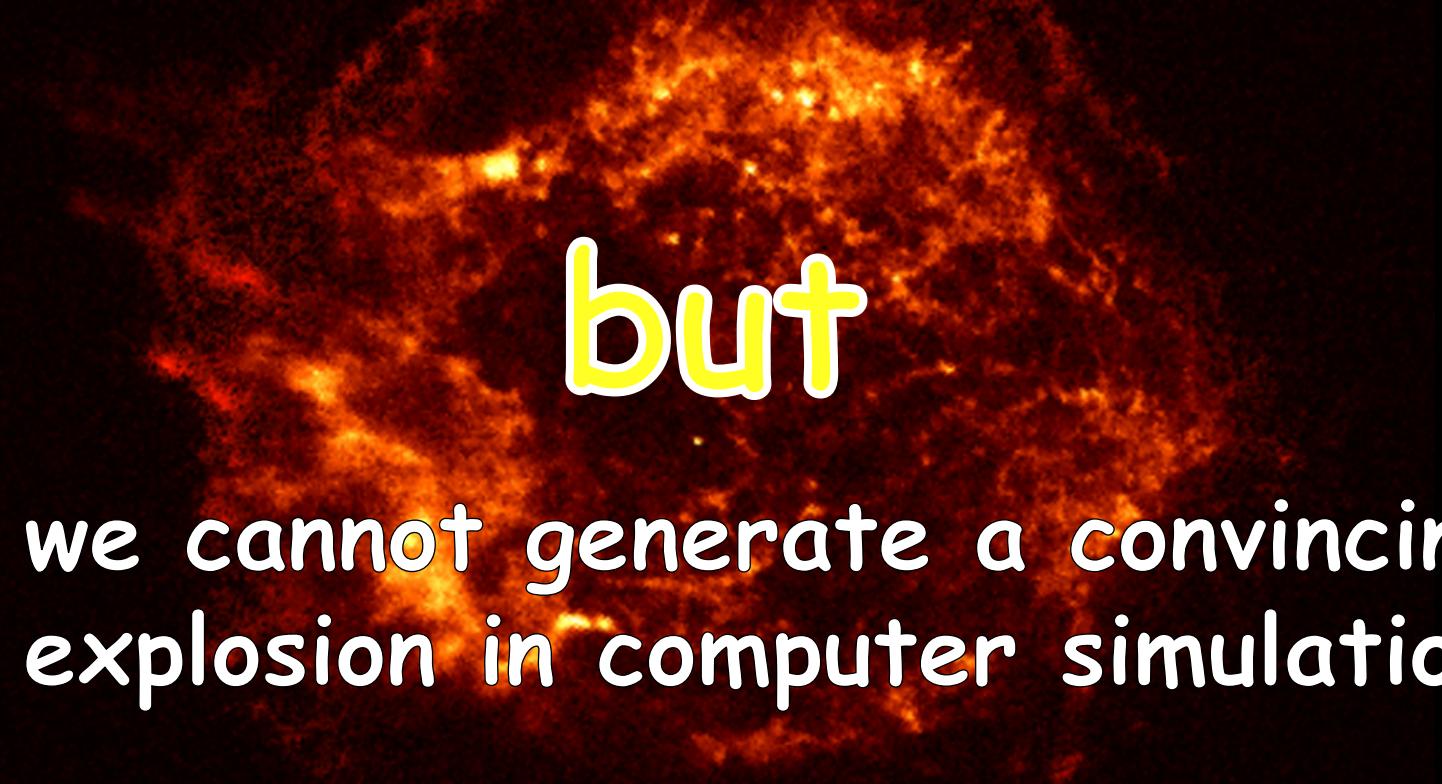
- ☒ rapid nucleosynthesis
- ☒ explosion into interstellar space

optical/kinetic energy  $10^{51}\text{ erg}$

neutrino energy  $10^{53}\text{ erg}$  ( $10^{57} - 10^{58}$  neutrinos!!)



Elements are made in  
**EXPLODING STARS**  
**(SUPERNOVAE)**



but

we cannot generate a convincing  
explosion in computer simulations

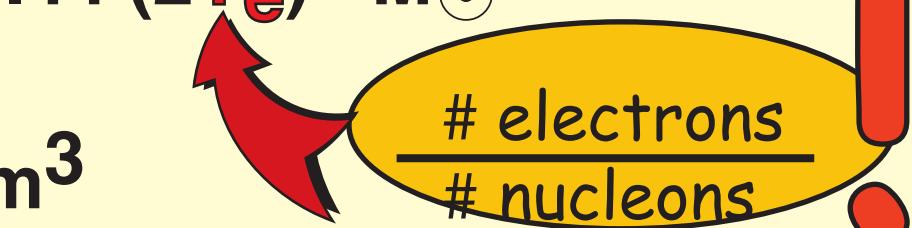
are there missing physics pieces



## SN-explosion scenario

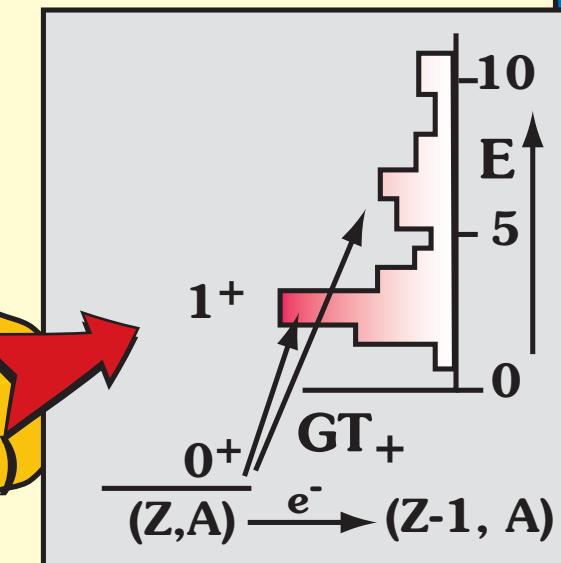
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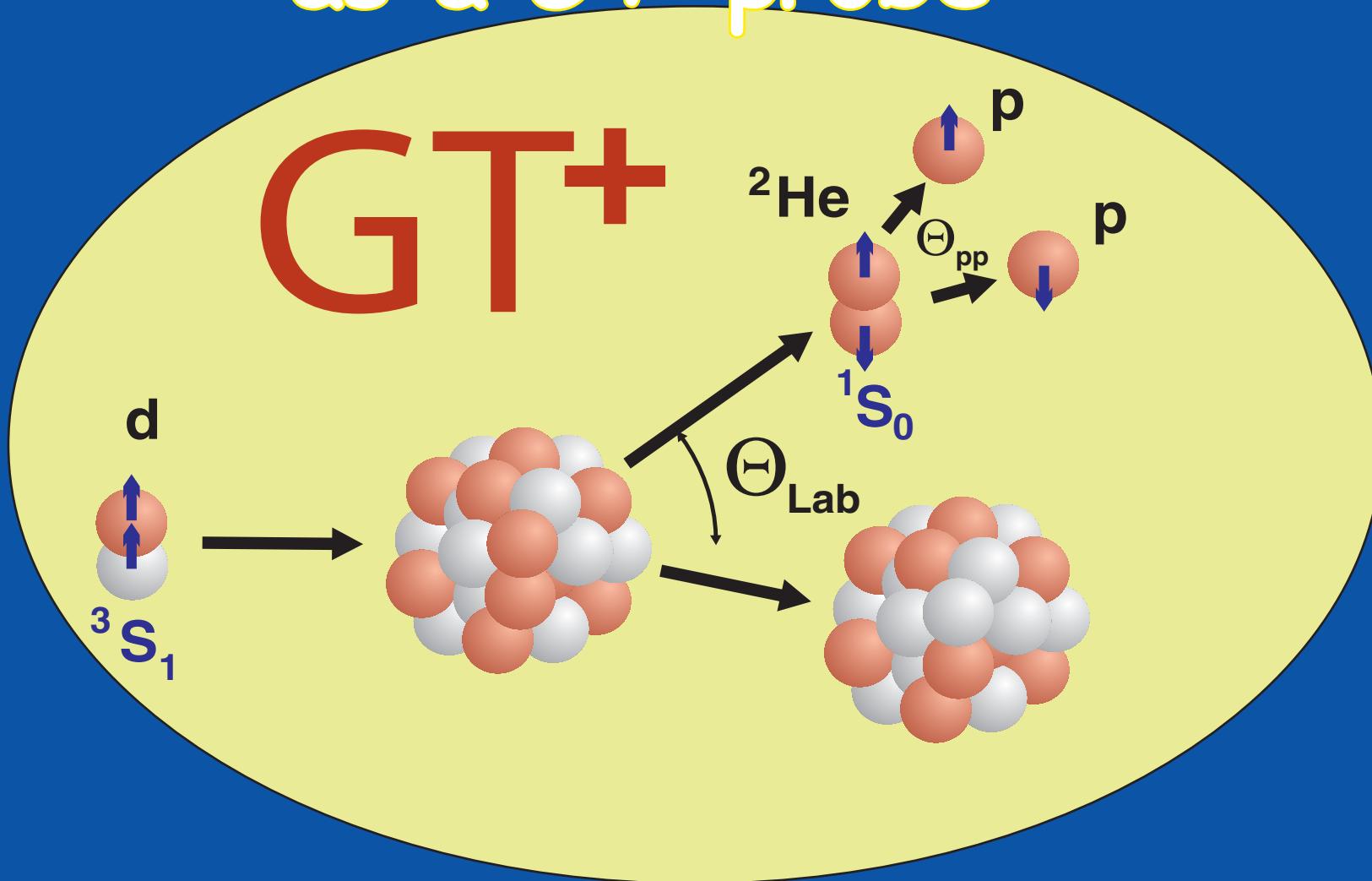
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rate determined by GT-strength  
( $\Delta S = 1, \Delta T = 1, \Delta L = 0$ )



$Y_e$  at freeze-out determines the explosive energy!!

# The $(d, 2\text{He})$ charge exchange reaction as a GT-probe

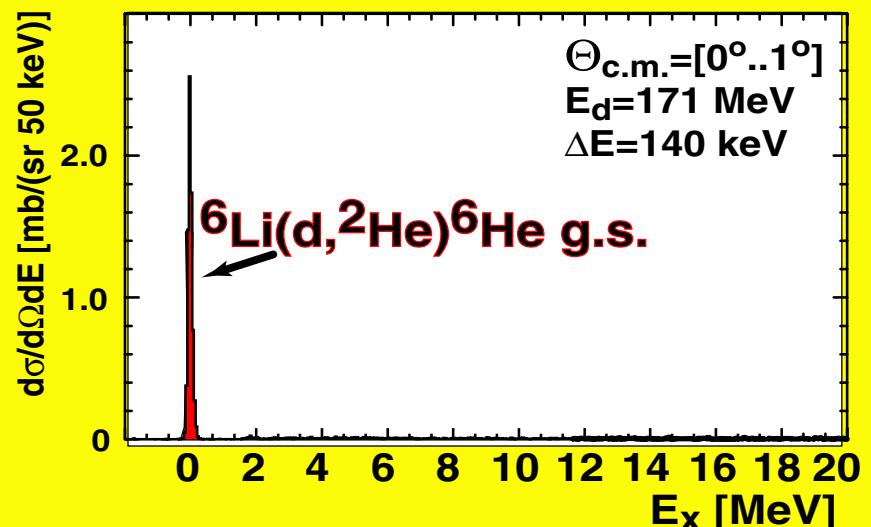
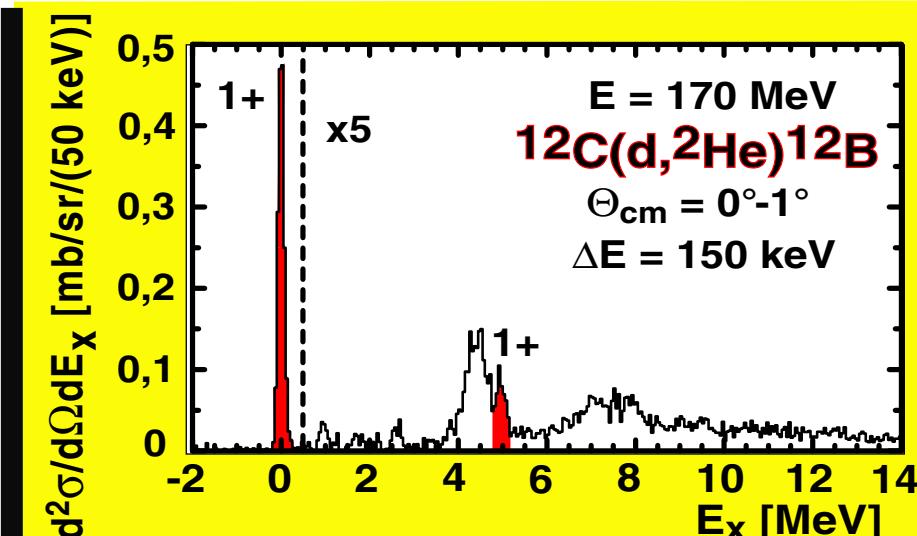
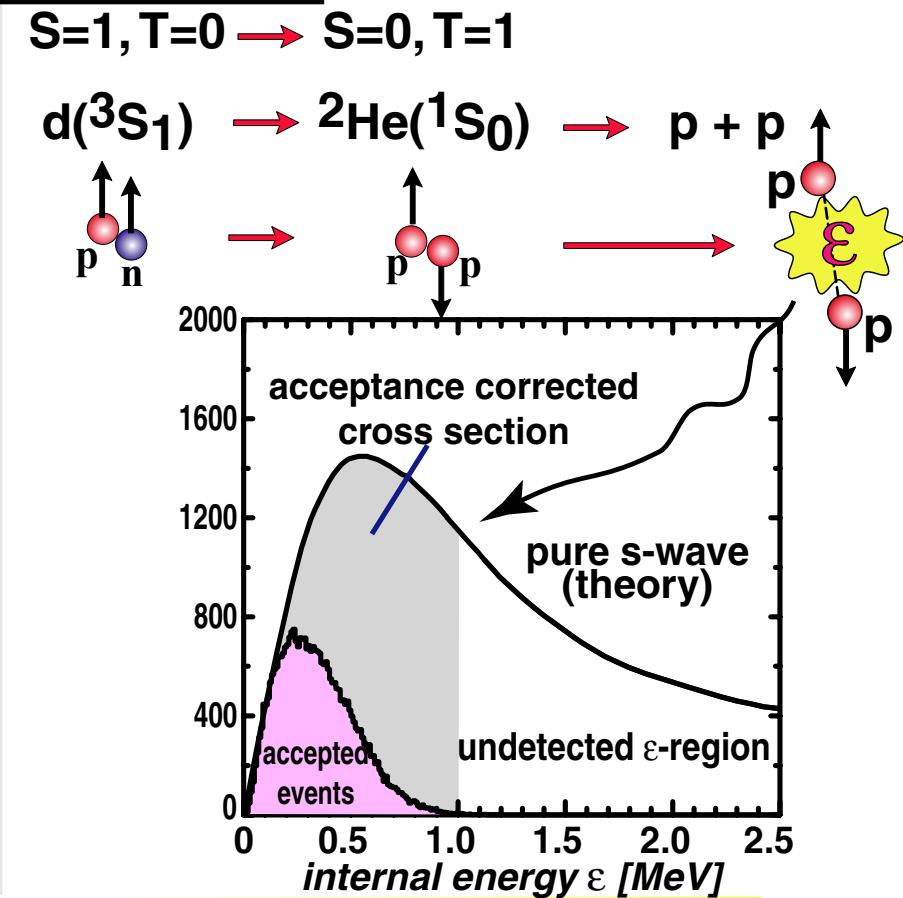


# The ( $d, {}^2\text{He}$ ) reaction

- 1)- reaction mechanism forces a spin-flip and an isospin-flip !  
 $\Delta S=1, \Delta T=1$  perfect GT filter
- 2)- coincident detection of two protons from  ${}^2\text{He}$  decay  
 → background-free spectra but need large accptnc spectrometer
- 3)- contributions from higher p-p partial waves? Dont' worry!!

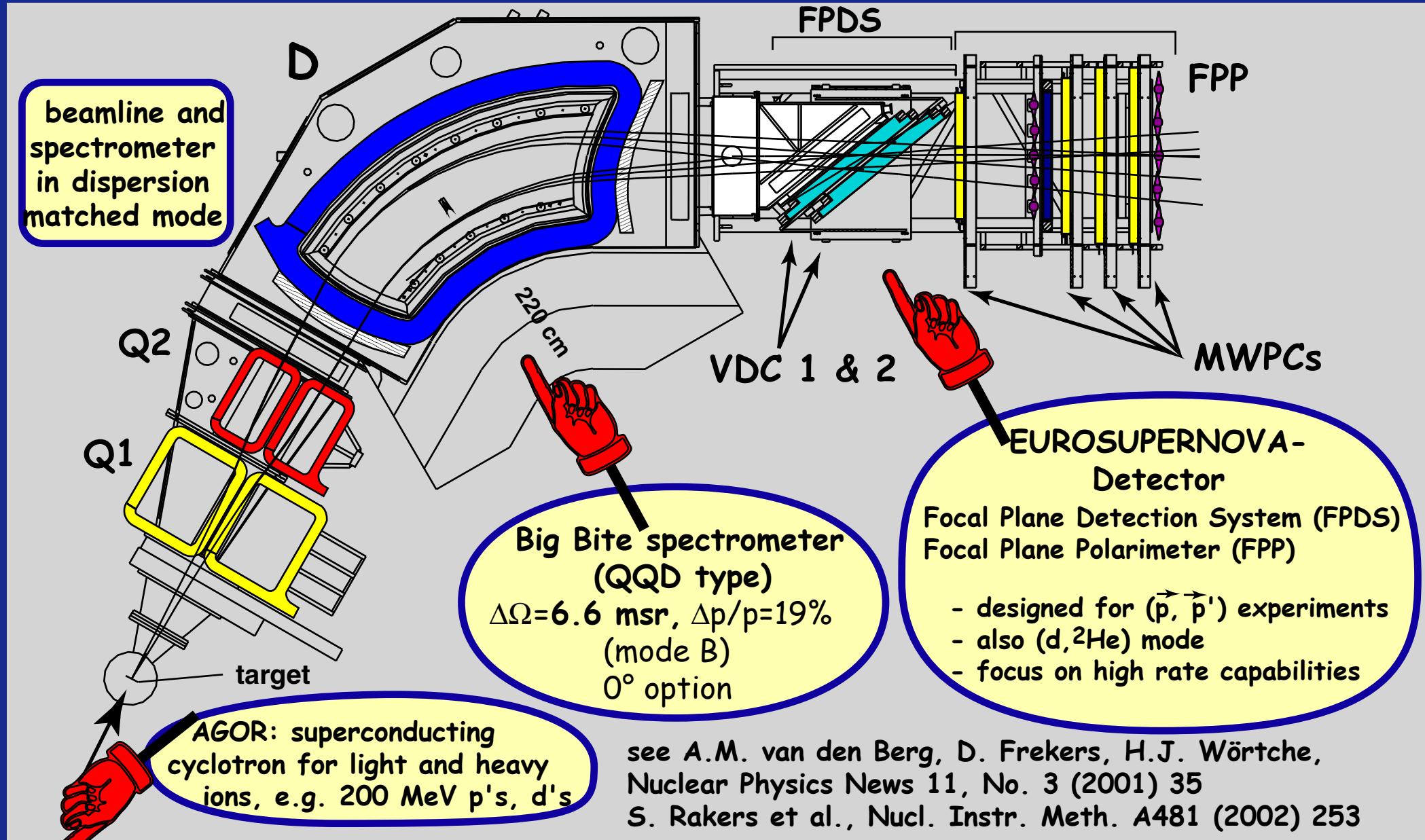
## Alternatives:

- (n,p) resolution?? Fermi transition  
 (t, ${}^3\text{He}$ ) triton beam?? Fermi transition  
 (HI,HI) resolution?? reaction mechanism??



# The experimental setup

at AGOR facility, KVI Groningen



# GT<sup>+</sup> transitions from nuclei of pf-shell: relevance for astrophysics

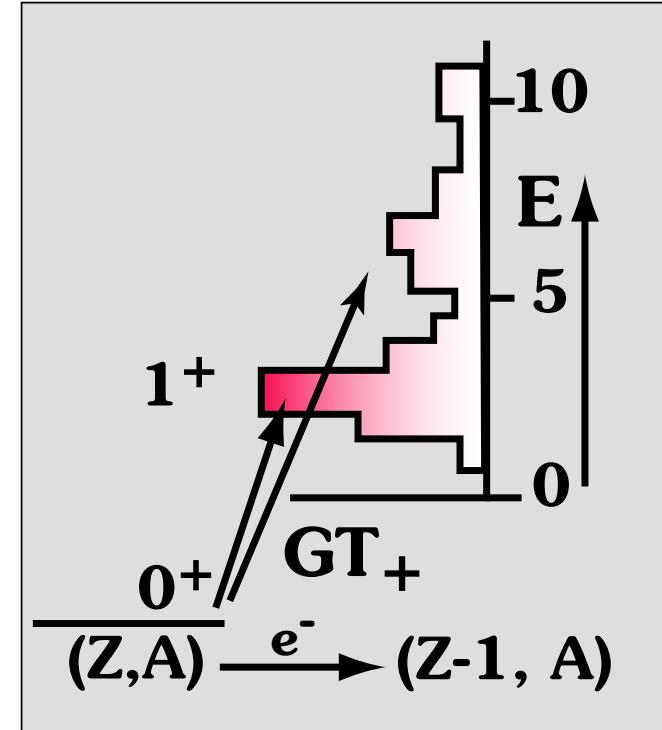
H.A. Bethe et al. (1979):

Electron-Capture (EC) from nuclei in pf-shell  
plays pivotal role in the deleptonization of a  
massive star prior to core-collapse.

Fuller, Fowler & Newman (FFN) (1982-1985),  
M. Aufderheide (1994):

systematic estimates of EC-rates  
in stellar environments  
-> calculations of GT-centroids only

FFN



Langanke, Martinez-Pinedo, Caurier (1999):

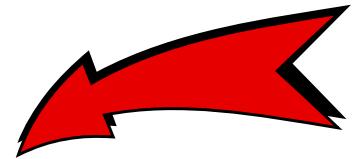
B(GT<sup>+</sup>)-distributions from modern  
shell-model calculations

some marked deviations from FFN-rates

->  $Y_e$  increases to about 0,445  
(FFN: ~ 0,430)

!

most dramatic cases are  
odd-odd nuclei  $^{60}\text{Co}$ ,  $^{58}\text{Mn}$



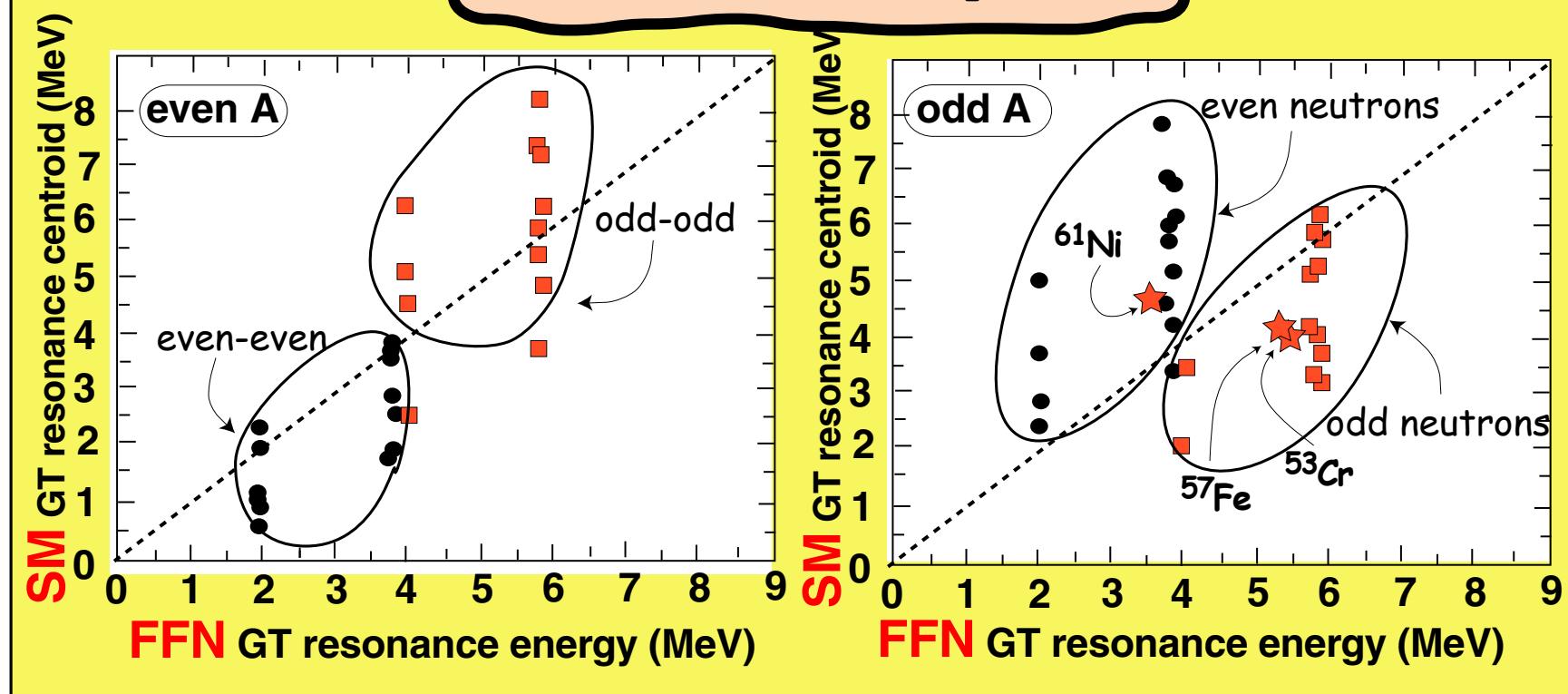
# Stellar EC rates at a given temperature

important parameters

- location of GT resonance (most important)
- level of quenching
- fragmentation over excitation energy

## SM and FFN comparison

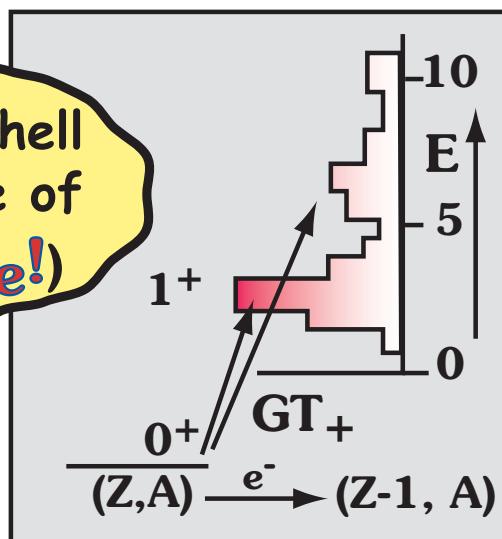
from:  
Langanke, Martinez-Pinedo  
Nucl.Phys. A 673, 481 (2000)



- no exp. data on odd-N nuclei (usually rare!!)
- no exp. data on odd-odd nuclei ( $^{50}\text{V}$  is the only stable one)

# Astrophysics applications, SN explosions, EC-rates and $Y_e$

GT-strength in (pf)-shell nuclei determines fate of SN-explosion ( $Y_e!$ )



EC-rates up  
deleptonization up  
 $\nu$ -cooling before collaps up  
 $Y_e$  down  
total energy down

$Y_e > 0.45$  explosion  
 $Y_e < 0.43$  no explosion

$$B(GT^+) = \sum_{i,f} \frac{n_i^p n_f^h}{(2j_i+1)(2j_f+1)} |\langle f | \vec{\sigma} \tau_+ | i \rangle|^2$$

$n_i^p$  → # of protons in orbital  $i$  of g.s. ( $j_i$ )  
 $n_f^h$  → # of neutron holes in orbital ( $j_f$ )

hadronic probes: (p,p'), (n,p), (p,n), (d,<sup>2</sup>He)

$$\left[ \frac{d\sigma}{d\Omega} \right] = \left[ \frac{\mu}{\pi \hbar} \right]^2 \frac{k_f}{k_i} N_D |V_{\sigma\tau}|^2 \left| \langle f | \sum_k \sigma_k \tau_k | i \rangle \right|^2$$

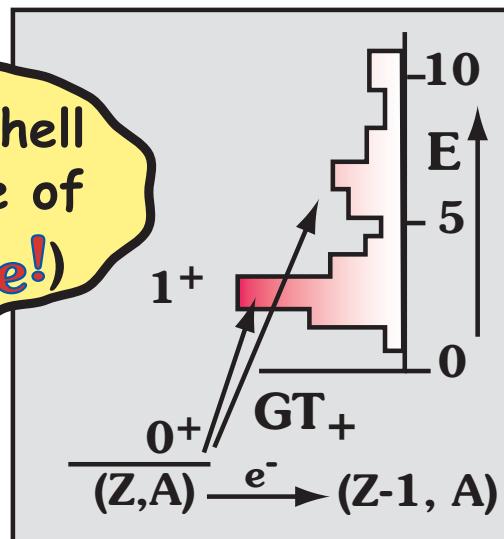
largest at 100 - 200 MeV/A

Q: How to connect the weak  $\vec{\sigma} \tau_+$  GT operator with hadronic reactions?

A: at intermediate energies exploit the dominance of  $V_{\sigma\tau}$  interaction.

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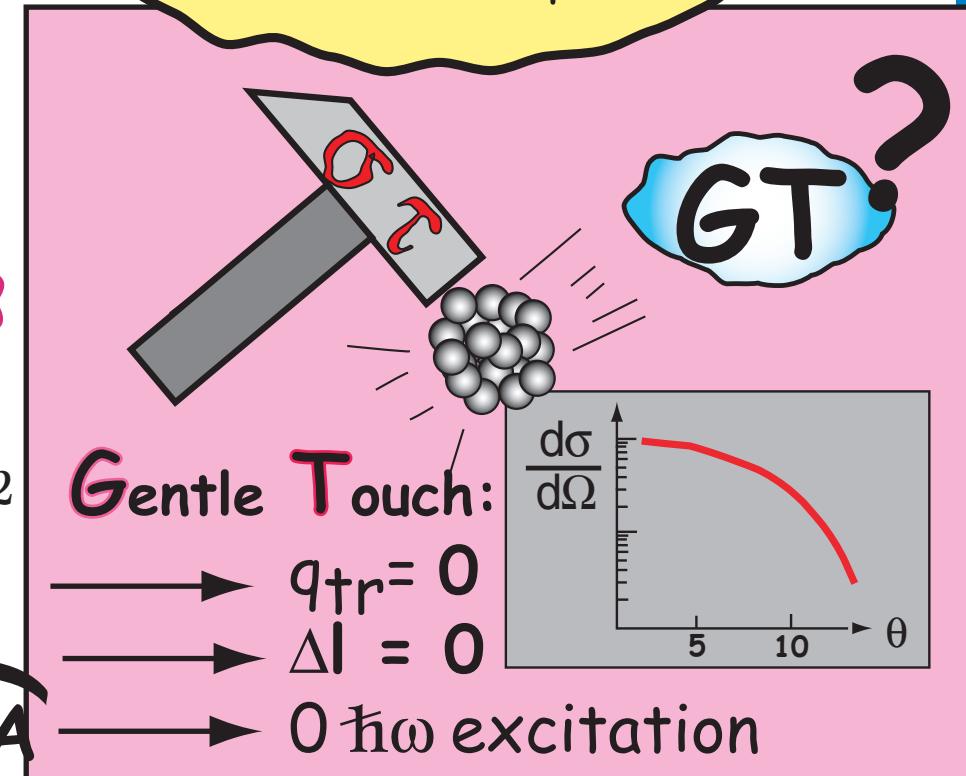
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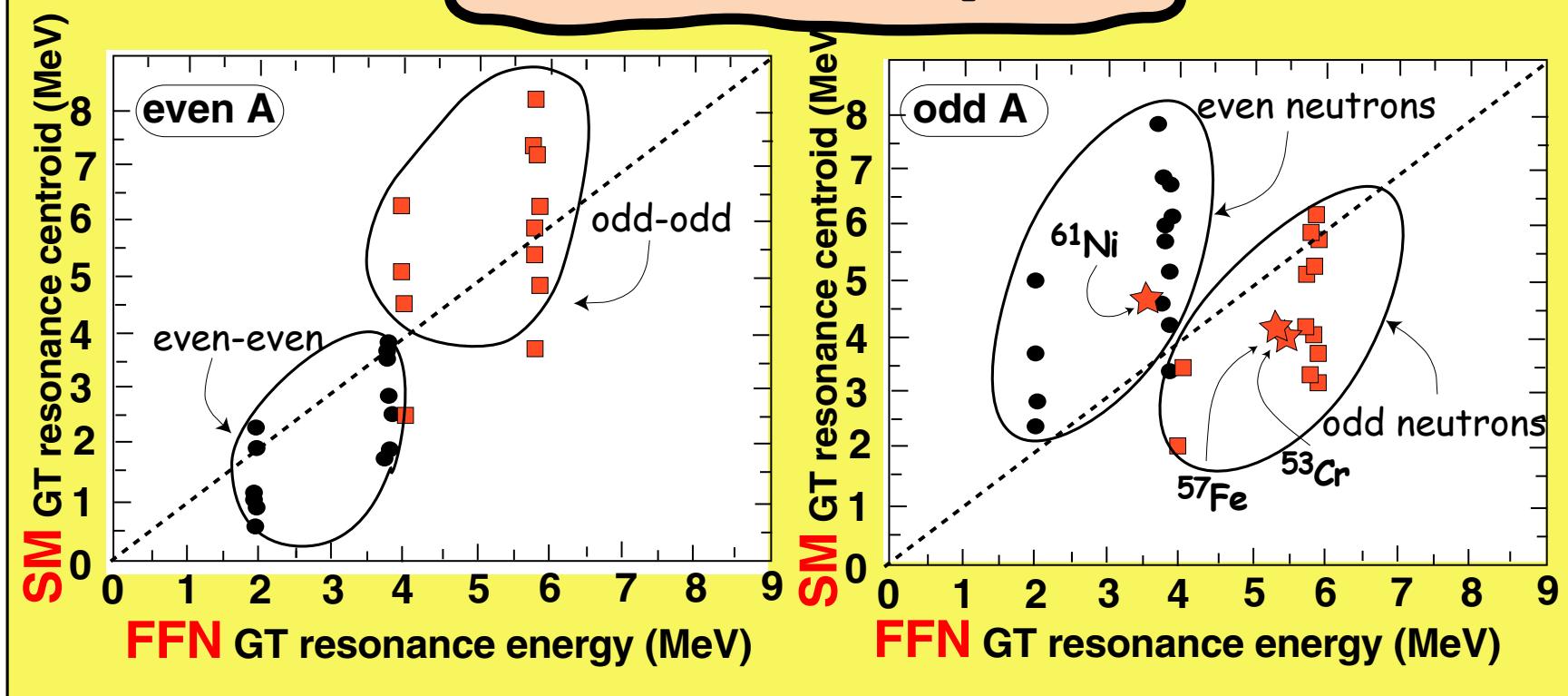
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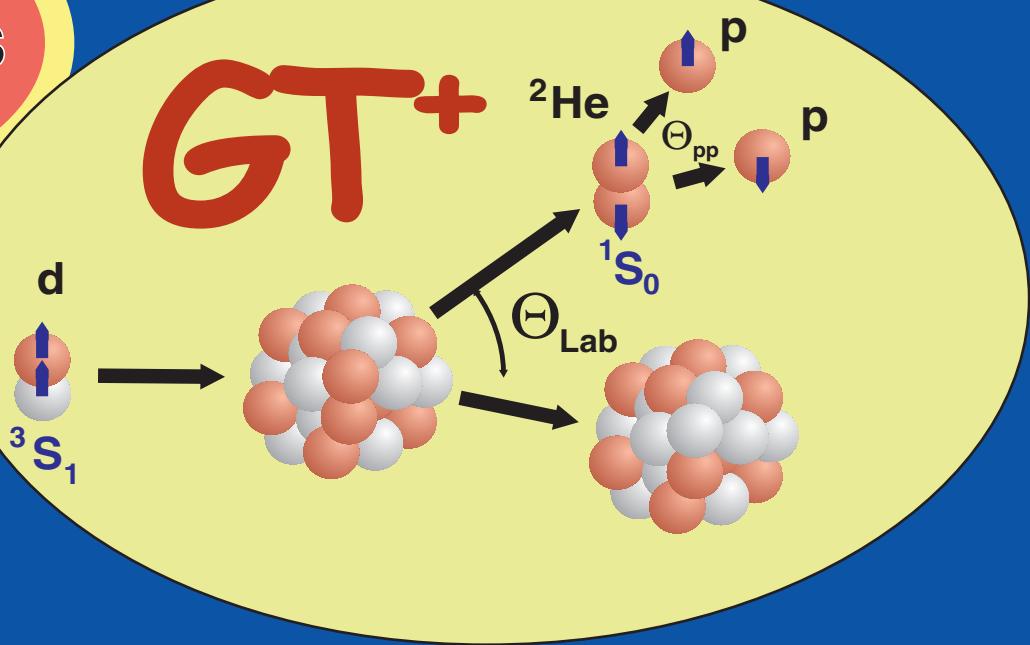


- no exp. data on odd-N nuclei (usually rare!!)
- no exp. data on odd-odd nuclei ( $^{50}\text{V}$  is the only stable one)

# odd-*A* odd-*p* nuclei

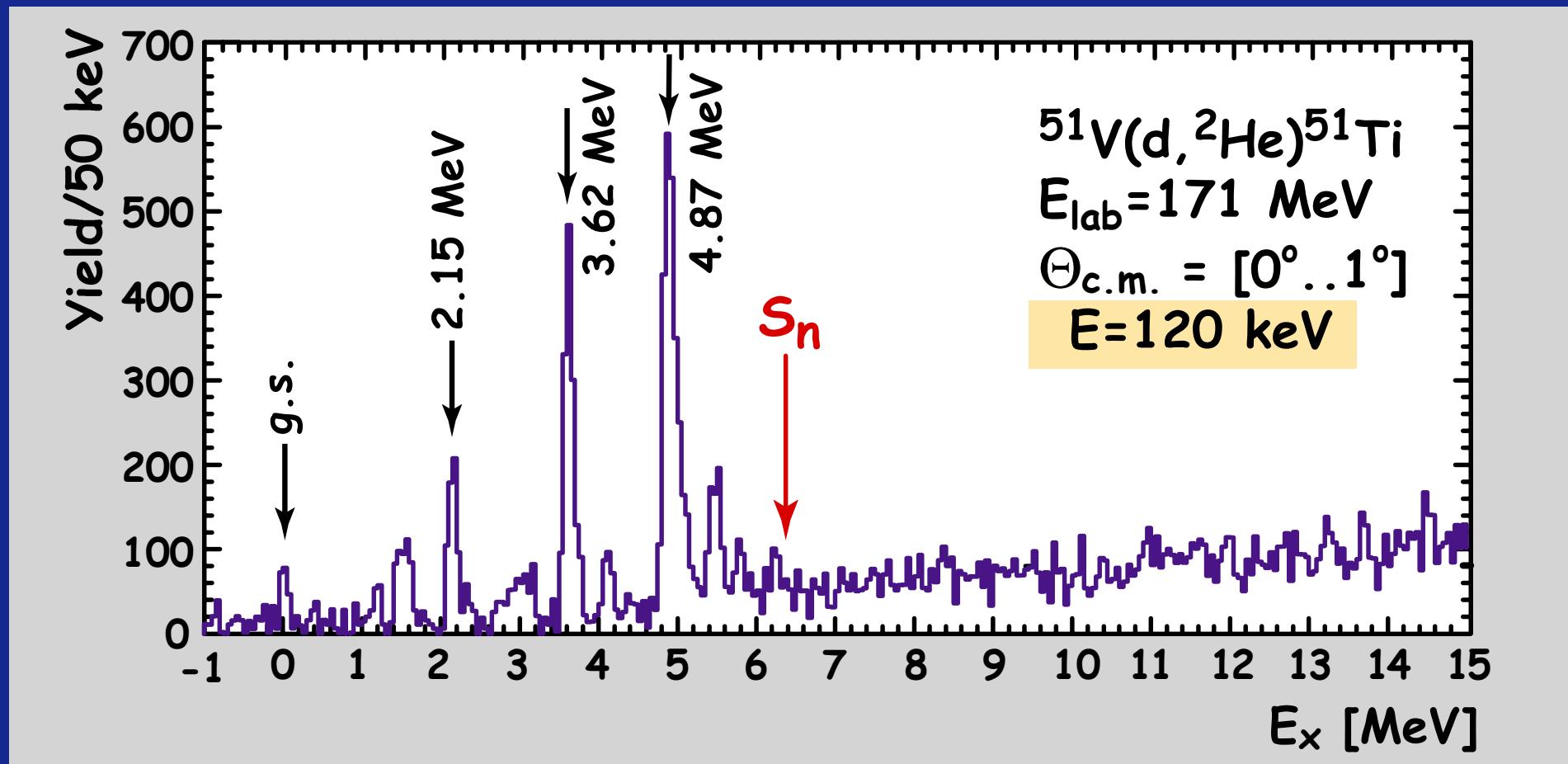
Astrophysics

**GT<sup>+</sup>**



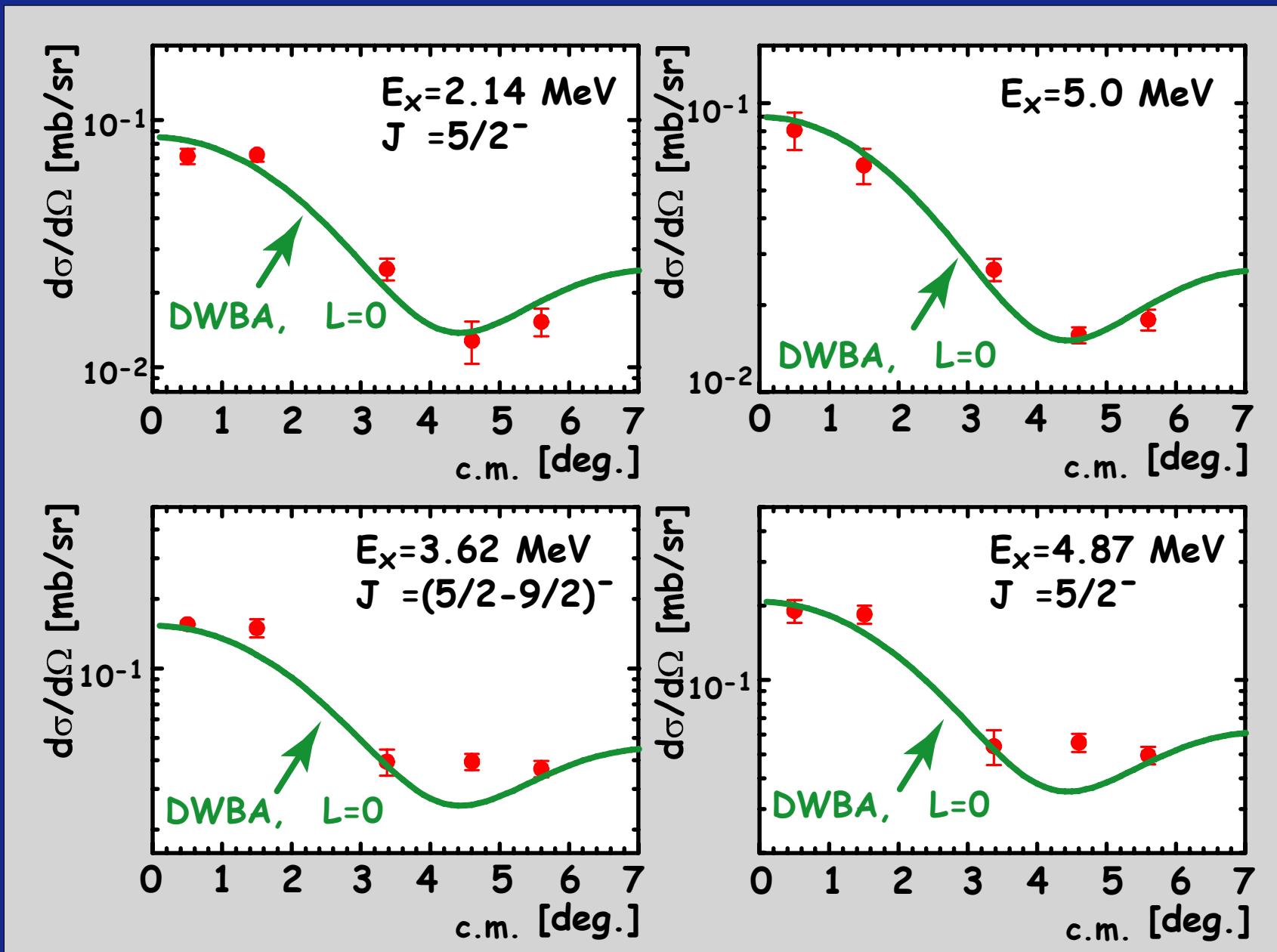
# B(GT<sup>+</sup>) from a proton-odd pf-shell nucleus: $^{51}\text{V}(\text{d}, ^2\text{He})^{51}\text{Ti}$

- $^{51}\text{V}$  g.s. ( $J = 7/2^-$ ,  $T=5/2$ )  $\rightarrow$   $^{51}\text{Ti}$  ( $J = 5/2^-, 7/2^-, 9/2^-$ ,  $T=7/2$ )
- independent single particle model:  $E_x(\text{GTR})=3.83$  MeV (FFN)

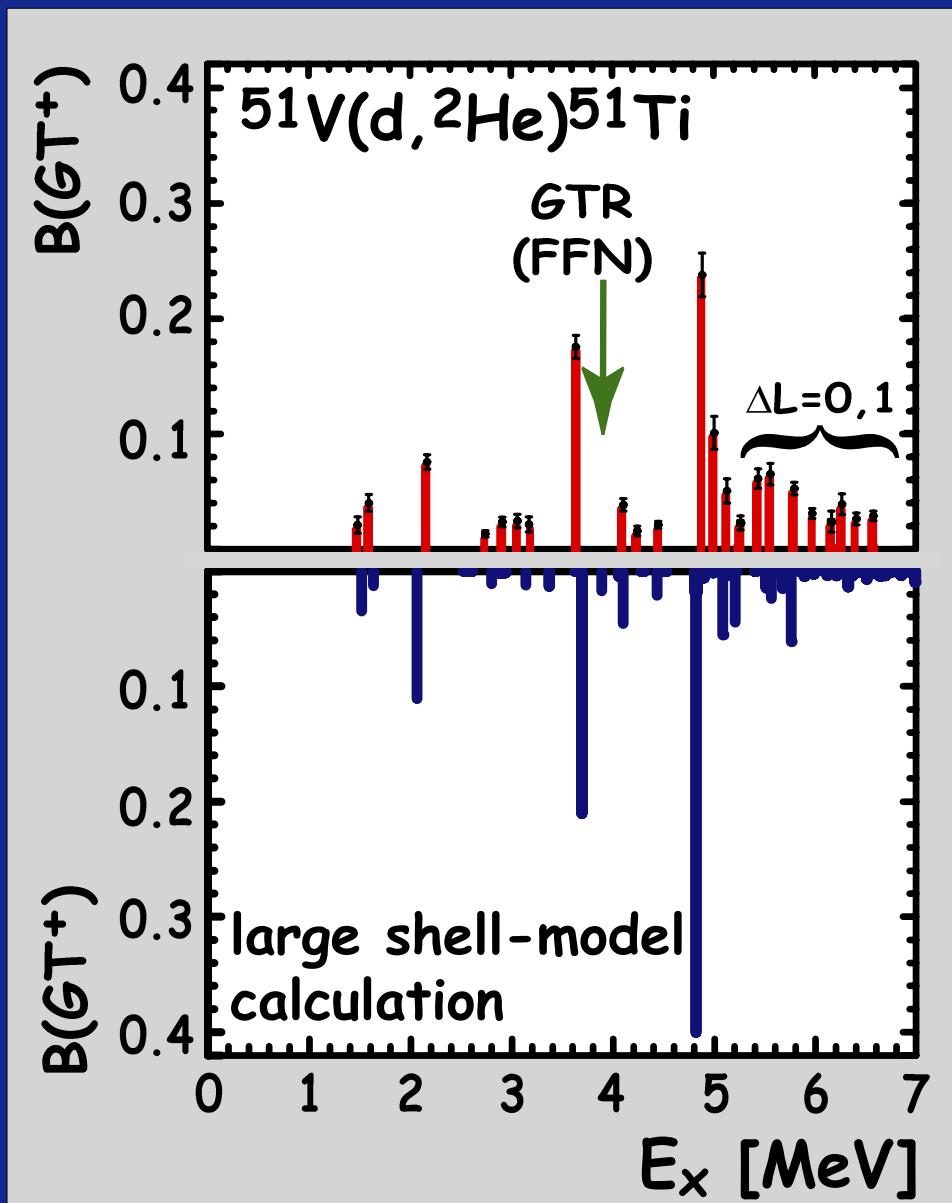


C. Bäumer et al., Phys. Rev. C 68 (2003) 031303(R)

# $^{51}\text{V}(\text{d},^2\text{He})$ : Angular distributions of $d\sigma/d\Omega$



# $^{51}\text{V}(\text{d},^2\text{He})$ : Comparison with shell-model calculation



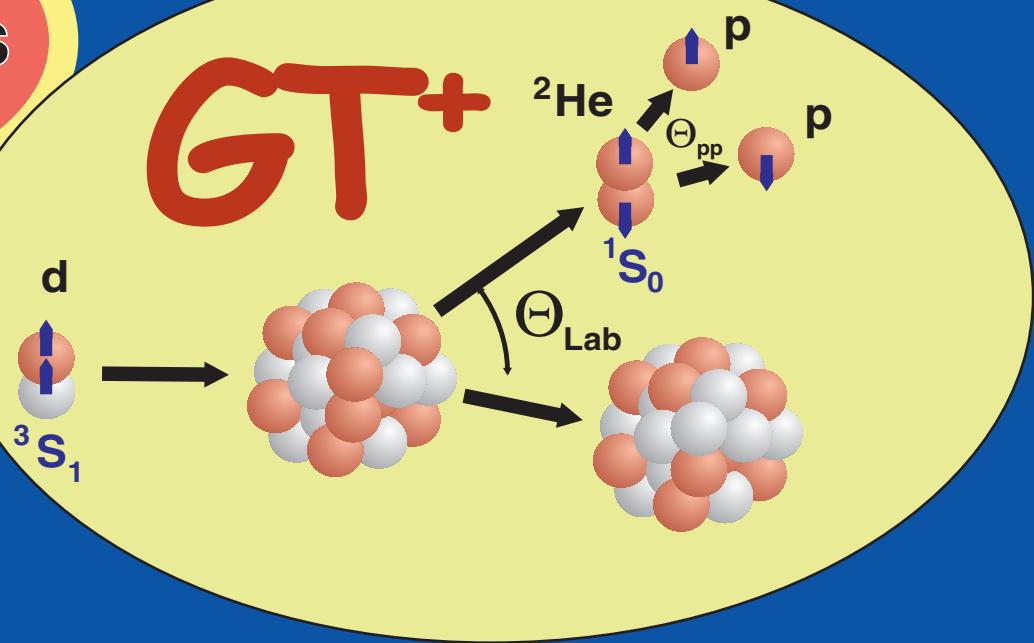
← experimental result

← full pf-shell model  
calculation  
(G. Martinez-Pinedo,  
K. Langanke)

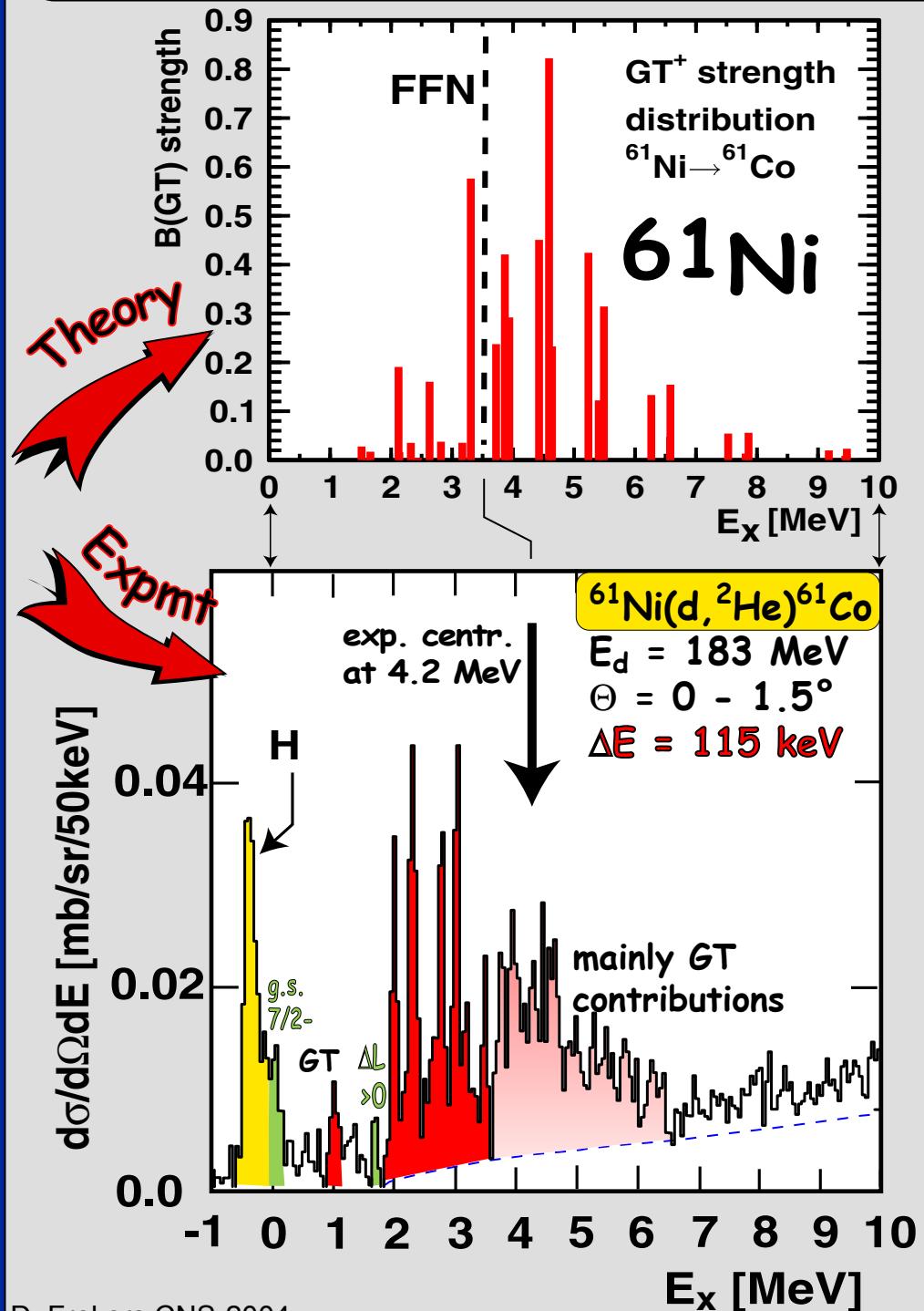
# odd-*A* odd-*n* nuclei

Astrophysics

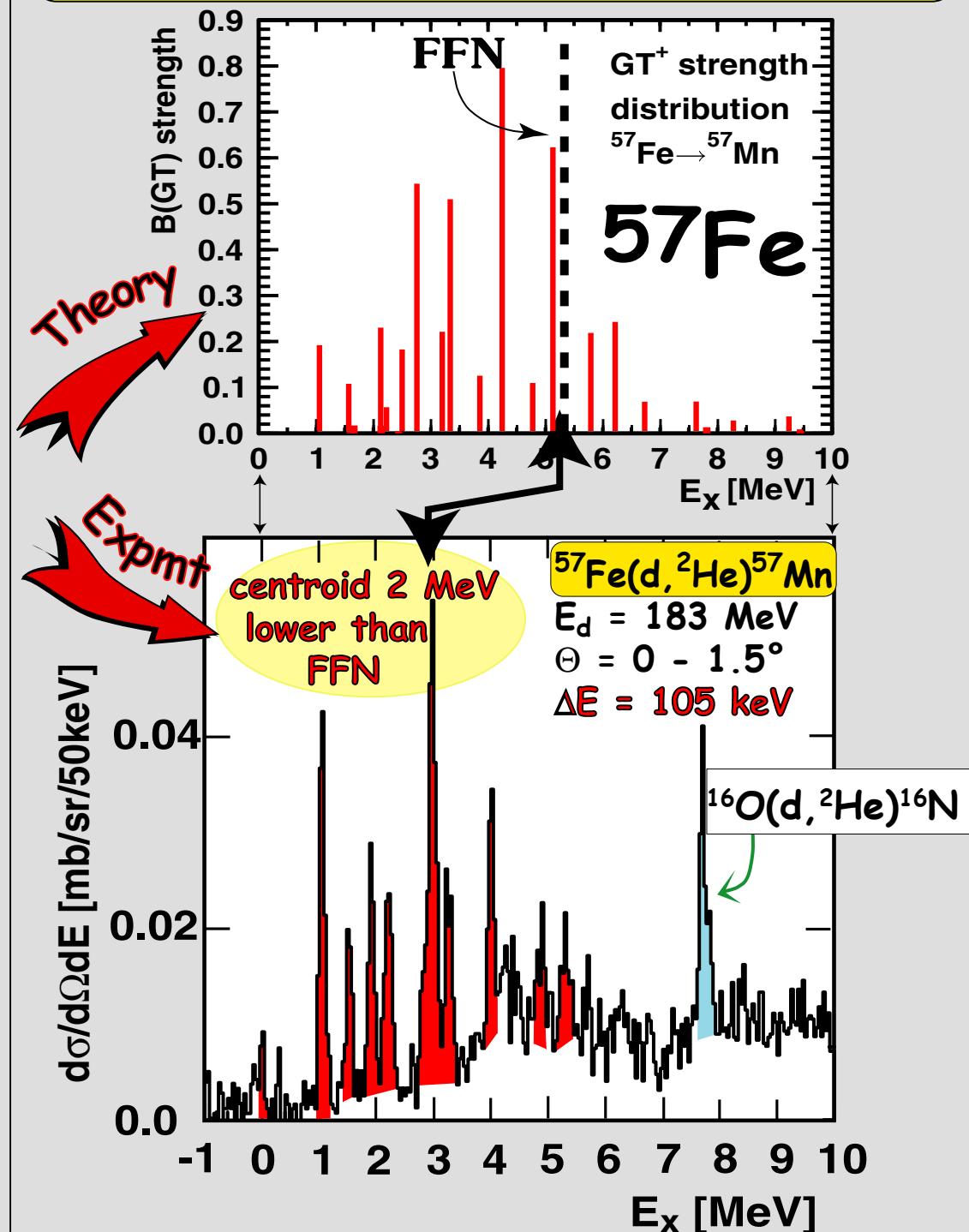
**GT<sup>+</sup>**



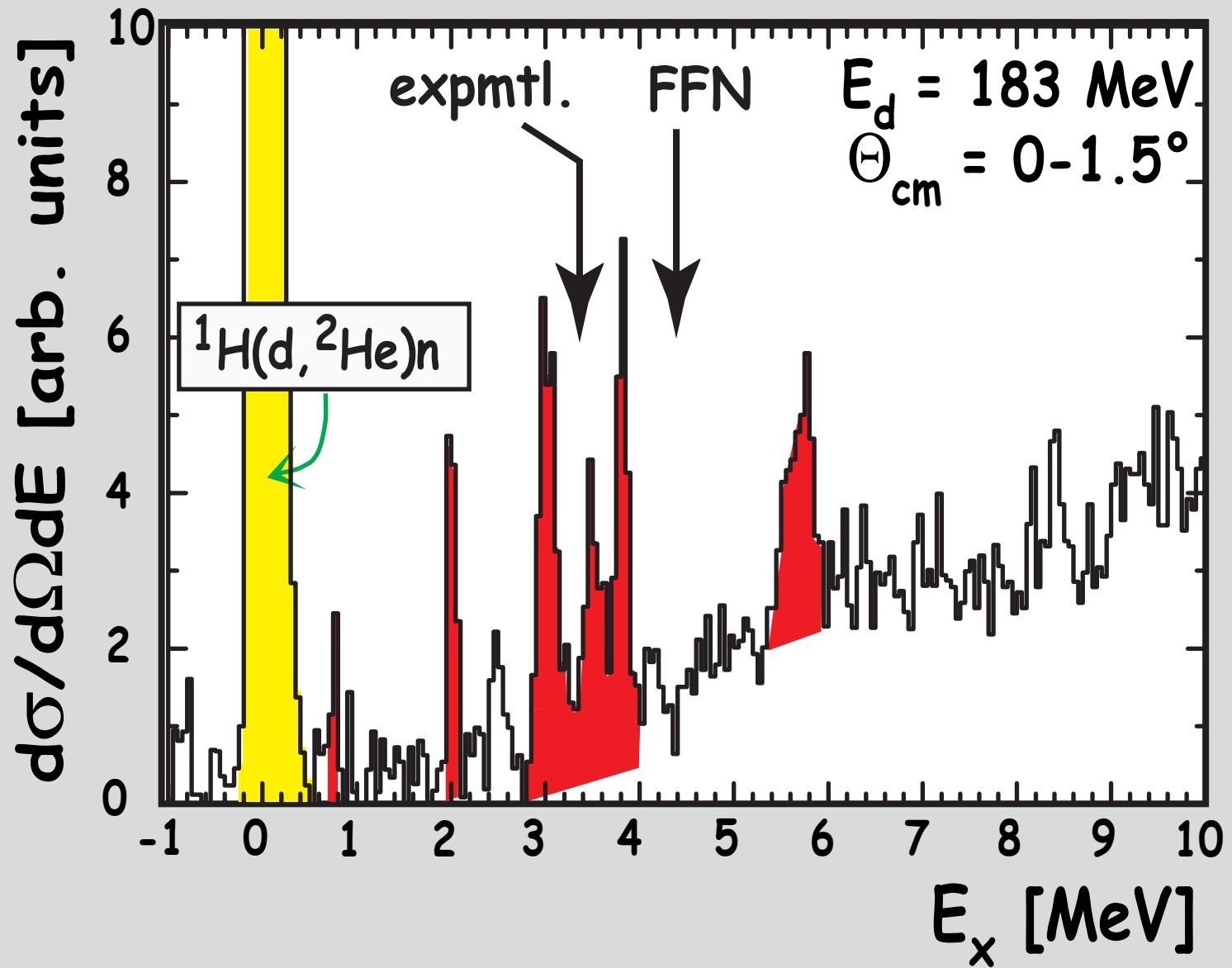
## $^{61}\text{Ni}(\text{d}, 2\text{He})^{61}\text{Co}$ : GT distribution



## $^{57}\text{Fe}(\text{d}, 2\text{He})^{57}\text{Mn}$ : GT distribution



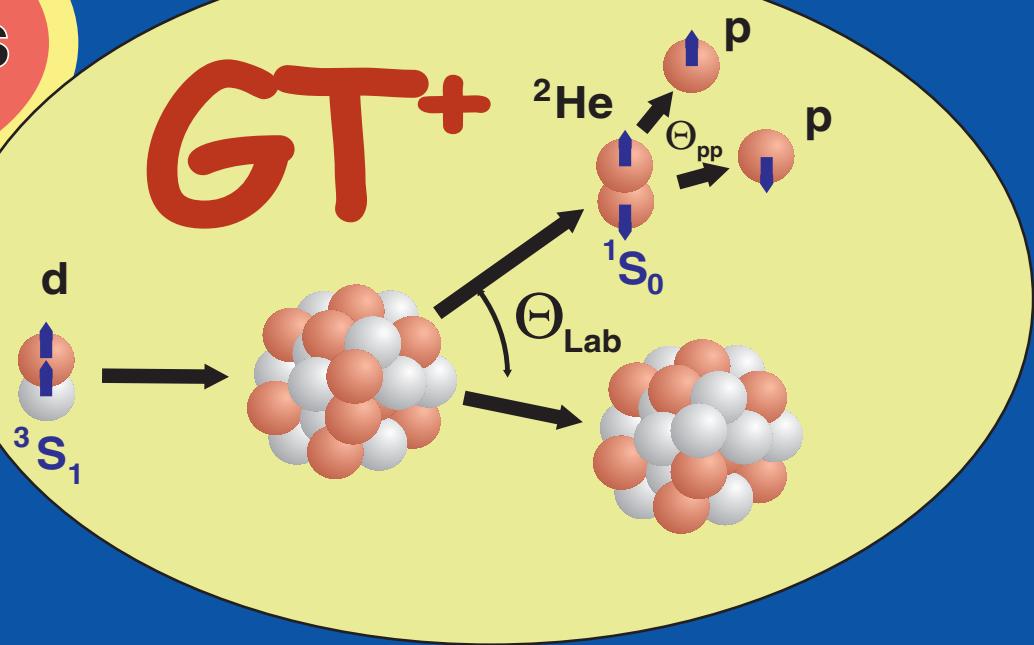
# $^{67}\text{Zn}(\text{d},^2\text{He})^{67}\text{Cu}$ : GT<sup>+</sup> distribution



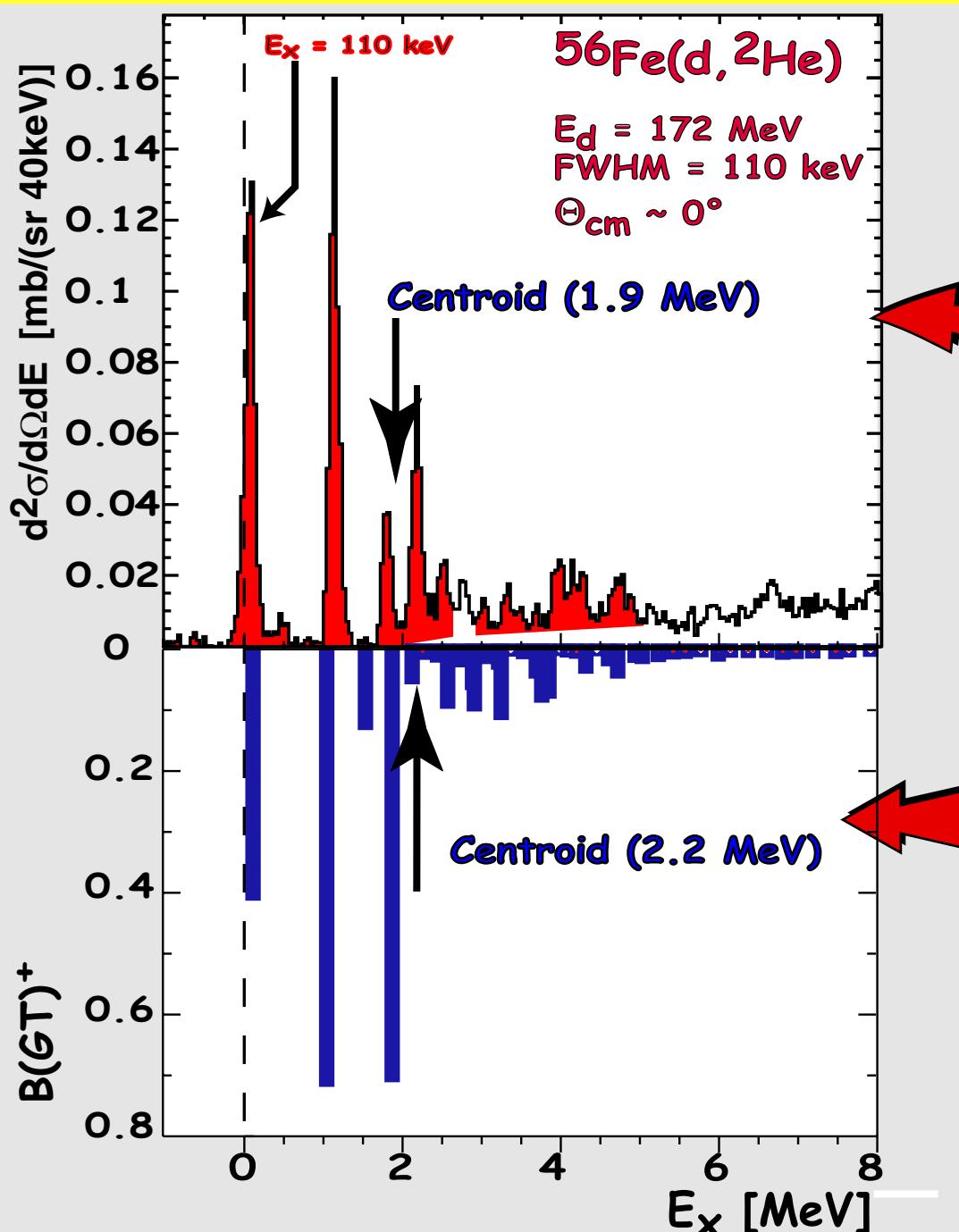
# even-even nuclei

Astrophysics

**GT<sup>+</sup>**



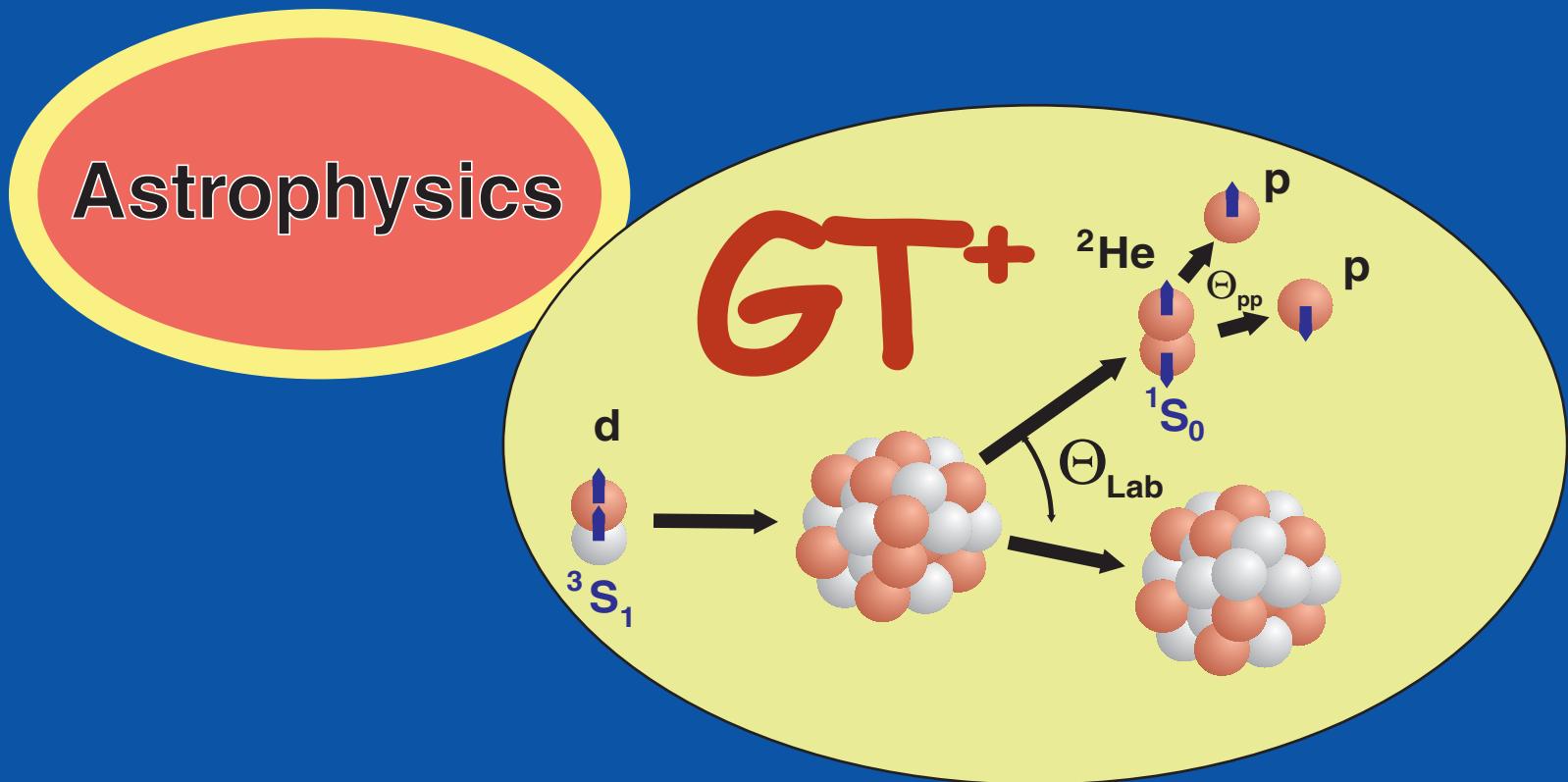
# $^{56}\text{Fe}(\text{d}, \text{d}^2\text{He})$ : Comparison with shell-model calculations



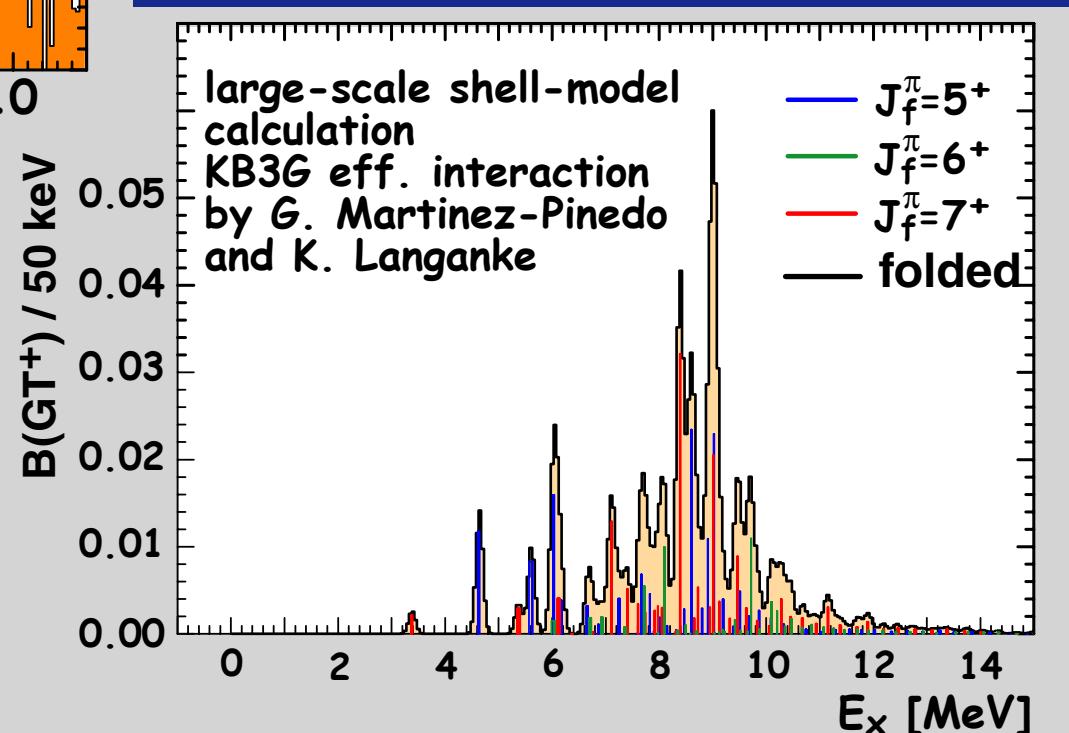
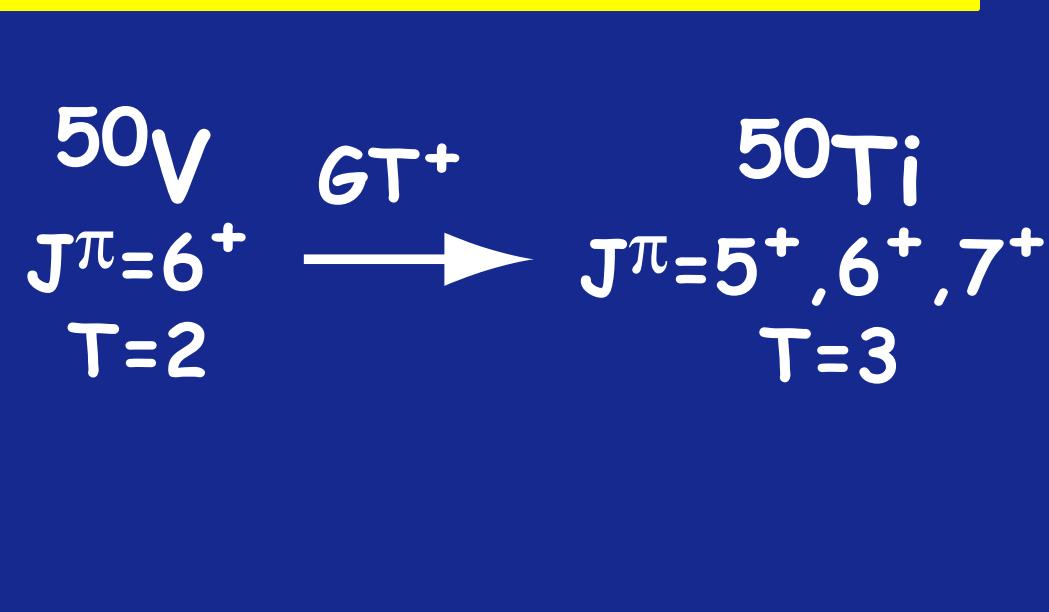
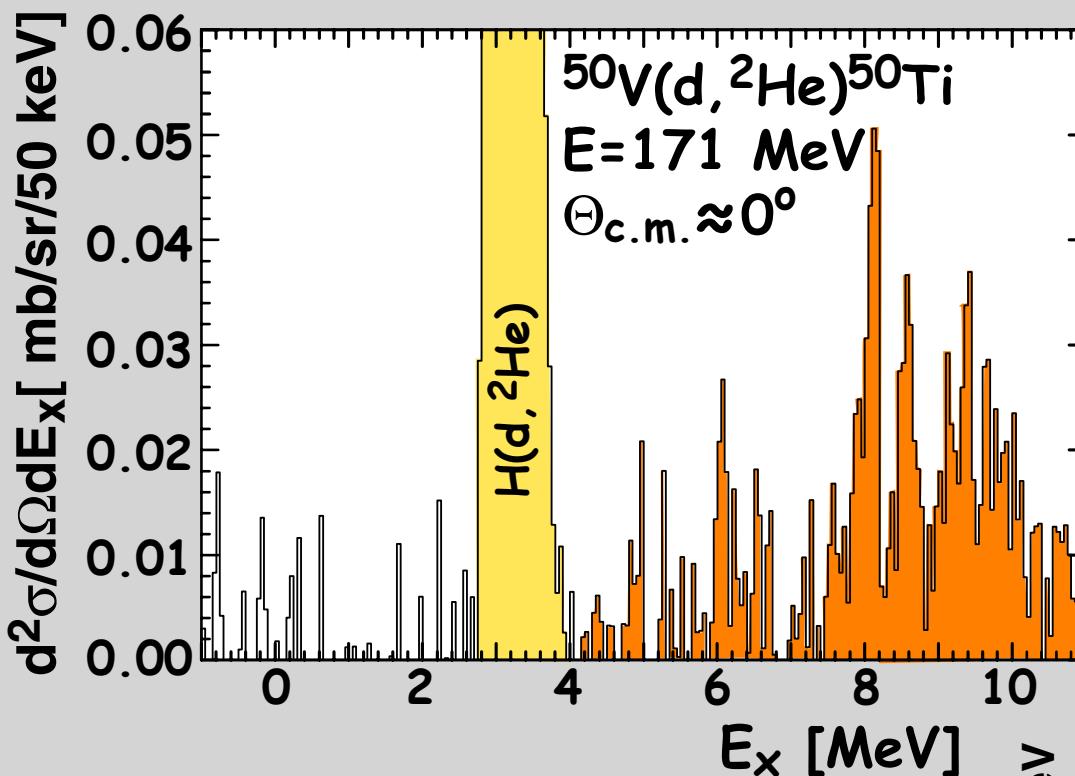
experiment

full fp-shell model  
calculations (KG3G)  
(G. Martinez-Pinedo)

# odd-odd nuclei



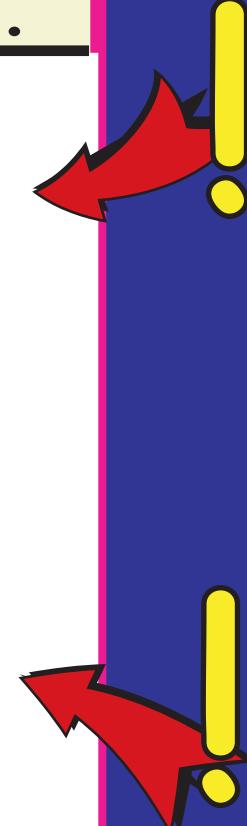
# $GT^+$ transitions from odd-odd nucleus $^{50}\text{V}(\text{d}, ^2\text{He})$



$GT^-$  centroid located  
at  $\sim 9 \text{ MeV} !!$

# GT+ centroid comparison

		FFN	SM	Exp.
even-even	Fe-56	3.8	2.2	1.9
	Ni-58	3.8	3.6	3.4
odd-A odd-p	V-51	3.8	4.7	4.6
odd-A odd-n	Fe-57	5.3	4.1	2.9
	Ni-61	3.5	4.6	4.2
	Zn-67	4.4	--	3.4
odd-odd	V-50	9.7	8.5	8.8

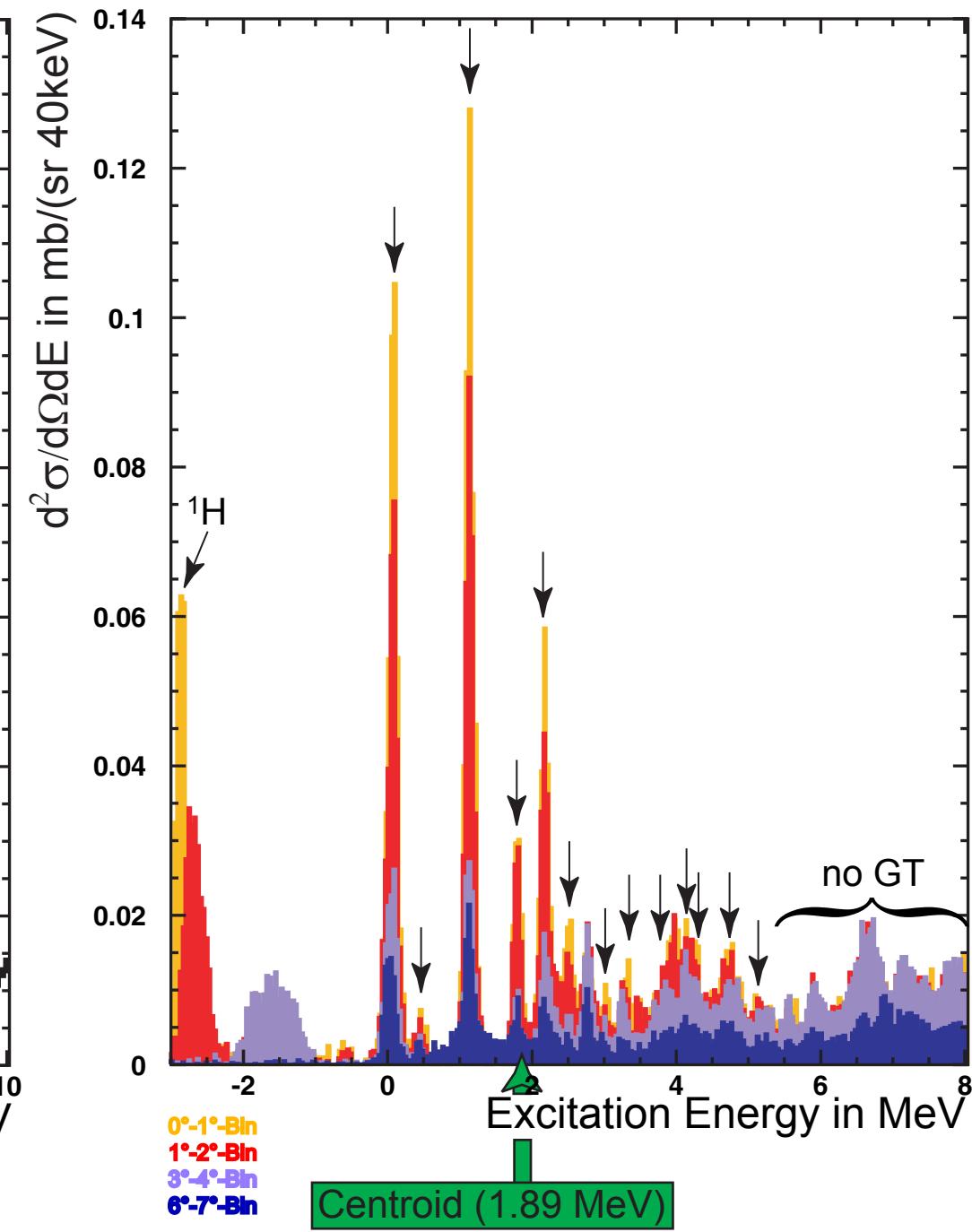
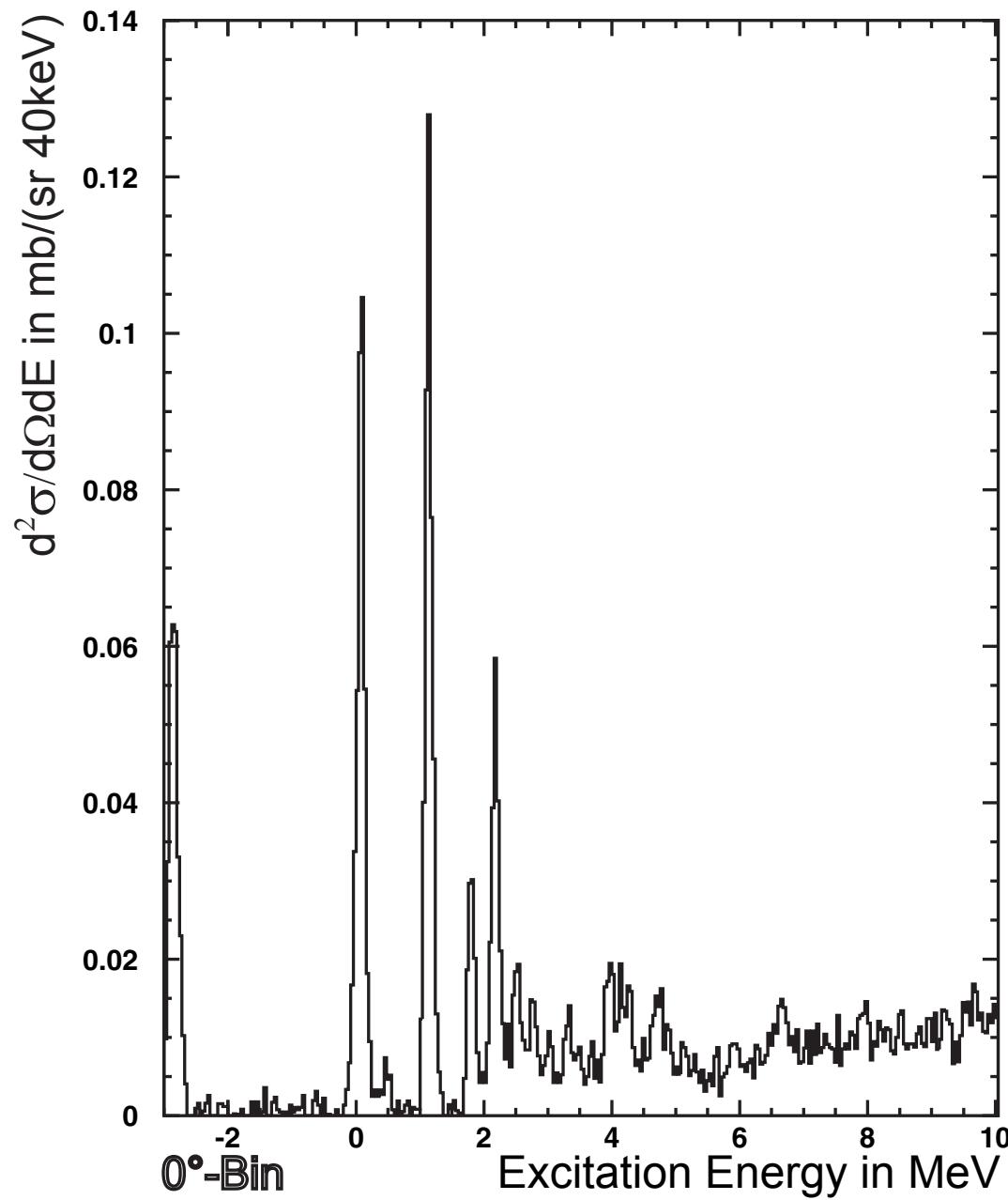


# CONCLUSIONS:

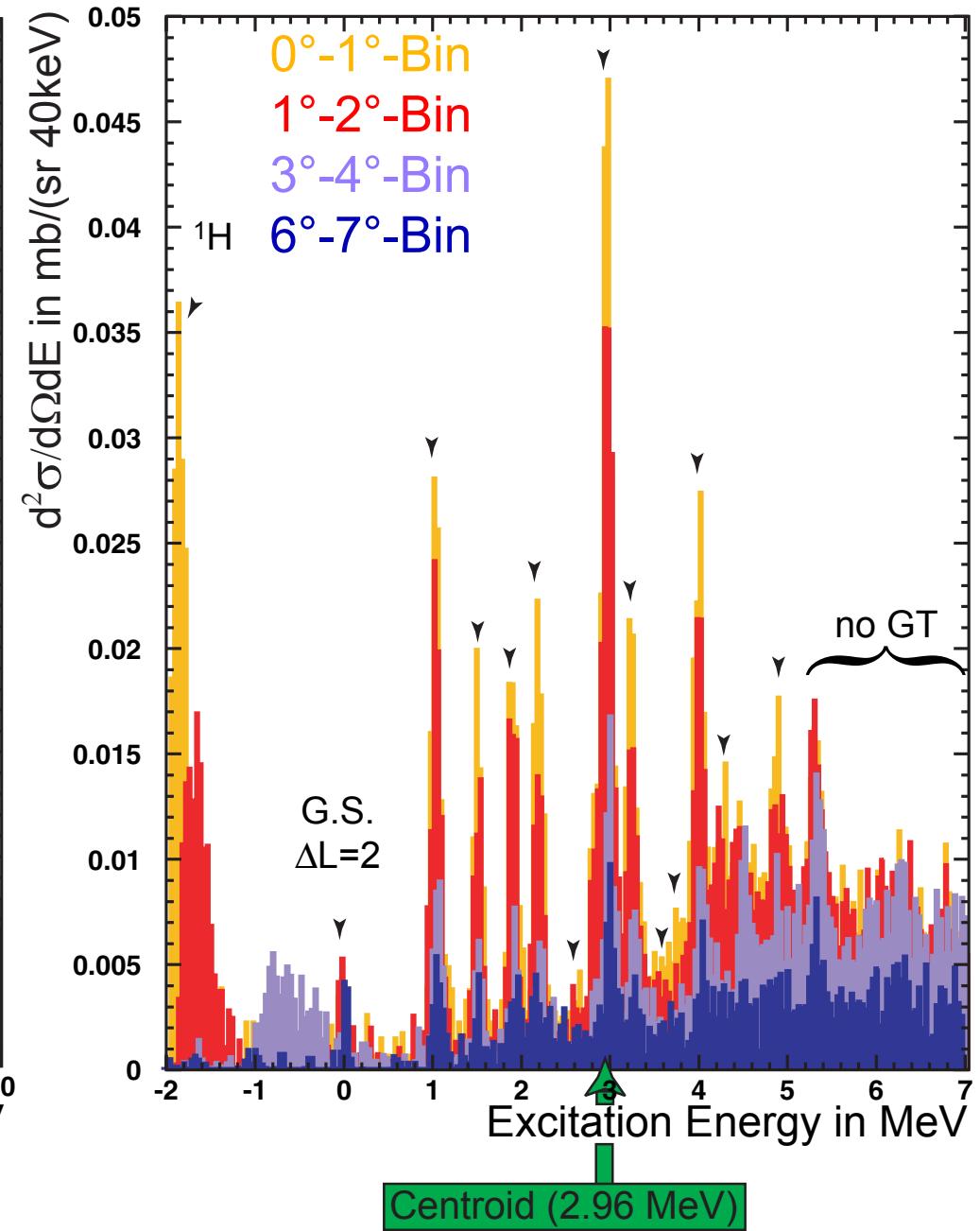
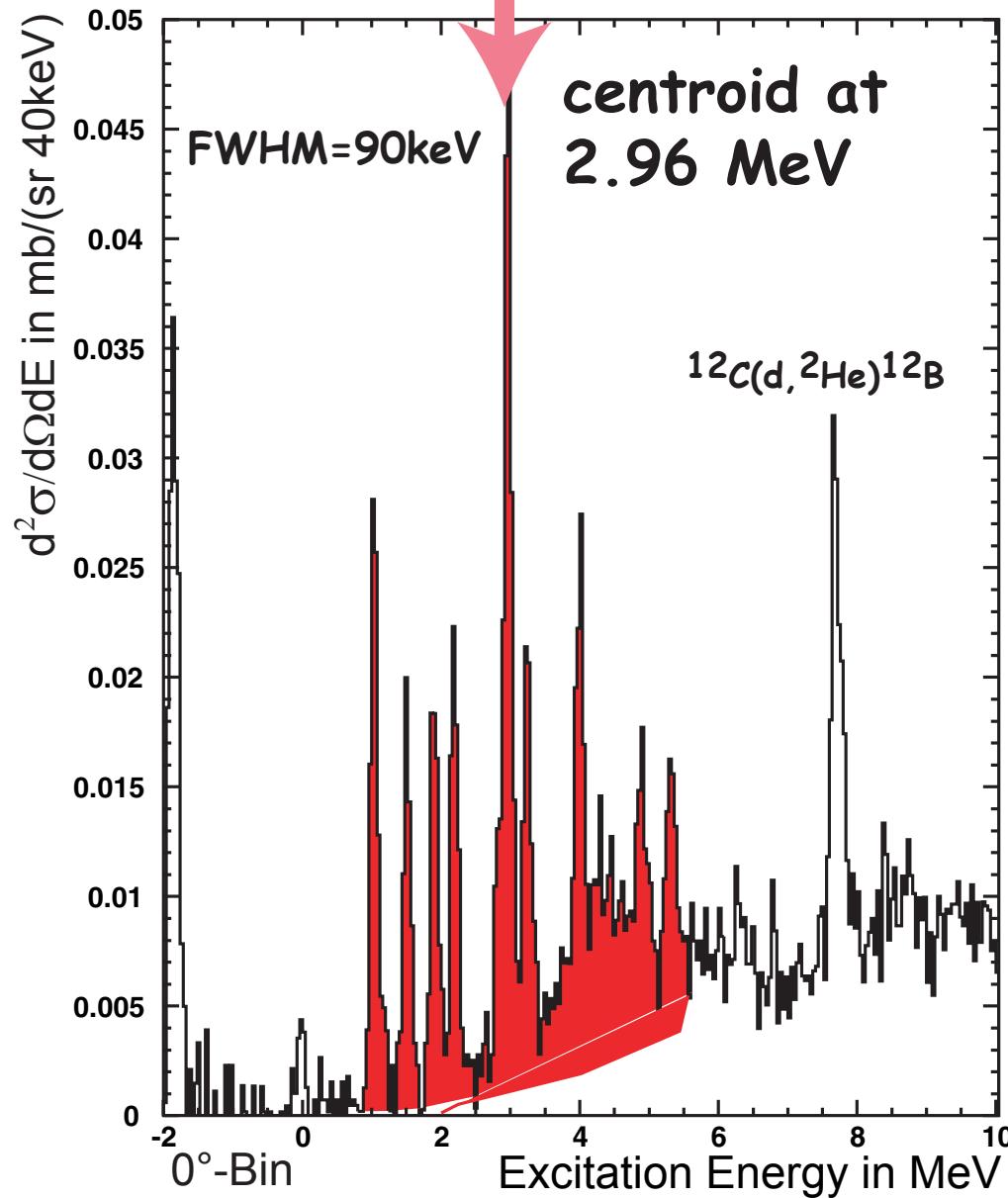
There are  
good news and bad news  
for a  
“**SUPERNOVA** in a computer”

we keep on the struggle

# Spectrum of the $^{56}\text{Fe}(\text{d},\text{He})^{56}\text{Mn}$ -Reaction

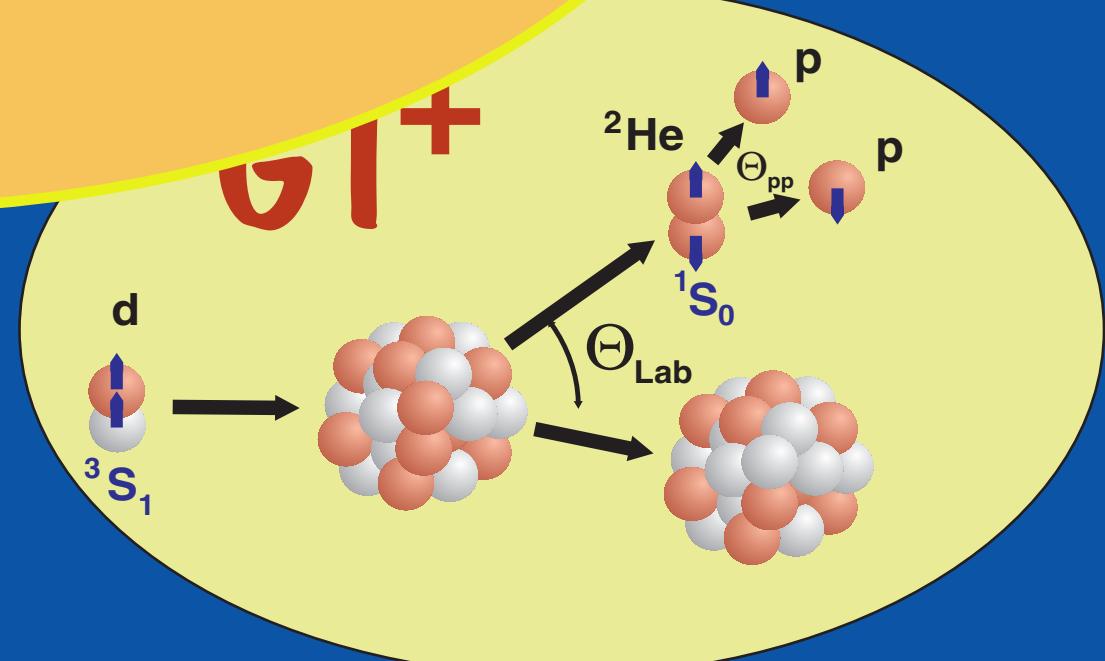


# Spectrum of the $^{57}\text{Fe}(\text{d},^2\text{He})^{57}\text{Mn}$ -Reaction



DF

# Double beta decay



# Neutrino questions

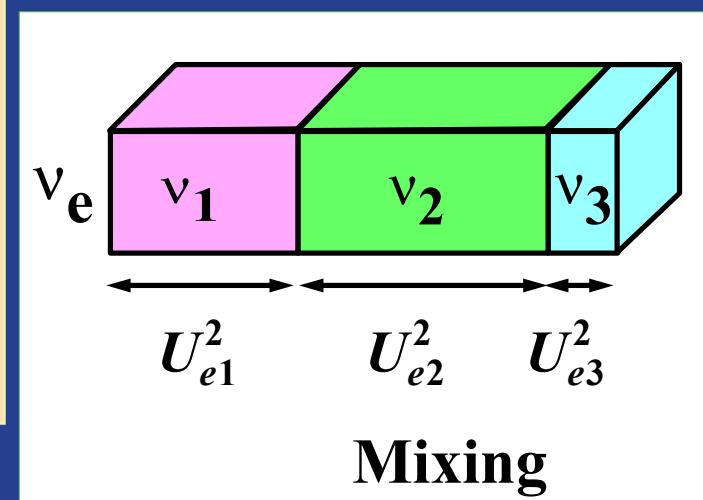
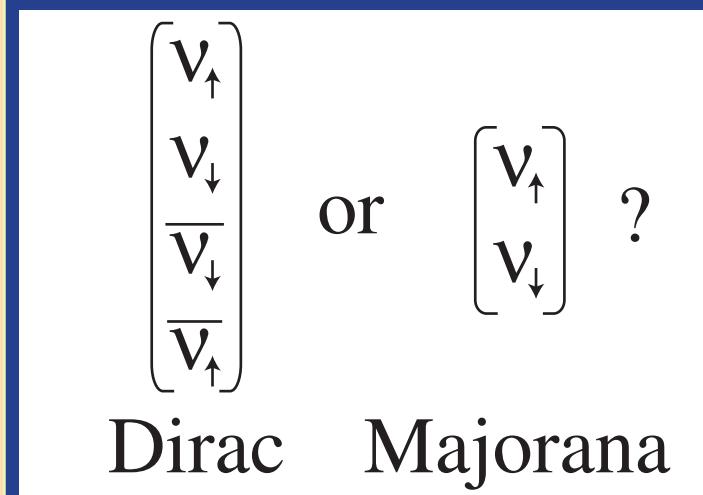
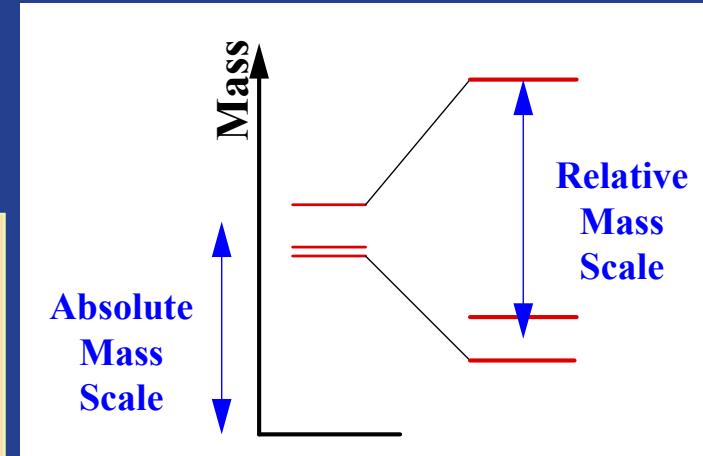
Main results from  $\nu$ -oscillation experiments:

- neutrinos have mass
- mass scale is  $\sim 50$  meV (but no absolute  $m_\nu$ !)
- flavour lepton number not conserved

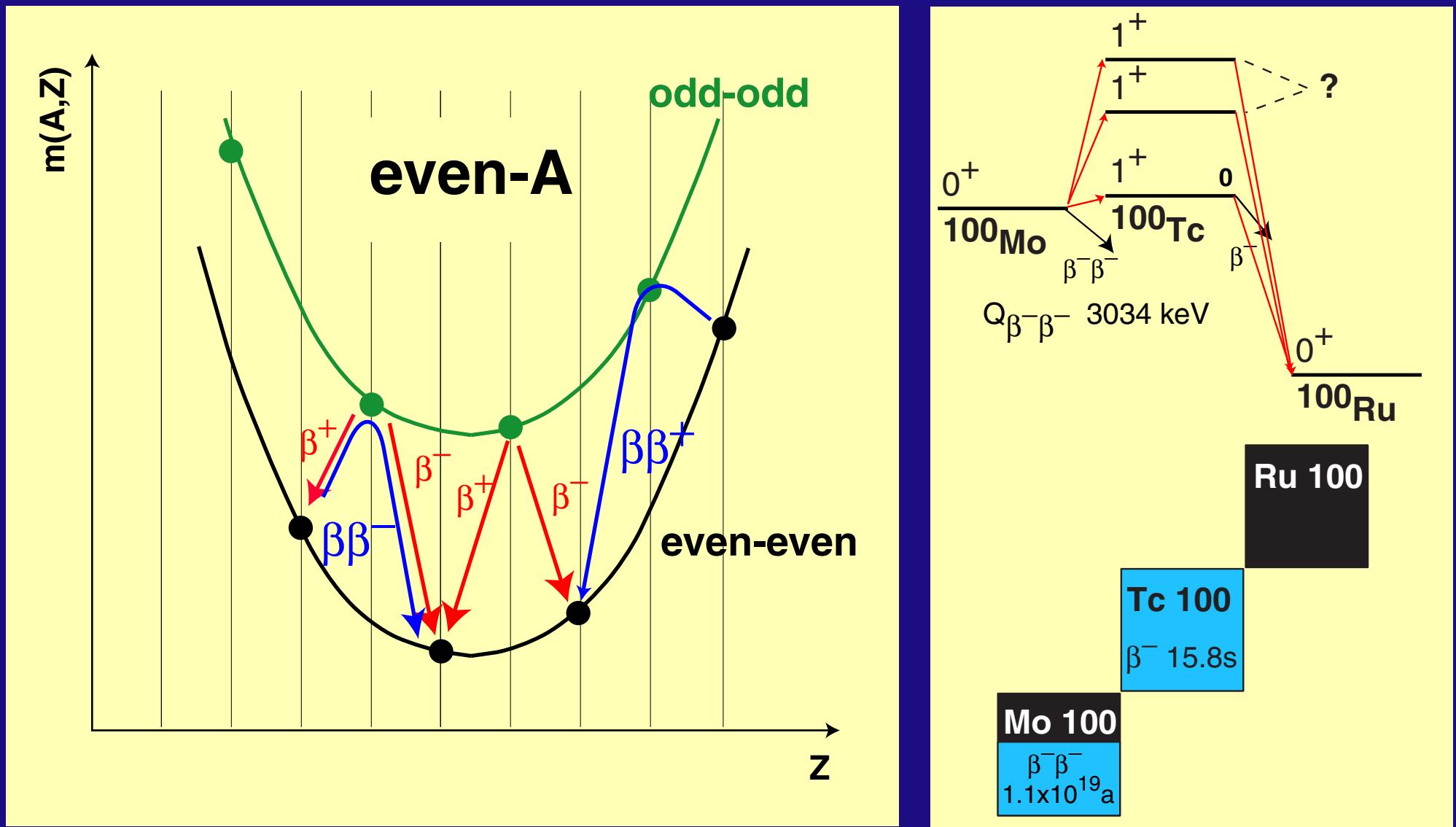
Total L-conservation?  
Hierarchical / degenerate mass pattern?

New information from  $0\nu\beta\beta$ -decay:

- Dirac or Majorana particle?
- Majorana neutrino violates L-conservation!
- Value for effective Majorana mass!

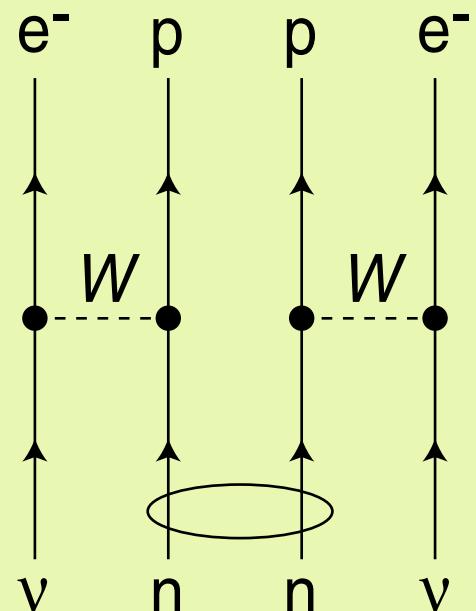


# Nuclear double beta decay



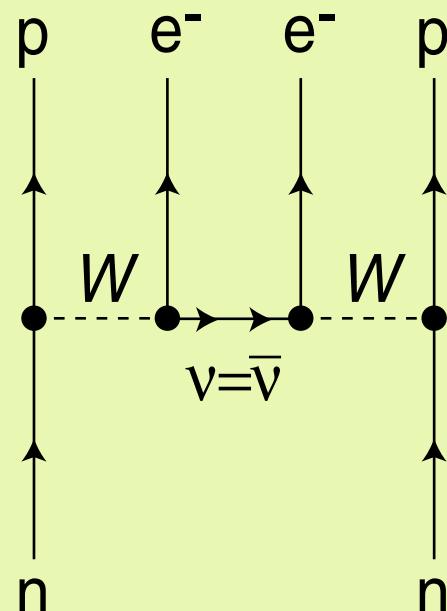
# Important $\beta\beta$ decay modes

( $2\nu\beta\beta$ )



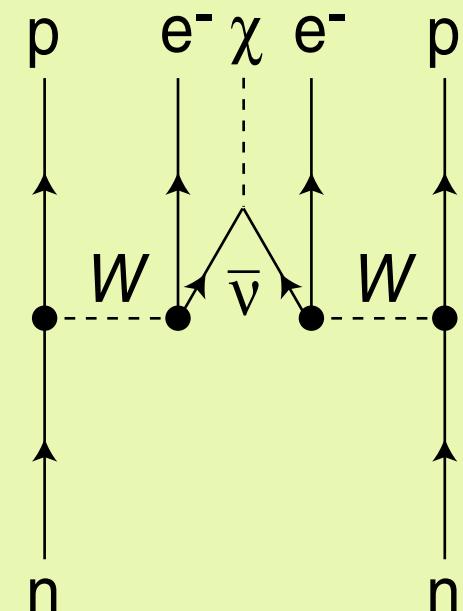
Dirac-Decay

( $0\nu\beta\beta$ )



Majorana-Decay

( $0\nu\chi\beta\beta$ )



Majoron-Decay

# 0νββ-decay: half-life & neutrino mass

$$\left[ T_{1/2}^{0\nu} (0^+ \rightarrow 0^+) \right]^{-1} = G^{0\nu} (E_0, Z) \left| M_{GT}^{0\nu} - \frac{g_V^2}{g_A^2} M_F^{0\nu} \right|^2 \langle m_\nu \rangle^2$$

measure!	look up	nuclear structure	ν mass
----------	---------	----------------------	-----------

$$M_{GT}^{0\nu} = \left\langle f \left| \sum_{lk} \boldsymbol{\sigma}_l \cdot \boldsymbol{\sigma}_k \boldsymbol{\tau}_l^+ \boldsymbol{\tau}_k^+ H(r_{lk}, \bar{A}) \right| i \right\rangle$$

$$M_F^{0\nu} = \left\langle f \left| \sum_{lk} \boldsymbol{\tau}_l^+ \boldsymbol{\tau}_k^+ H(r_{lk}, \bar{A}) \right| i \right\rangle$$

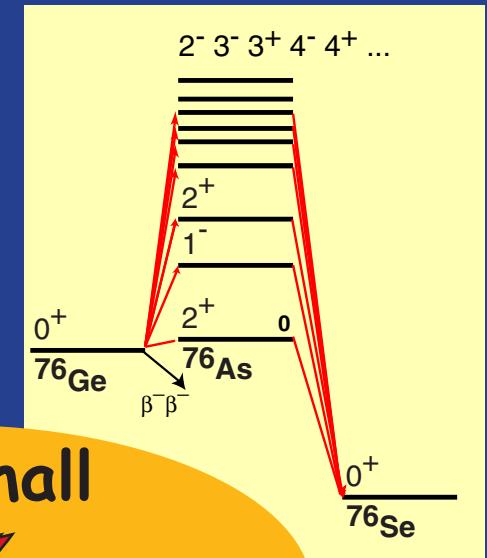
Neutrino potential  
(ν's don't escape  
from nucleus)

# 0νββ-decay: half-life & neutrino mass

$$M_{GT}^{0\nu} = \left\langle f \left| \sum_{lk} \sigma_l \cdot \sigma_k \tau_l^+ \tau_k^+ H(r_{lk}, \bar{A}) \right| i \right\rangle$$

$$M_F^{0\nu} = \left\langle f \left| \sum_{lk} \tau_l^+ \tau_k^+ H(r_{lk}, \bar{A}) \right| i \right\rangle$$

Neutrino potential



Expand expression with  $H(r, A)$

Many higher multipoles contribute!

$r_{lk}$  small  
q large ( $0.5 \text{ fm}^{-1}$ )

$$[t_{1/2}^{(0\nu)}]^{-1} = G^{(0\nu)} | M_{GT}^{(0\nu)} |^2 \langle m_\nu \rangle^2 + \text{Fermi contribution}$$

$$= G^{(0\nu)} \left| \sum_m \frac{\langle 0_{\text{g.s.}}^{(f)} || O_{\sigma\tau^-}(r, S, L) || J_m^\pi \rangle \langle J_m^\pi || O_{\sigma\tau^-}(r, S, L) || 0_{\text{g.s.}}^{(i)} \rangle}{1/2 Q_{\beta\beta}(0_{\text{g.s.}}^{(f)}) + E(J_m^\pi) - E_0} \right|^2 \langle m_\nu \rangle^2 + \text{Fermi contribution}$$

Easier case:

$2\nu\beta\beta$

# Half-lives & Matrix elements

Half life:

$$[t_{1/2}^{(2\nu)}]^{-1} = G^{(2\nu)} |M_{DGT}^{(2\nu)}|^2$$

Phase space + coupling constants:  $G \sim Q^{-11}$

$\beta\beta$  matrix element:

$$M_{DGT} = \sum_m \frac{\langle 0_{g.s.}^{(f)} || \sigma \tau^- || 1_m^+ \rangle \langle 1_m^+ || \sigma \tau^- || 0_{g.s.}^{(i)} \rangle}{1/2 Q_{\beta\beta}(0_{g.s.}^{(f)}) + E(1_m^+) - M_i}$$

All  $1^+$  levels must be considered!

Approximation:

$$M_{DGT} \approx \frac{M_S |M_{S'}|}{\Delta S}$$

$M_S$ : Single beta decay matrix elements

$\Delta S$ : Energy denominator

holds if

- only one strong  $1^+$  intermediate state
- further excited states weak or  $E_x$  high

2v

# DBD Experimental / theoretical results

Isotope	experimental $T_{1/2}$ [yr]	calculated $T_{1/2}$ [yr]
$^{48}\text{Ca}$	$(4.2 \pm 1.2) \times 10^{19}$	$6 \times 10^{18} \dots 5 \times 10^{20}$
$^{76}\text{Ge}$	$(1.3 \pm 0.1) \times 10^{21}$	$7 \times 10^{19} \dots 6 \times 10^{22}$
$^{82}\text{Se}$	$(9.2 \pm 1.0) \times 10^{19}$	$3 \times 10^{18} \dots 6 \times 10^{21}$
$^{96}\text{Zr}$	$(1.4 \pm 0.8) \times 10^{19}$	$3 \times 10^{17} \dots 6 \times 10^{20}$
$^{100}\text{Mo}$	$(8.0 \pm 0.6) \times 10^{18}$	$1 \times 10^{17} \dots 2 \times 10^{22}$
$^{116}\text{Cd}$	$(3.2 \pm 0.3) \times 10^{19}$	$3 \times 10^{18} \dots 2 \times 10^{21}$
$^{128}\text{Te}$	$(7.2 \pm 0.3) \times 10^{24}$	$9 \times 10^{22} \dots 3 \times 10^{25}$
$^{130}\text{Te}$	$(2.7 \pm 0.1) \times 10^{21}$	$2 \times 10^{19} \dots 7 \times 10^{20}$
$^{150}\text{Nd}$	$(7.0 \pm 1.7) \times 10^{18}$	$2 \times 10^{16} \dots 4 \times 10^{20}$

Matrix elements from different nuclear structure models vary by factor 10



Factor 100 on half-life



Similar situation for  $^{0\nu}\beta\beta$ -decay



Need calibration points for  $\beta\beta$ -decay calculations!

# Measurement of $M_{DGT}^{(2v)}$ thru hadronic probes

$$M_{DGT} = \sum_m \frac{\langle 0_{g.s.}^{(f)} || \sigma\tau^- || 1_m^+ \rangle \langle 1_m^+ || \sigma\tau^- || 0_{g.s.}^{(i)} \rangle}{1/2 Q_{\beta\beta}(0_{g.s.}^{(f)}) + E(1_m^+) - M_i}$$

$$= \sum_m \frac{M_m^{GT+} M_m^{GT-}}{1/2 Q_{\beta\beta}(0_{g.s.}^{(f)}) + E(1_m^+) - M_i}$$

Measure  $B(GT+)$  through  $(n,p)$ -type reactions

Measure  $B(GT-)$  through  $(p,n)$ -type reactions

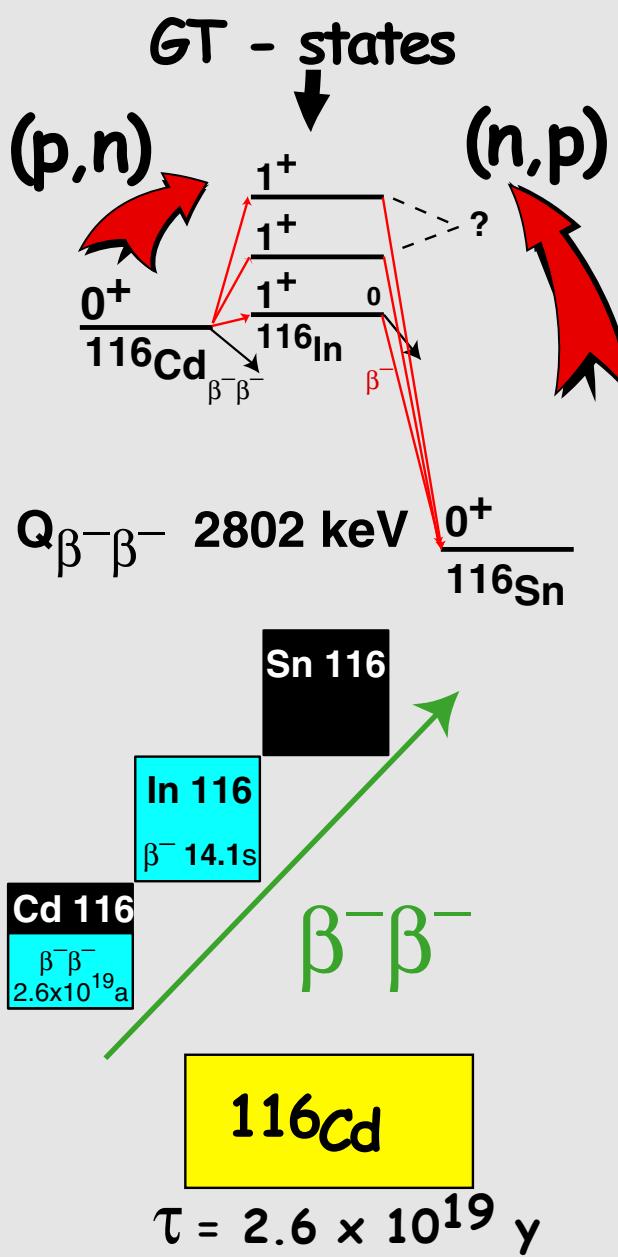
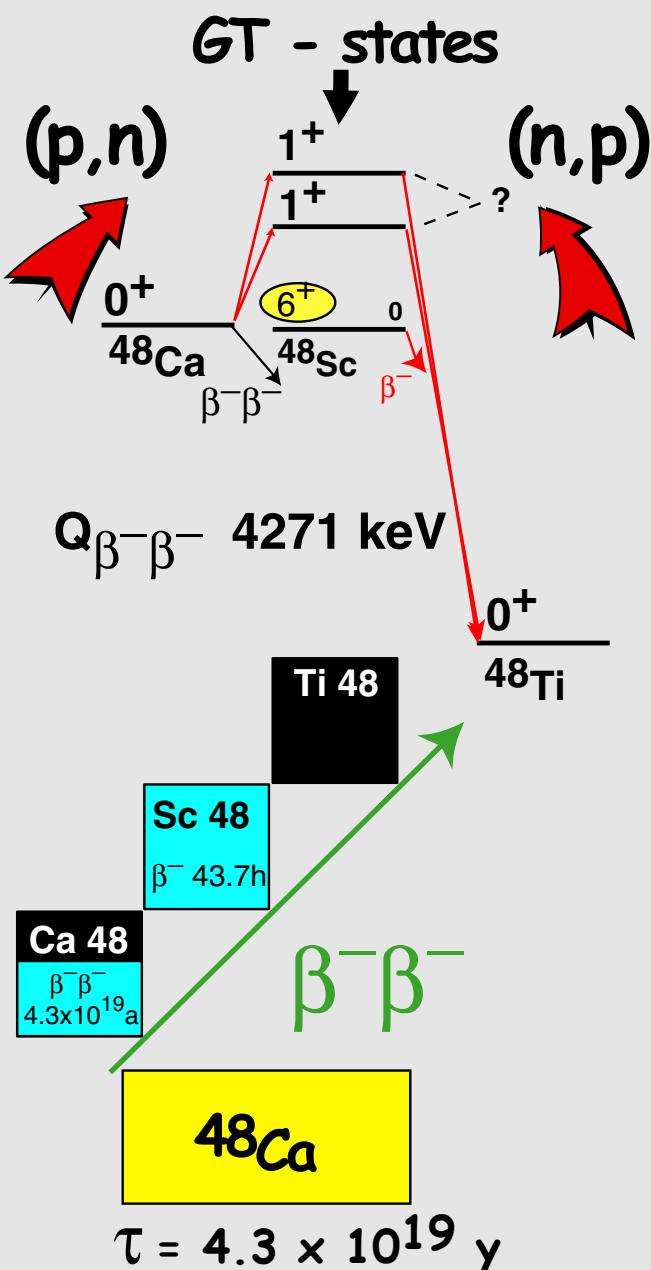
$$B(GT) = \frac{1}{2J_i + 1} | M(GT) |^2$$

- Phase cannot be measured
- Simple relation  $\sigma \leftrightarrow B(GT)$
- Little model dependence

$$B(GT) = \hat{\sigma}(GT) \frac{d\sigma(q=0)}{d\Omega}$$

forward  
angles

# The $2\nu$ double- $\beta$ decay



$\tau$  from counting experiments and as 2nd order weak process ( $\beta^- \rightarrow \beta^-$ ) !!!

Half life:

$$[t_{1/2}]^{-1} = G^{(2\nu)} | M_{DGT} |^2$$

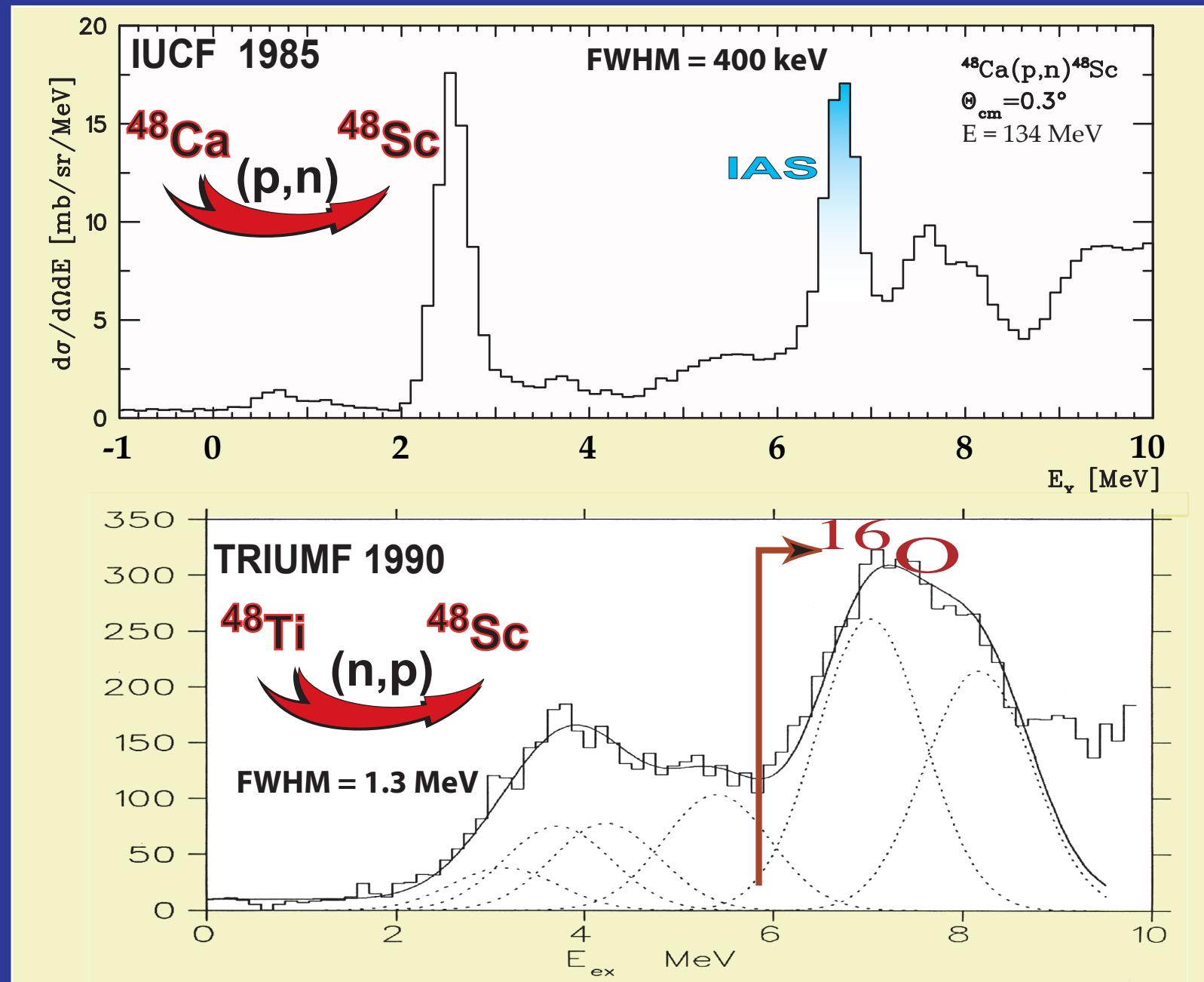
$M_{DGT} =$

$$\sum_m \frac{\langle 0_{g.s.}^{(f)} || \sigma \tau^- || 1_m^+ \rangle \langle 1_m^+ || \sigma \tau^- || 0_{g.s.}^{(i)} \rangle}{1/2 Q_{\beta\beta}(0_{g.s.}^{(f)}) + E(1_m^+) - E_0}$$

$$G^{(2\nu)} \sim (Q_{\beta\beta})^{11}$$

matrix elements available thru  $(p,n)$  and  $(n,p)$  type reactions

# $^{48}\text{Ca} - ^{48}\text{Sc} - ^{48}\text{Ti}$

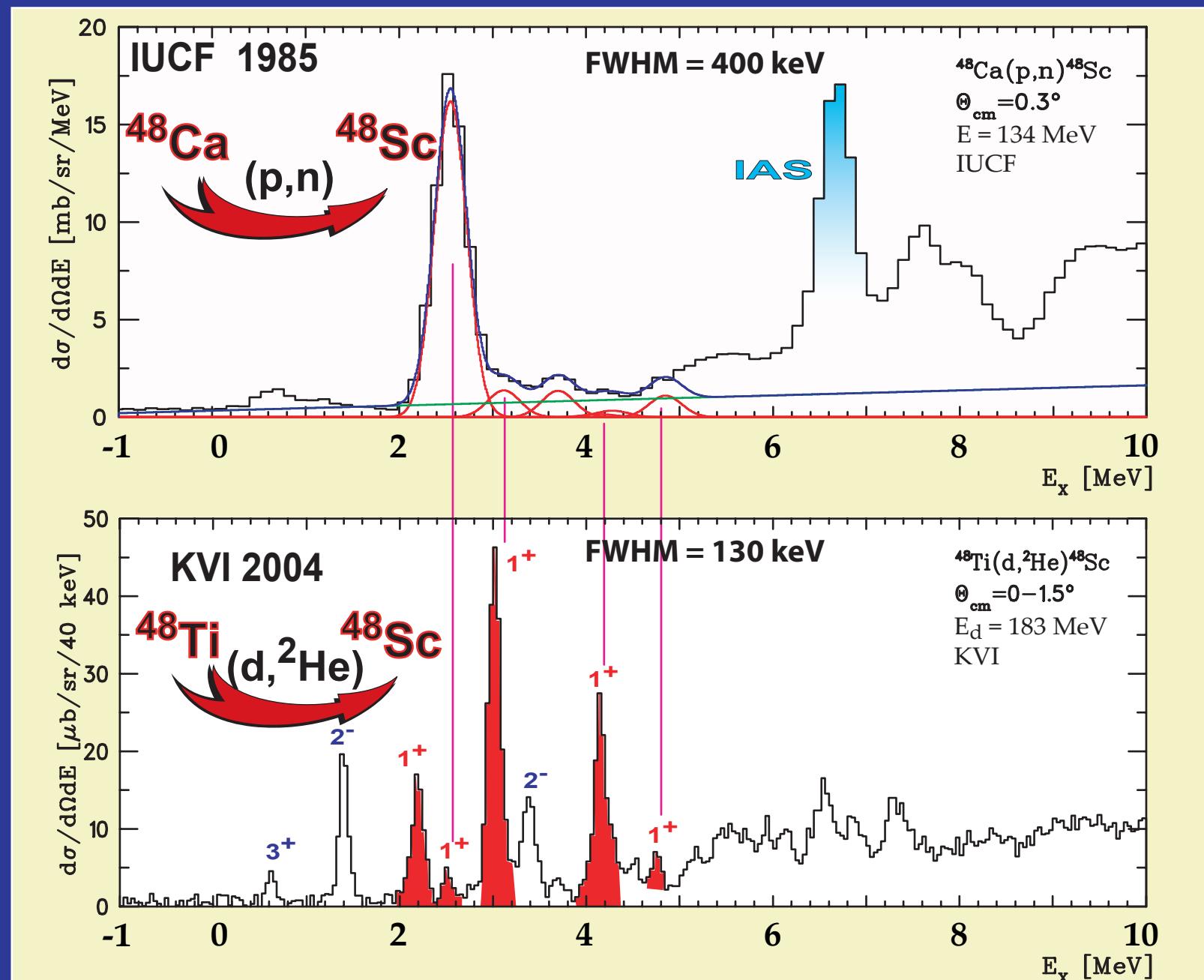


(p,n)

(n,p)

How to connect  
these states ??

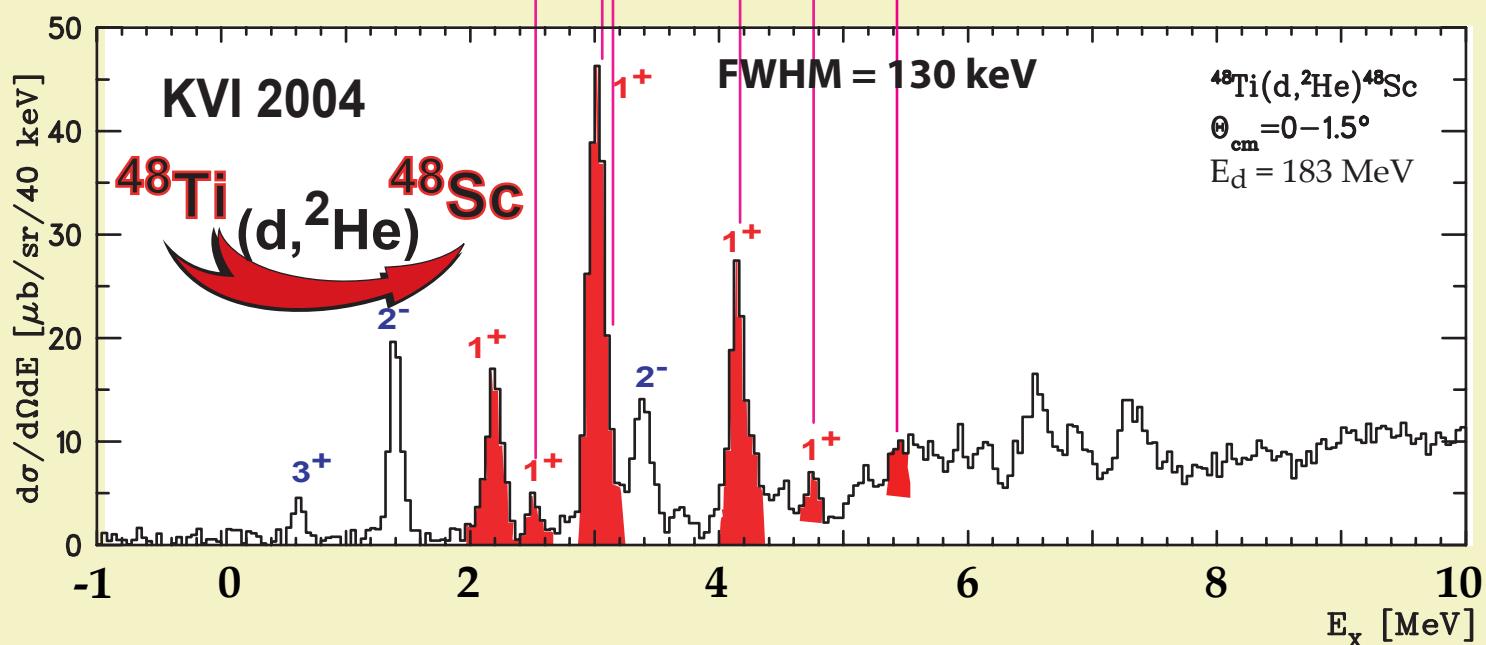
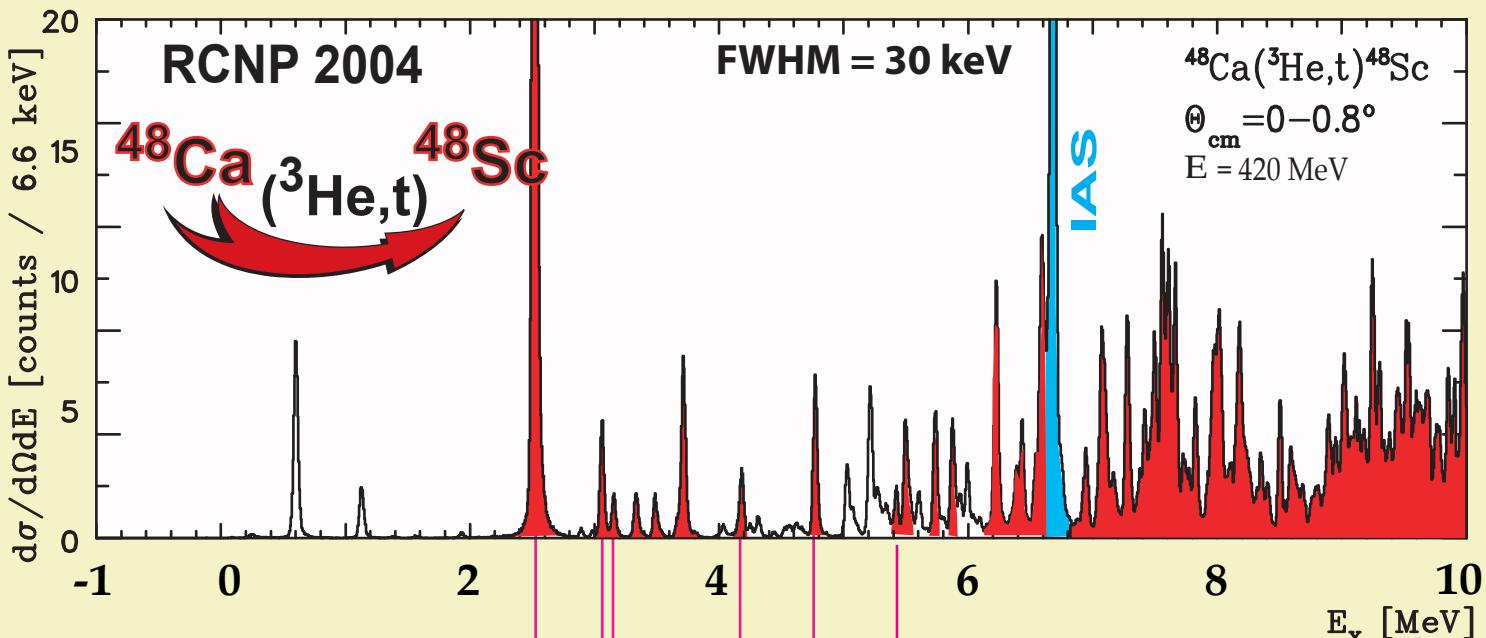
# $^{48}\text{Ca} - ^{48}\text{Sc} - ^{48}\text{Ti}$



(p,n)

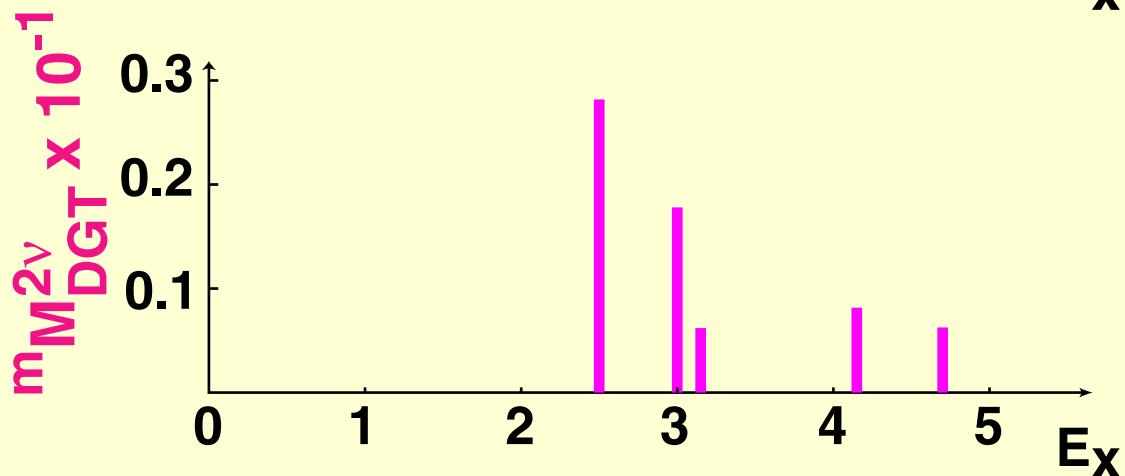
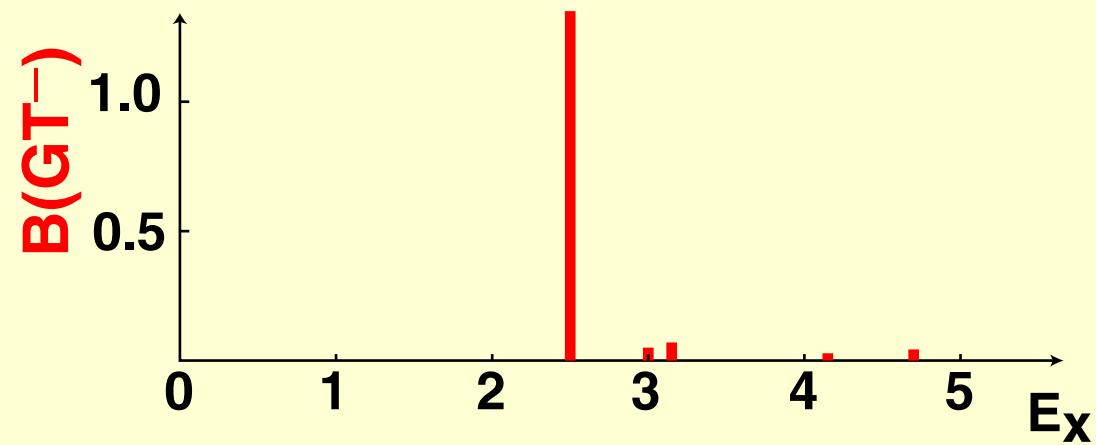
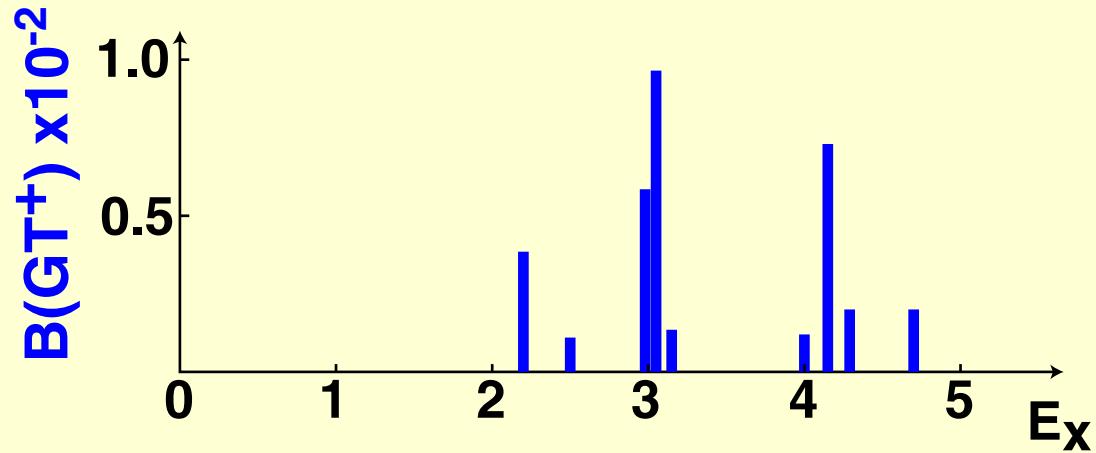
(d, $^2\text{He}$ )

# $^{48}\text{Ca} - ^{48}\text{Sc} - ^{48}\text{Ti}$



( ${}^3\text{He}, t$ )

(d,  ${}^2\text{He}$ )



## Experimental matrix elements

$$M_{DGT} = \sum_m m M_{DGT} / E_m$$

$$= 0.0668 \pm 0.0097$$



$$T_{1/2} = (2.04 \pm 0.60) \times 10^{19} \text{ yr}$$

Compare to counting exp't:

$$T_{1/2} = (4.3 \pm 2.5) \times 10^{19} \text{ yr}$$

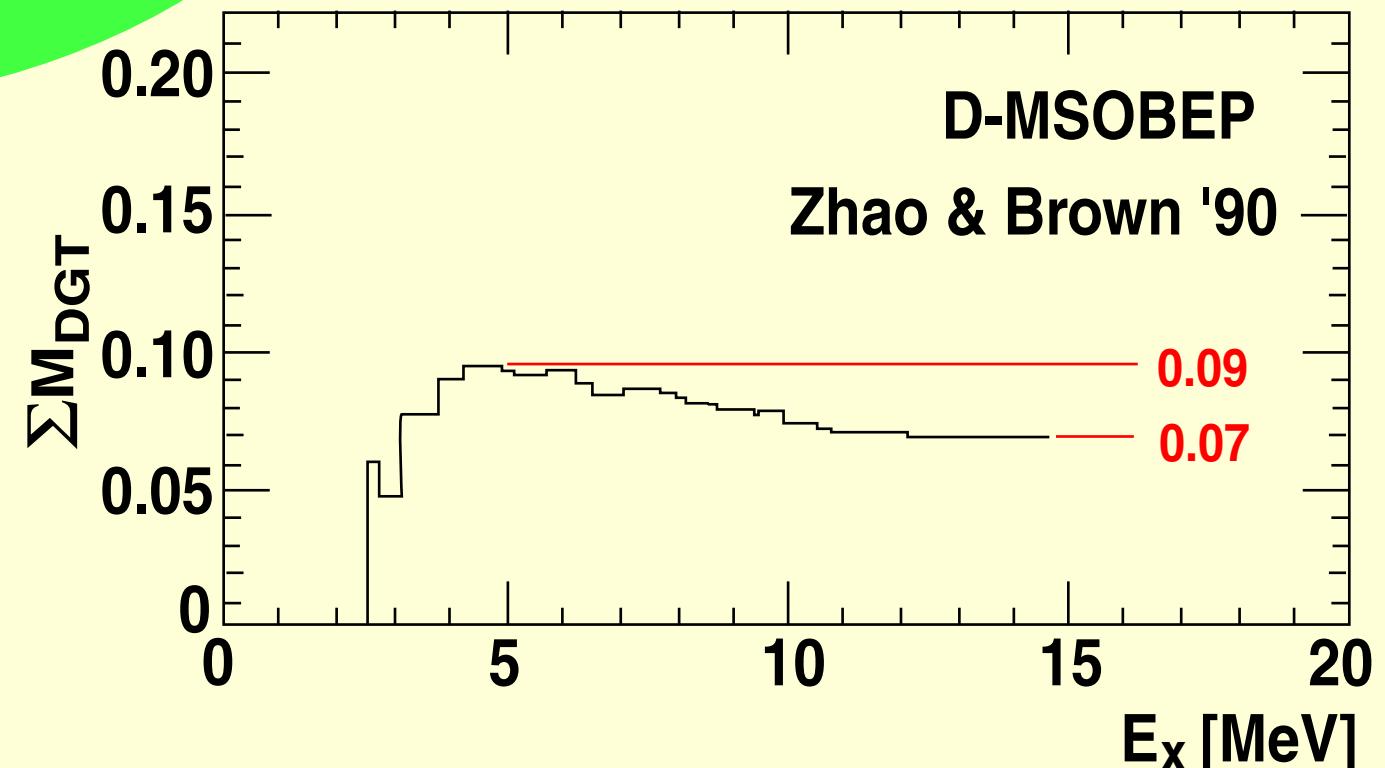
# Higher lying states ( $E_x > 5$ MeV)

SHELL MODEL

Reduction of  
matrix element  
by ~ 25%



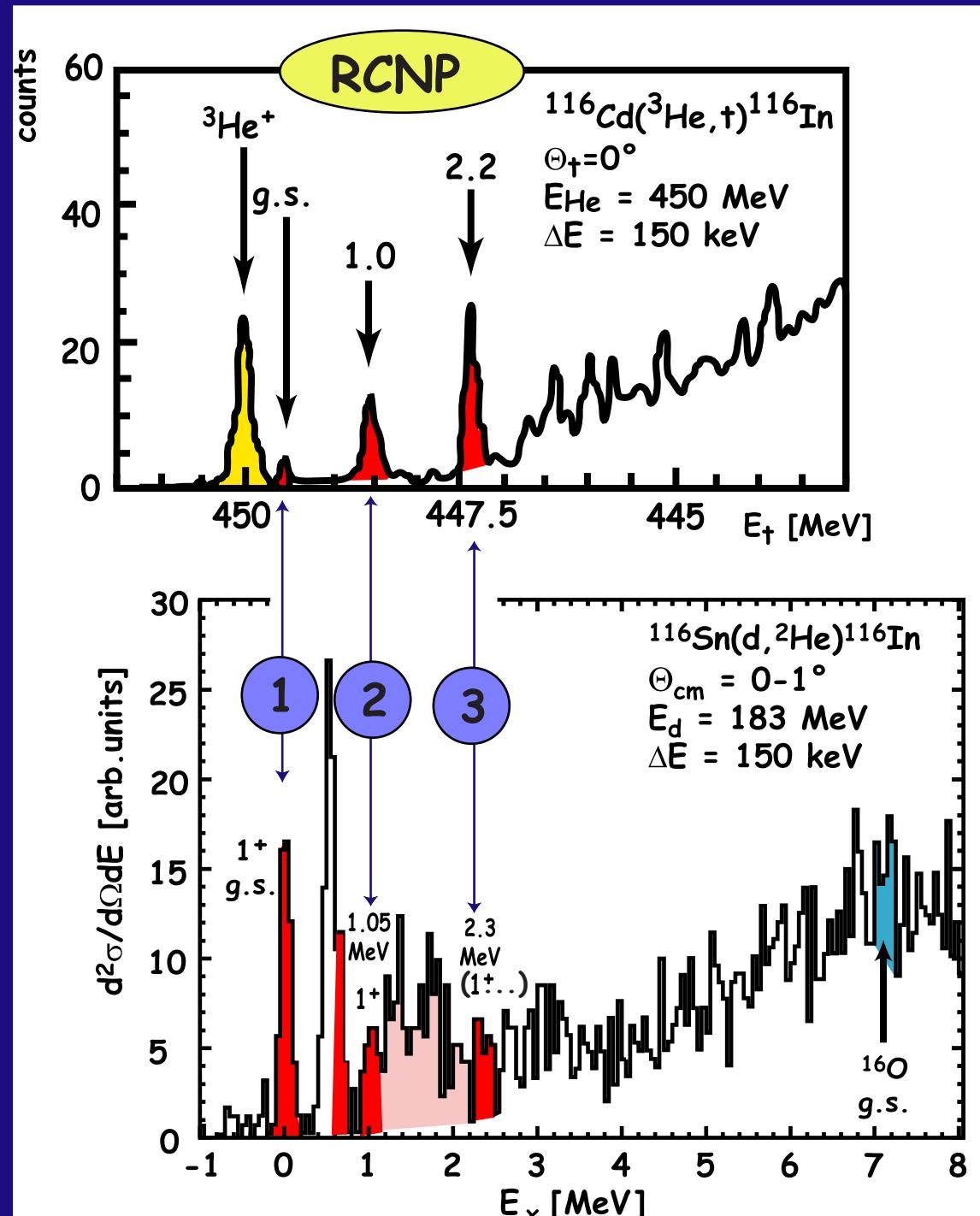
$$T_{1/2} = 3.5 \times 10^{19} \text{ yr}$$



# $^{116}\text{Cd}$ $2\nu\beta\beta$ decay

	$B(GT^-)$	$B(GT^+)$	$M_{DGT}^m$	running sum $\Sigma M_{DGT}$
1	0.032	0.235	0.028	0.028
2	0.12	0.12	0.029	0.057
3	0.17	0.05	0.017	0.074

Matrix element from counting experiment:  
 $\Sigma M_{DGT} = 0.069 \pm 0.009$



preliminary



# Study of Gamow-Teller transitions to intermediate states in $\beta\beta$ -decay

**Status:**

**Finished:**

$^{48}\text{Ca}$

$^{116}\text{Cd}$

**Proposed  
for 2004:**

$^{76}\text{Ge}$

$^{96}\text{Zr}$

$^{100}\text{Mo}$

$^{150}\text{Nd}$

**2005-2007:**

$^{82}\text{Se}$

$^{128,130}\text{Te}$

$^{136}\text{Xe}$



Westfälische  
Wilhelms-Universität  
Münster

# The case of $^{48}\text{Ca}$

$$T_{1/2} \sim G \sim Q^{-11}$$

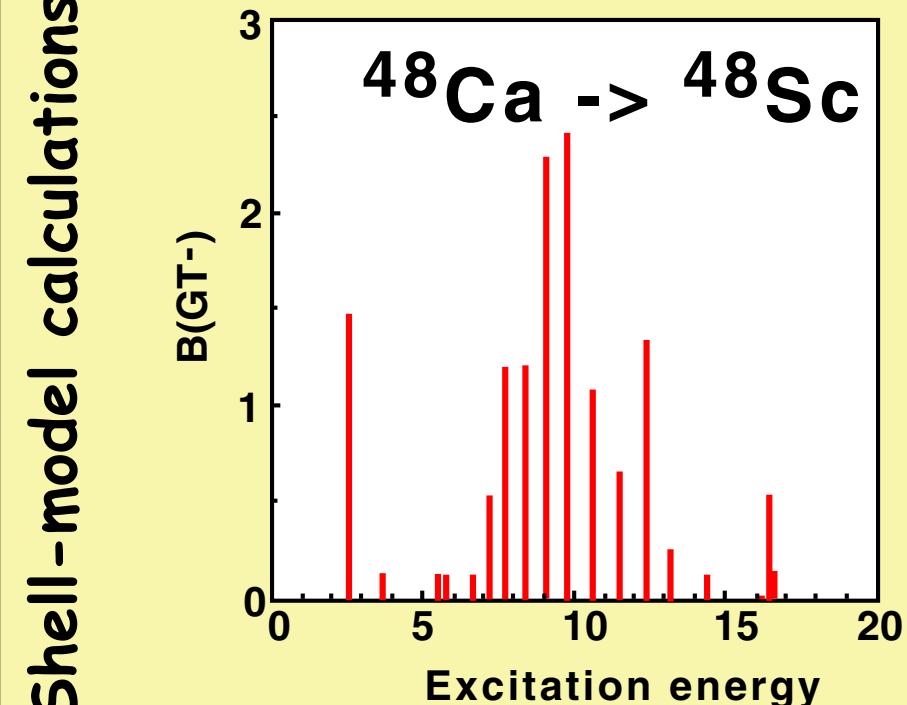
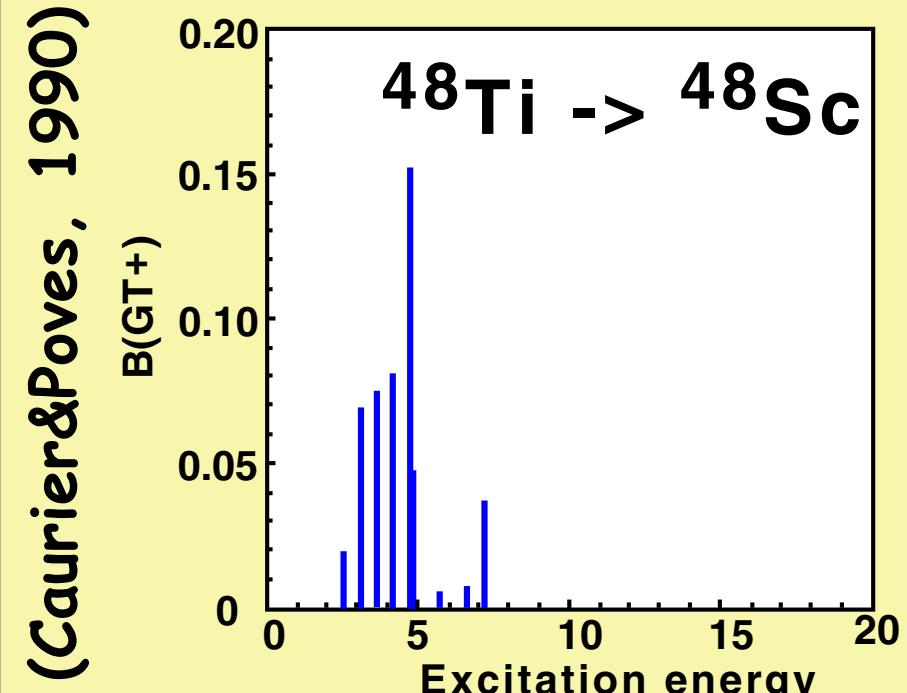
$^{48}\text{Ca}$

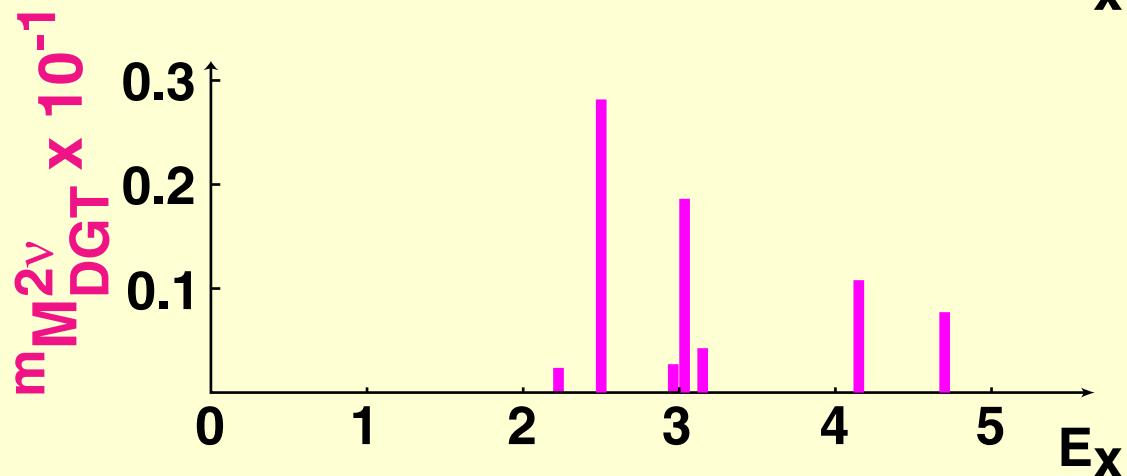
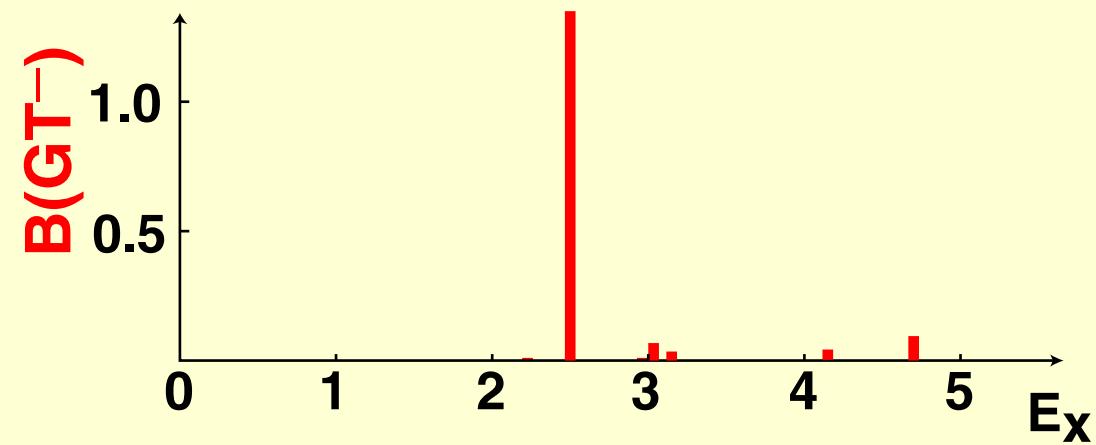
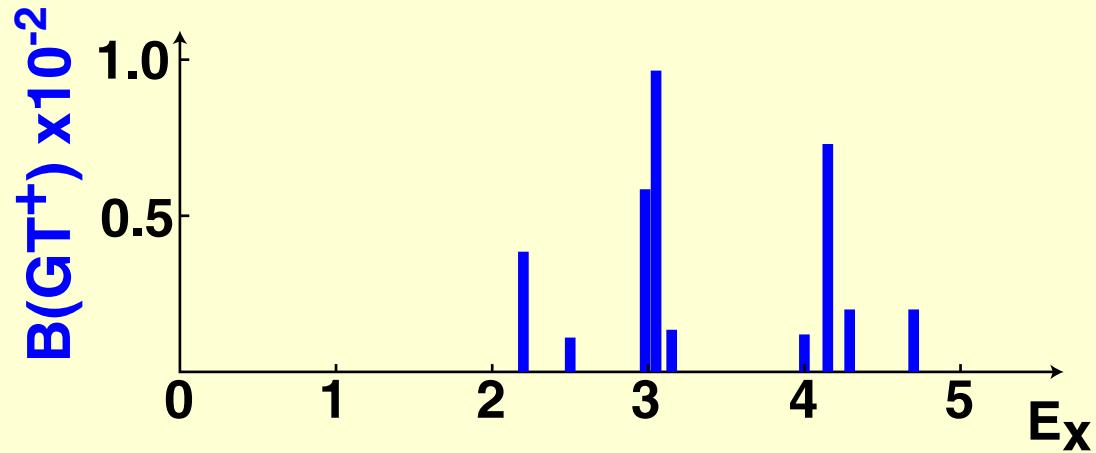
$$\begin{aligned} \frac{Q}{T_{1/2}} &= 4.27 \text{ MeV} \\ T_{1/2} &= 4.3 \times 10^{19} \text{ yr} \end{aligned}$$

$^{116}\text{Cd}$

$$\begin{aligned} \frac{Q}{T_{1/2}} &= 2.80 \text{ MeV} \\ T_{1/2} &= 3.8 \times 10^{19} \text{ yr} \end{aligned}$$

NUCLEAR STRUCTURE





## Experimental matrix elements

$$M_{DGT} = \sum_m m M_{DGT} / E_m$$

$$= 0.0726 \pm 0.0155$$
all positive

$\downarrow$

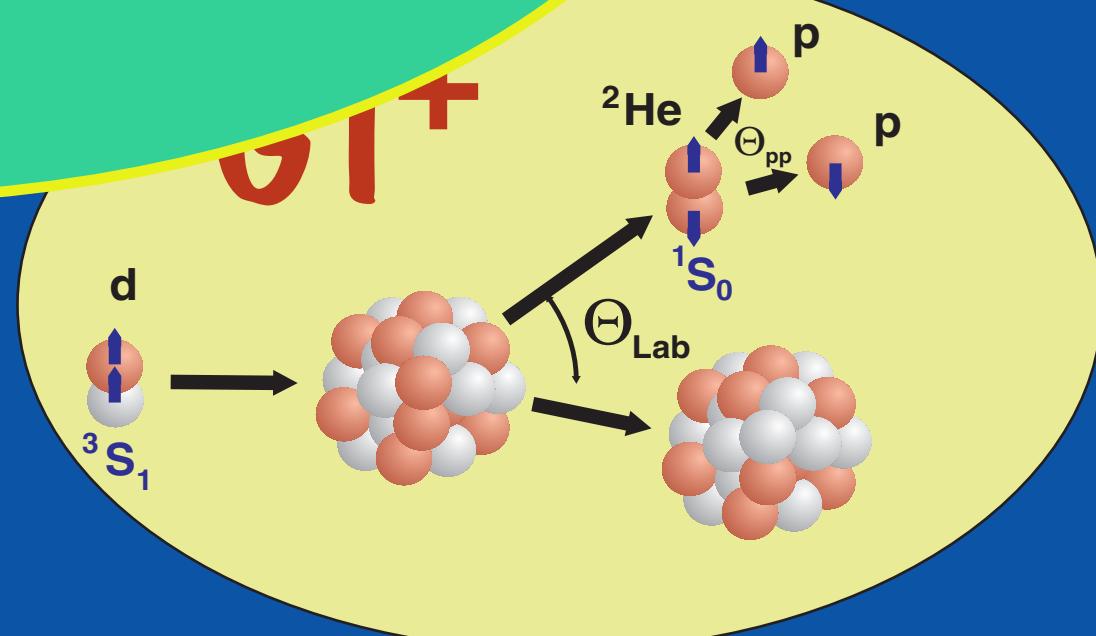
$$T_{1/2} = (1.72 \pm 0.73) \times 10^{19} \text{ yr}$$

Compare to counting exp't:

$$T_{1/2} = (4.3 \pm 2.5) \times 10^{19} \text{ yr}$$

DF

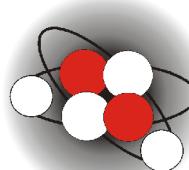
# Halo nuclei



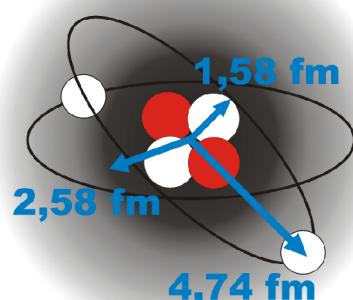
# Halo nuclei

$^7\text{He}$

reduced  
spin-orbit force?  
low-lying  
 $p_{1/2}$   
spin-orbit partner  
at  $\sim 600$  keV?  
continuum structure

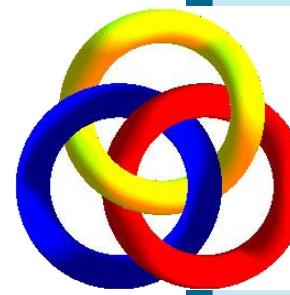


skin  
or  
halo?

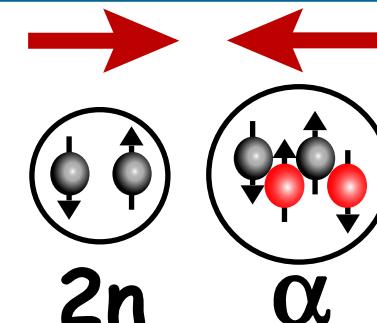


$^6\text{He}$

Borromean  
structure



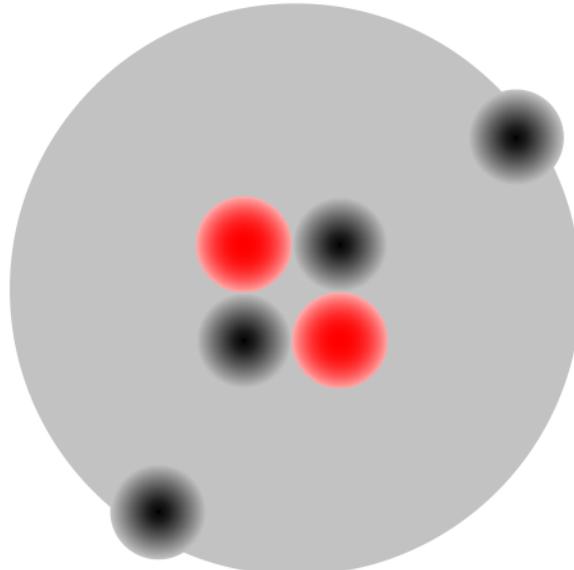
reduced  
spin-orbit force ?



$^6\text{Li}(\text{d}, 2\text{He})^6\text{He}$   
 $^7\text{Li}(\text{d}, 2\text{He})^7\text{He}$

Soft dipole resonance ?

# $^6\text{He}$ - prototype of a halo-nucleus



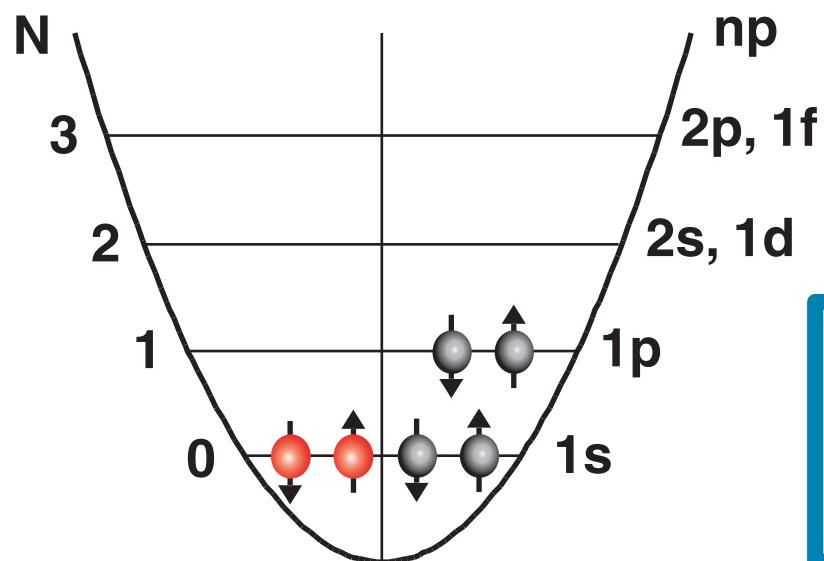
**3-body  $\alpha+n+n$  structure  
("Borromean system")**

**3-body calculations\*:**

- narrow  $0^+, 2^+$  states (g.s.,  $\sim 1.6$  MeV)
- $2^+$  "soft mode" state at 4.3 MeV;  $\Gamma=1.2$  MeV
- $1^+$  resonance at 4.5 MeV
- $0^+$  resonance at 5 MeV
- no conclusions about "soft dipole" modes (at low energies).

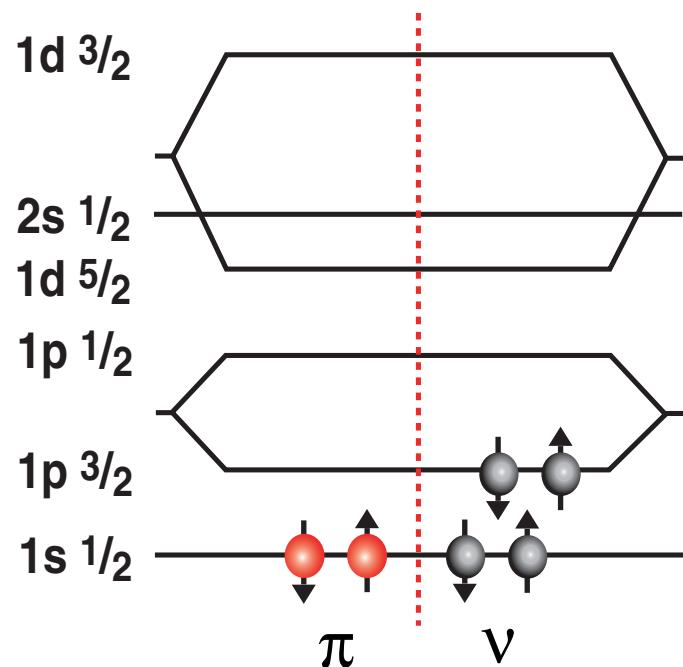
\*B.V. Danilin et al., PRC 55, 577 (1997)

easily reachable thru  $^6\text{Li} (d, ^2\text{He}) ^6\text{He}$   
resolution 120 keV  
angular distributions



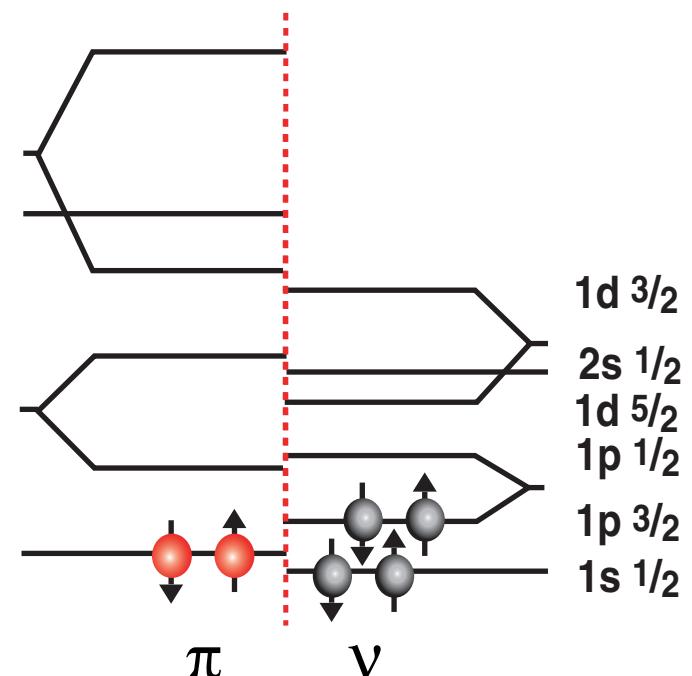
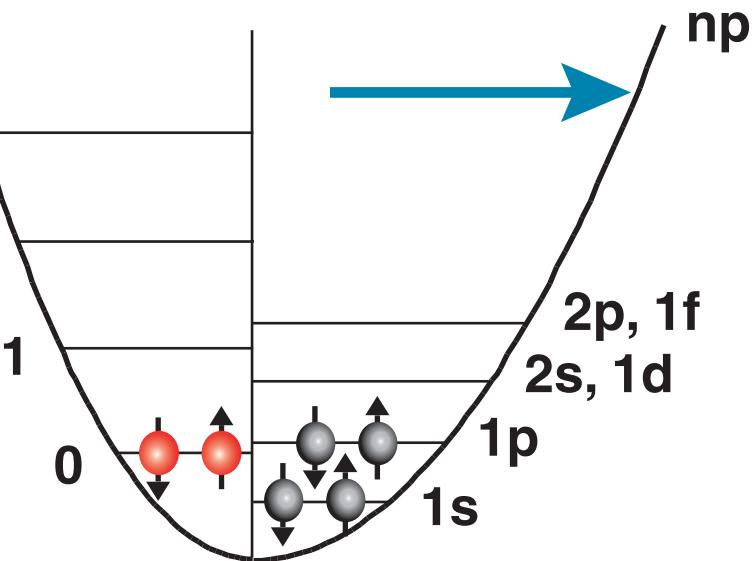
## harmonic oscillator

$$V(r) = \frac{1}{2} m \omega^2 r^2$$
$$E = \left(N + \frac{3}{2}\right) \hbar \omega$$



## spin-orbit potential

$$V_s(r) = V_{0s} \frac{1}{r} \frac{d}{dr} f(r)$$
$$f(r) = \frac{1}{1 + \exp[(r-R)/a]}$$

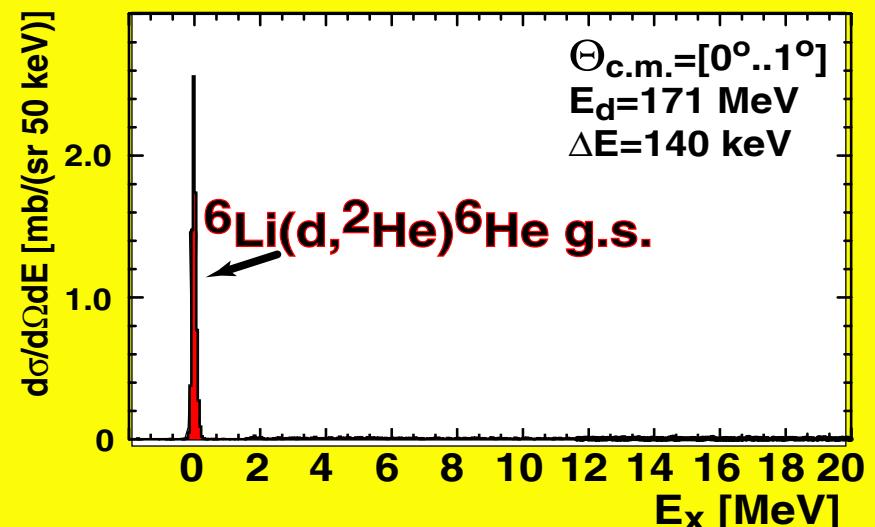
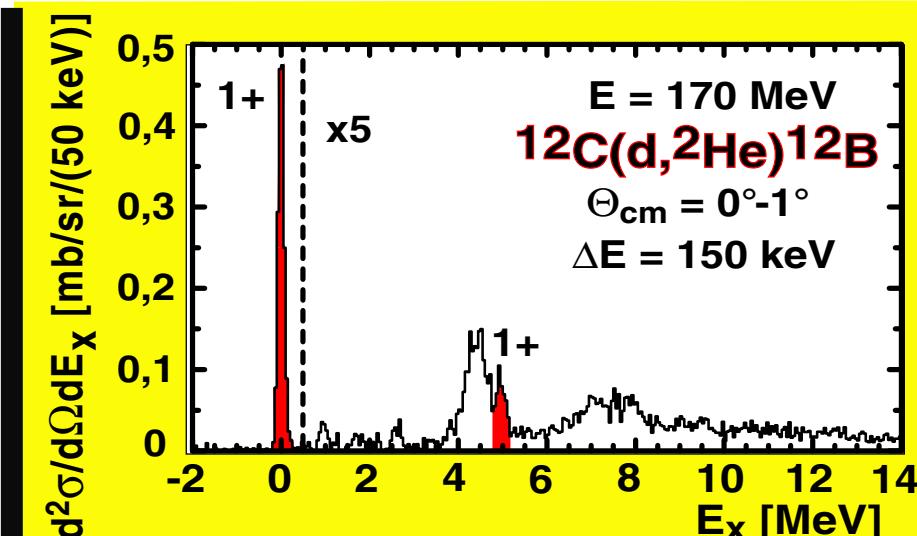
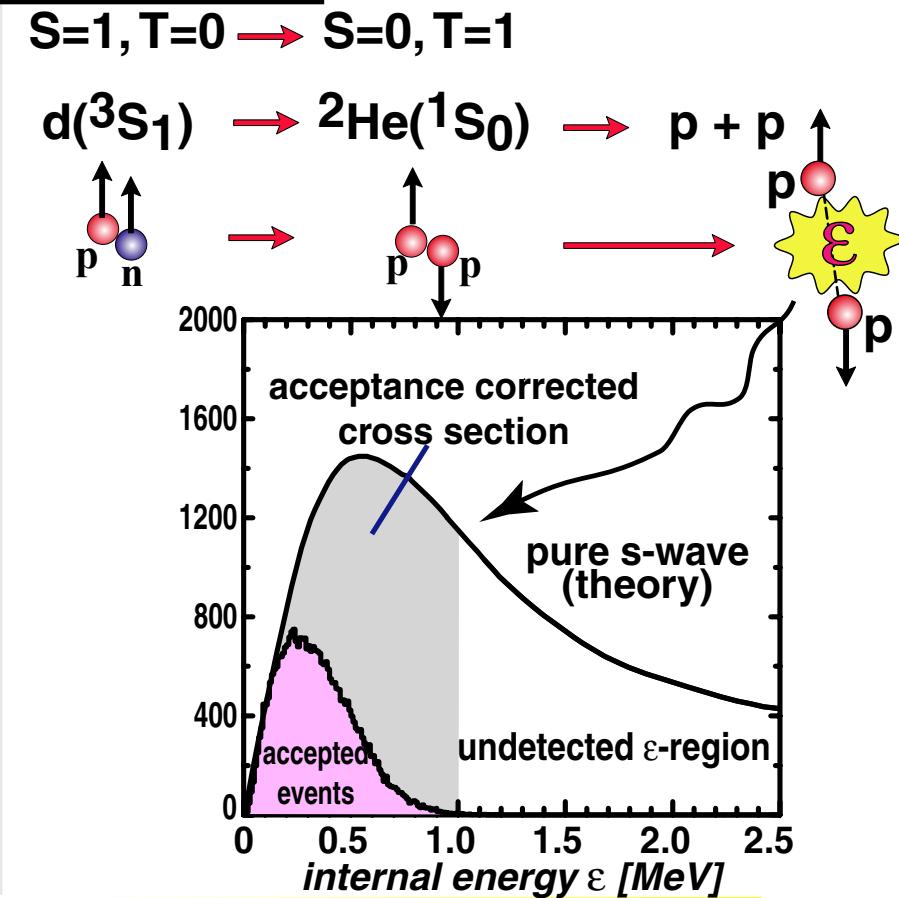


# The ( $d, {}^2\text{He}$ ) reaction

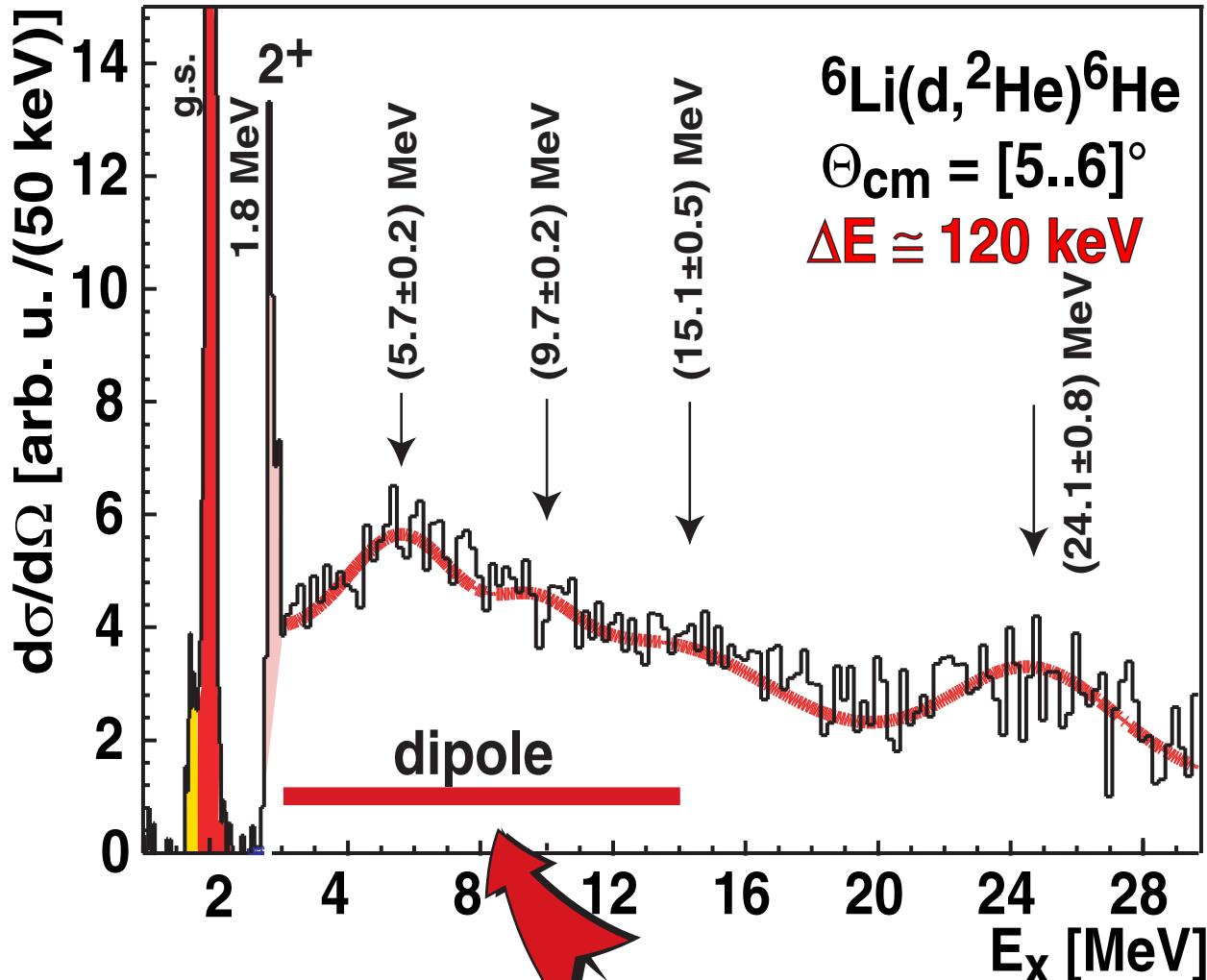
- 1)- reaction mechanism forces a spin-flip and an isospin-flip !  
 $\Delta S=1, \Delta T=1$  perfect GT filter
- 2)- coincident detection of two protons from  ${}^2\text{He}$  decay  
 → background-free spectra but need large accptnc spectrometer
- 3)- contributions from higher p-p partial waves? Dont' worry!!

## Alternatives:

- (n,p) resolution?? Fermi transition  
 (t, ${}^3\text{He}$ ) triton beam?? Fermi transition  
 (HI,HI) resolution?? reaction mechanism??



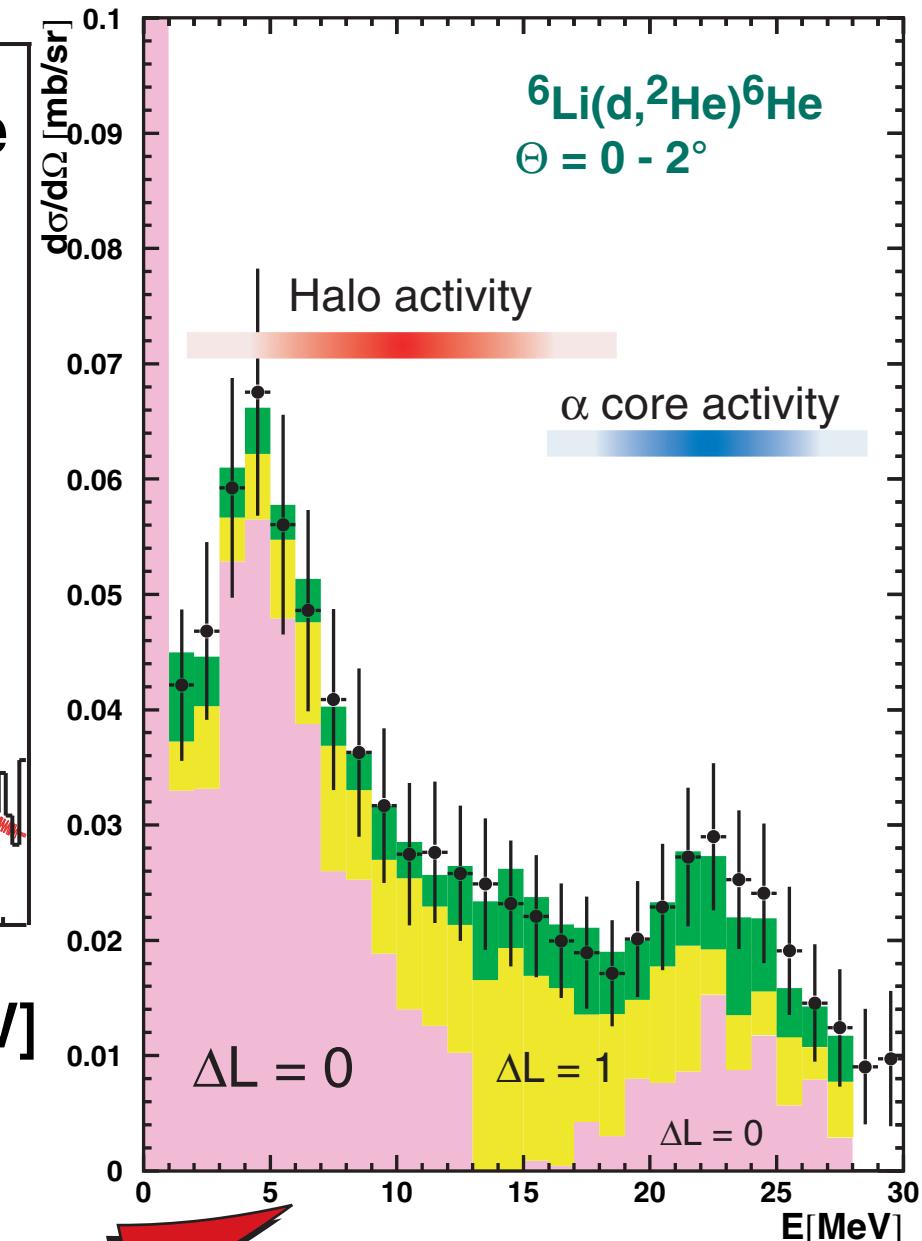
# ${}^6\text{Li}(\text{d}, {}^2\text{He}) {}^6\text{He}$



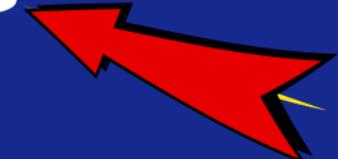
some low-lying dipole strength  
(soft dipole ??)



${}^6\text{Li}(\text{d}, {}^2\text{He}) {}^6\text{He}$   
 $\Theta_{\text{cm}} = [5..6]^\circ$   
 $\Delta E \approx 120 \text{ keV}$



# Spin-orbit splitting halo nucleus $^7\text{He}$



Origin and strength of spin-orbit force?

- p- and sd-shell nuclei:  $V_{\text{s.o.}} \sim 5\text{-}6 \text{ MeV}$
- halo nuclei: reduction of s.o. interaction because of large radial extent?

Theoretical predictions for  $^7\text{He}$  s.o. splitting:

large scale shell models  
Resonating Group Methods } 2 - 3 MeV

Quantum Monte Carlo ~ 1 MeV

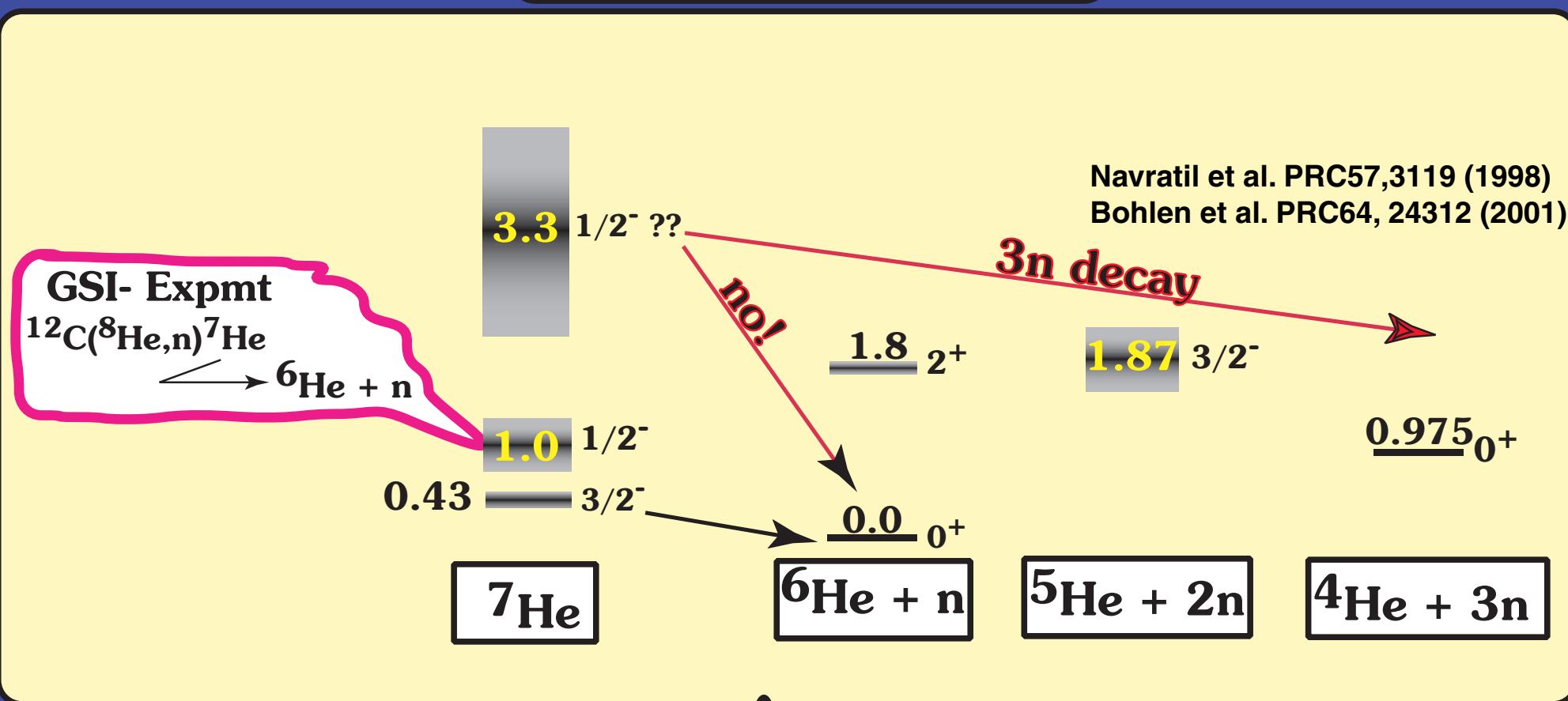
$^7\text{He}$  g.s. :  $J^\pi = 3/2^-$   
 $^7\text{He}$  s.o. :  $J^\pi = 1/2^-$   
partner

Experimental situation for  $^7\text{He}$  states above g.s.

Reaction	Ex [MeV]	$\Gamma$ [MeV]	method
$^{12}\text{C}(^8\text{He}, n)^7\text{He}$	0.6	0.75	inv. mass
$^1\text{H}(^8\text{He}, d)^7\text{He}$	2.9	2.2	miss. mass
$^9\text{Be}(^{15}\text{N}, ^{17}\text{F})^7\text{He}$	2.95	1.9	miss. mass
$^{10}\text{B}(\pi^-, pd)^7\text{He}$	2.8	2.0	miss. mass
$^7\text{Li}(n, p)$	~6, 20.0	? , 9.0	charge-ex.

claimed by recent  
GSI expmt !

# The A = 7 system



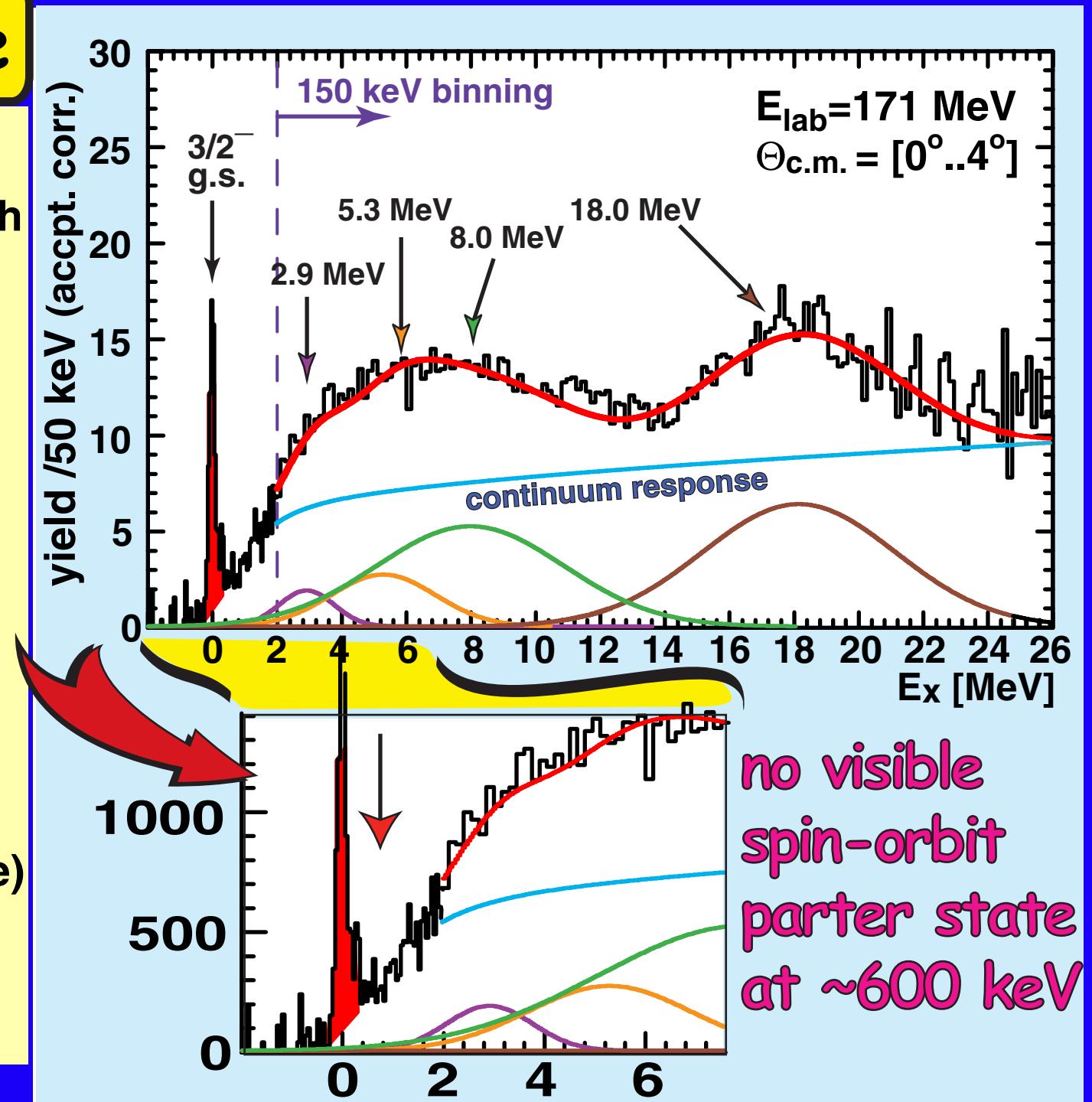
$^{7}\text{He}$  (0.43, g.s.):  $\Gamma = 160$  keV  
 $^{7}\text{He}$  (1.0):  $\Gamma = 750$  keV  
 $^{7}\text{He}$  (3.3): broad



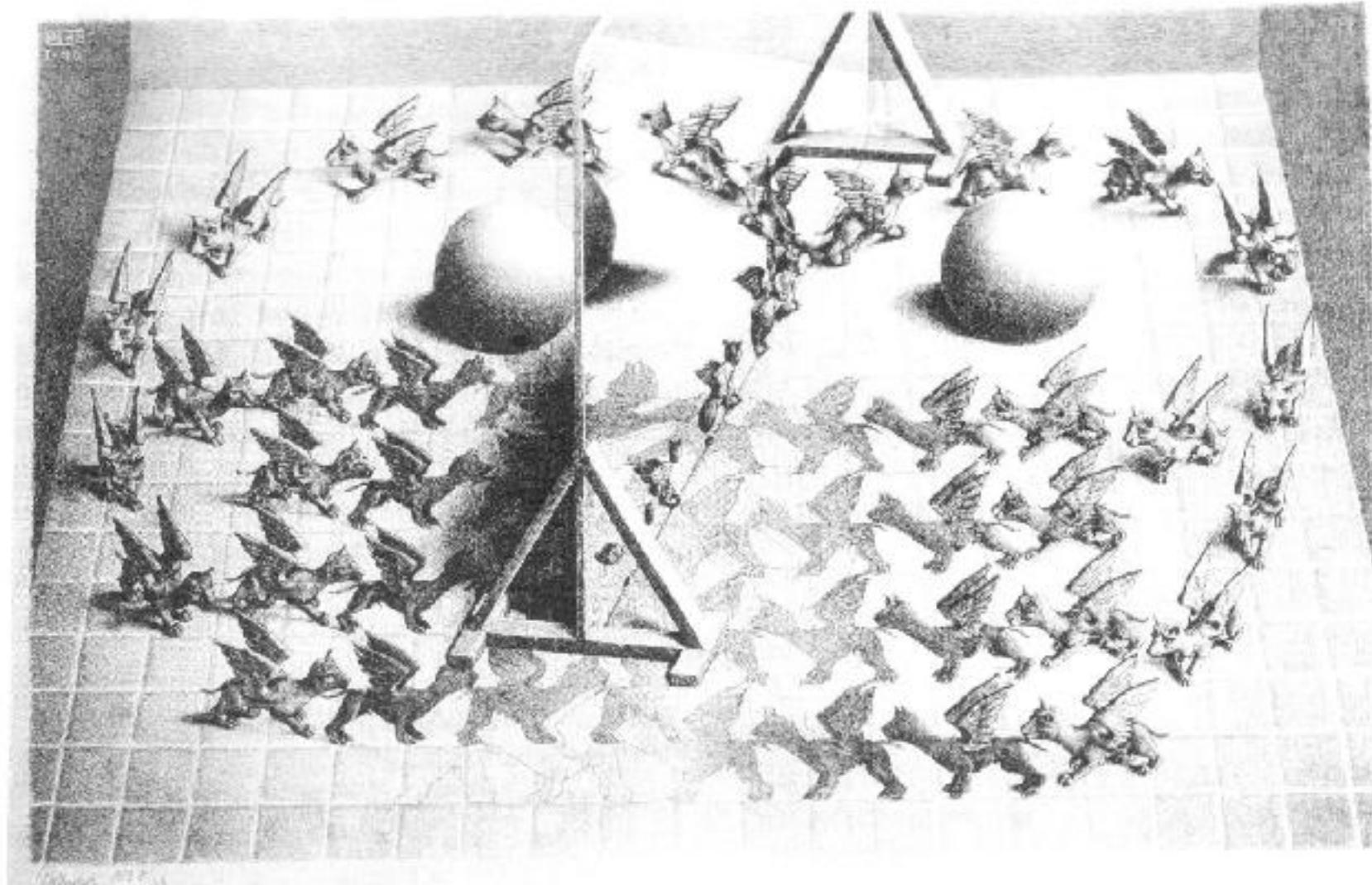
$^{7}\text{Li} (\text{d}, \text{He})^{7}\text{He}$   
 exploit **GT-tool** !!!

# $^7\text{Li}(\text{d}, 2\text{He})^7\text{He}$

- unexpectedly weak GT-transition strength ( $^7\text{Li} = \alpha + \text{t}$ )
- strong reduction of spin-orbit force not observed
- although favoured by GT-operator, no low-lying spin-orbit partner visible
- several broad states observed at:  
2.9 MeV (seen before)  
5.3 MeV  
8.0 MeV  
18.0 MeV (strong!!)



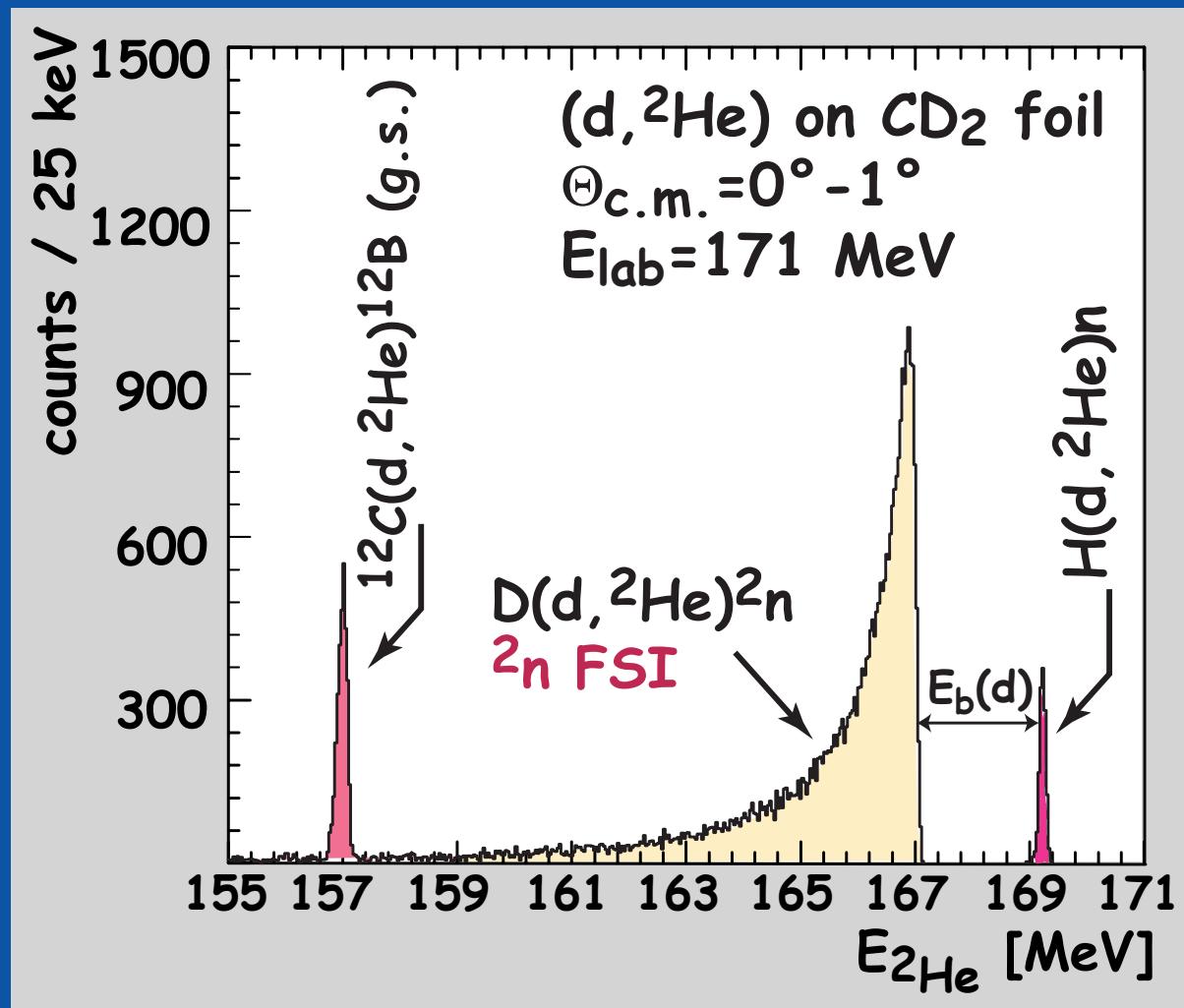
# Charge Symmetry Breaking



M.C. Escher

# Measurement of nn-scattering length $a_{nn}$ thru $D(d, {}^2\text{He}){}^2\text{n}$

Spectroscopy of n-n FSI thru  $(d, {}^2\text{He})$  on  $\text{CD}_2$  foil at  $\Theta_{\text{BBS}}=0^\circ$



## idea:

- GT operator populates  ${}^2\text{n}$  in  ${}^1\text{S}_0$  state
- $a_{nn}$  determined by shape of GT strength function

## data:

- $\Delta E = 115 \text{ keV}$  [FWHM]
- check energy calibration with  ${}^1\text{H}$  and  ${}^{12}\text{C}$  target components

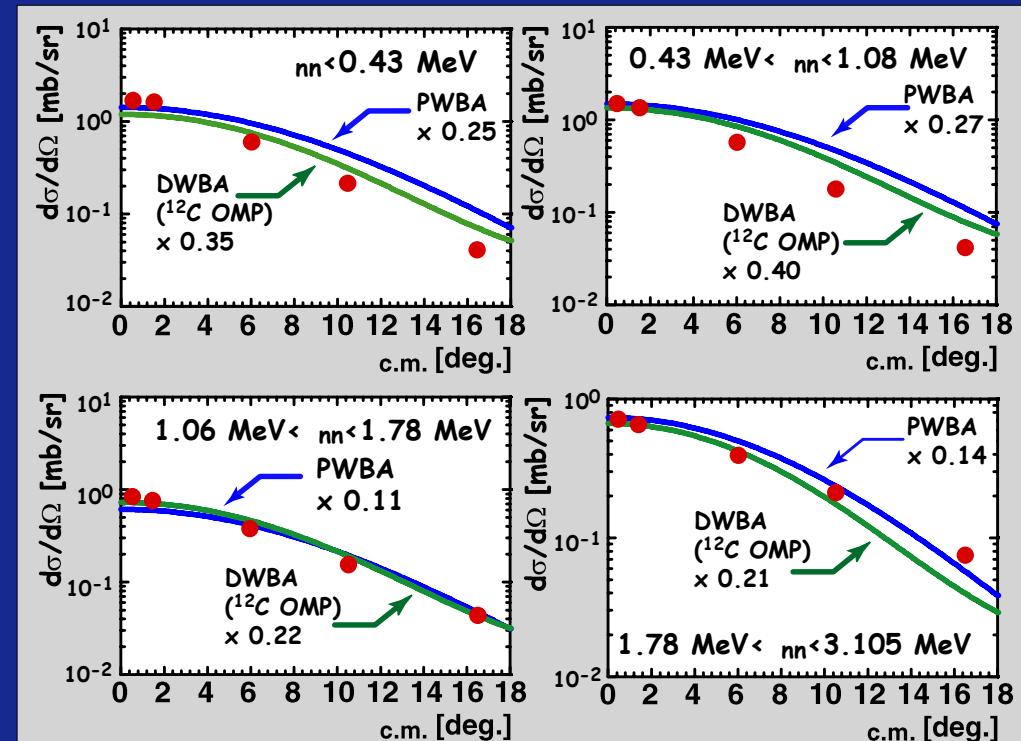
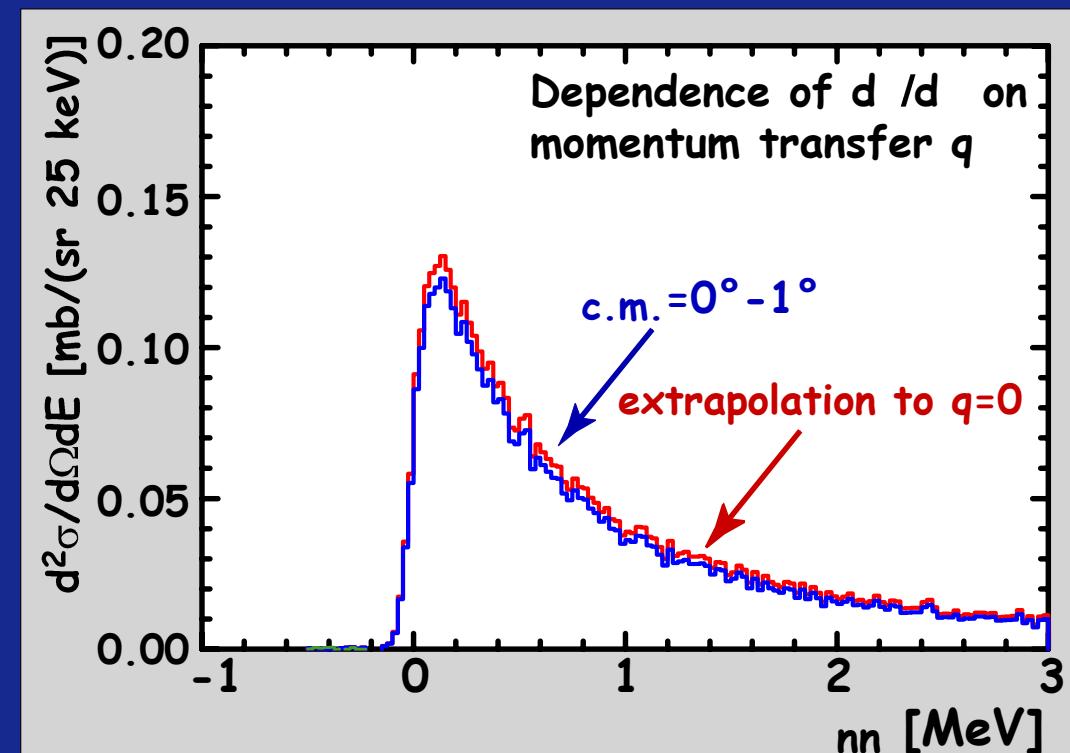
# Momentum dependence of $D(d, {}^2\text{He})^2\text{n}$ : extrapolation to momentum transfer $q=0$

Experimental data at c.m. =  $[0^\circ - 1^\circ]$  and  $nn < 9 \text{ MeV}$  correspond to momentum transfers  $q$ :  $0.05 \text{ fm}^{-1} < q < 0.18 \text{ fm}^{-1}$

Apply transformation

$$\frac{d}{d} (q=0) = \frac{\text{DWBA}(q=0)}{\text{DWBA}(q)} \frac{d}{d} \text{exp}(q)$$

Check  $q$ -dependence of  $d/d$  with angular distributions:  
data and DWBA-calculation

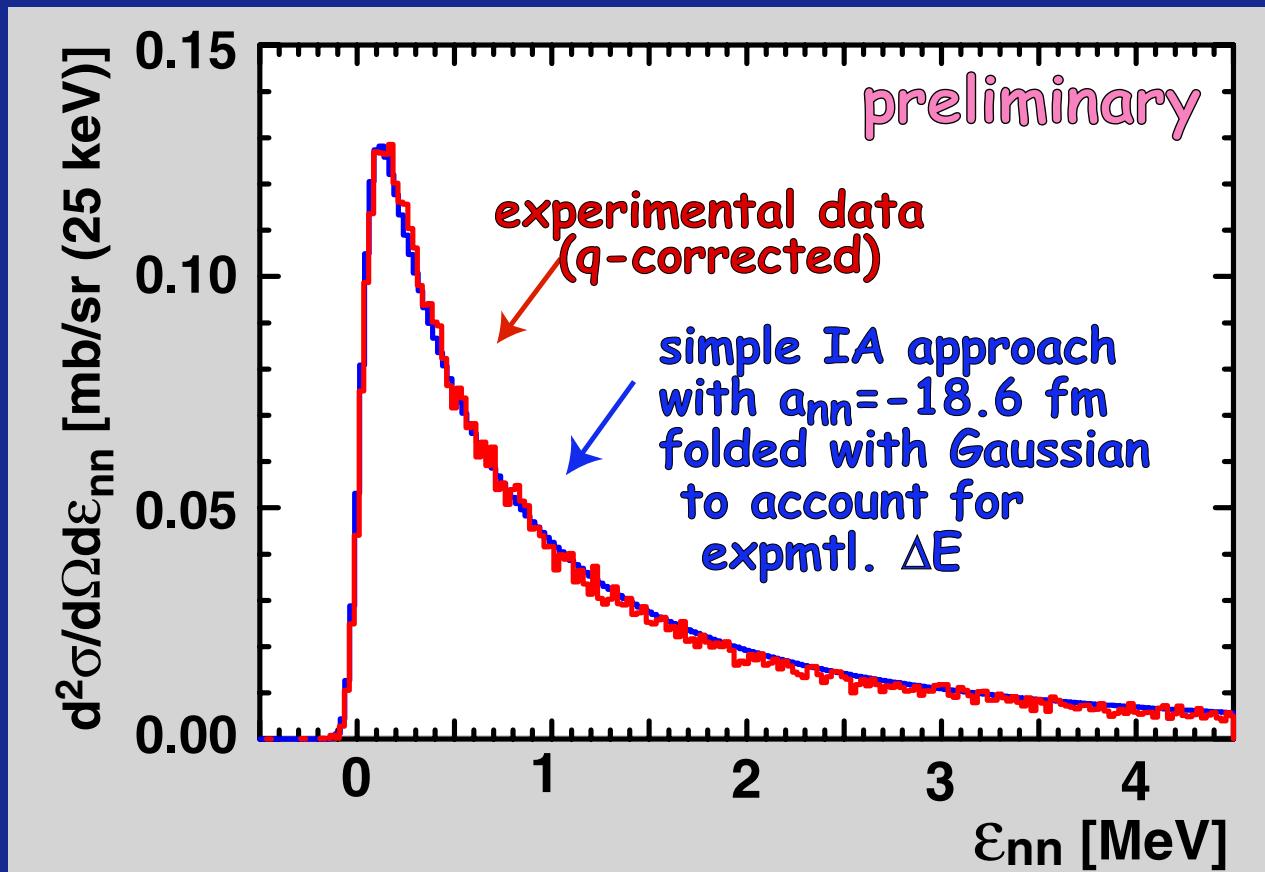


ann

## Impulse Approximation, leading order:

$$\frac{d\sigma}{d\Omega}(\epsilon_{pp}, \epsilon_{nn}) \sim \frac{k_f}{k_i} \sqrt{\epsilon_{pp} \epsilon_{nn}} |t_{\sigma\tau}|^2 B_{GT^-}(\epsilon_{pp}, d \rightarrow {}^2He) B_{GT^+}(\epsilon_{nn}, d \rightarrow {}^2n)$$

$$B_{GT}(\epsilon_{NN}) = \frac{1}{3} |\langle NN(\epsilon_{NN}, a_{NN}) || \sum_k \vec{\sigma}_k \tau_k || d \rangle|^2, N = n, p$$



Integrate over  $\epsilon_{pp}$ :

$$\frac{d\sigma}{d\Omega}[(d, {}^2He)] = \int_{0 \text{ MeV}}^{1 \text{ MeV}} d\epsilon_{pp} \frac{d^2\sigma}{d\Omega d\epsilon_{pp}}$$

Fitting procedure: fit only shape of spectrum

Result in agreement with recommended value

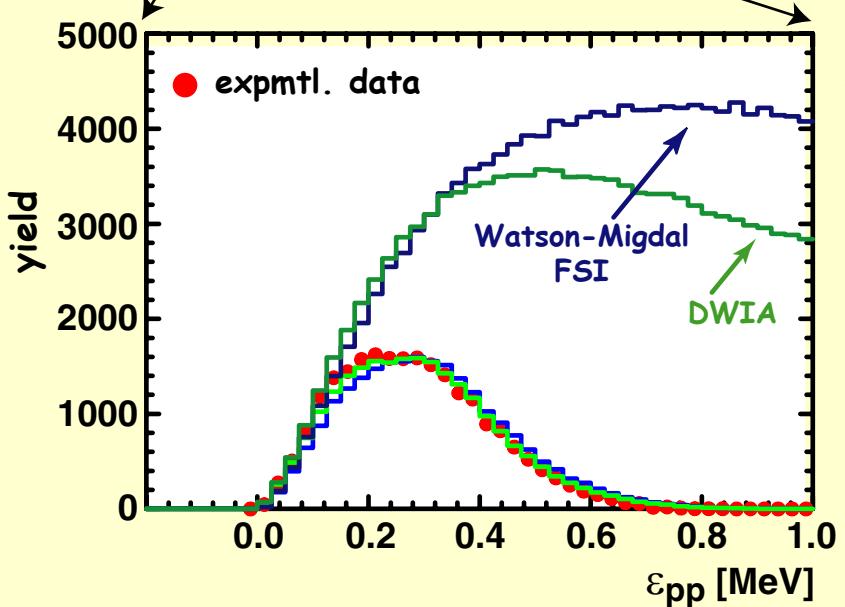
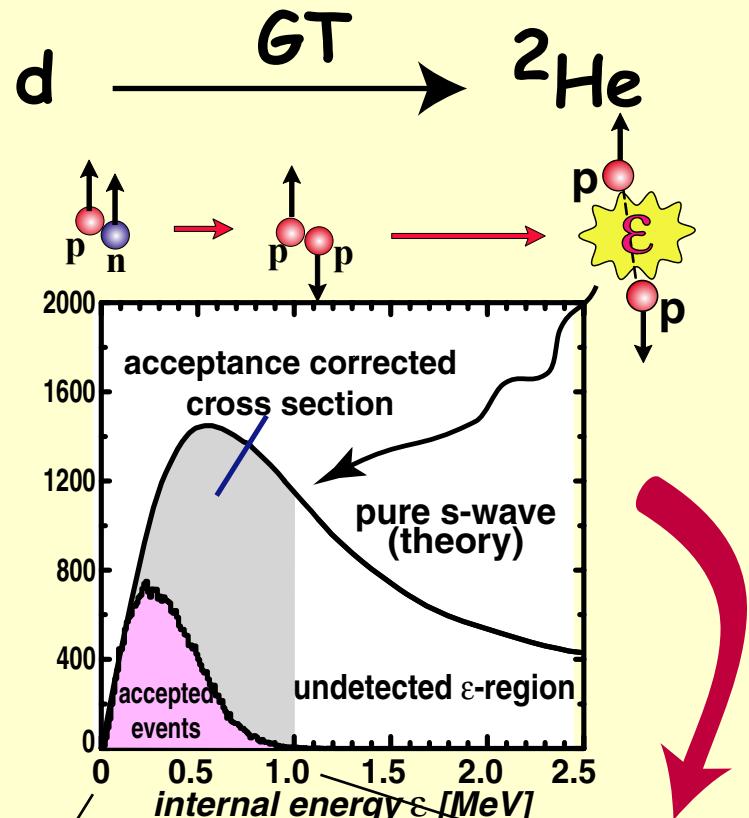
$a_{nn} = -18.6$  fm

# how to calibrate ( $d,^2\text{He}$ )

- detector and acceptance calibration
- cross section calibration
- does the cross section scale with  $B(\text{GT})$

$$\frac{d\sigma}{d\Omega} (q=0) = C \left[ \frac{\mu}{\pi \hbar} \right]^2 \frac{k_f}{k_i} N_D |V_{\sigma\tau}|^2 B(\text{GT}+)$$

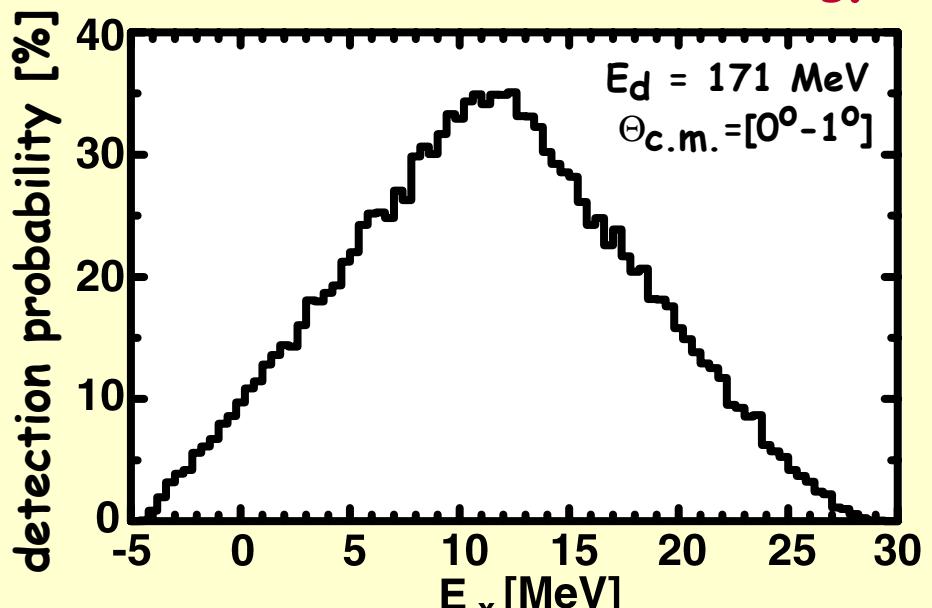




- 1) get a model for  $^1\text{S}_0$  of 2p-system
- 2) Monte-Carlo  $\varepsilon$ -acceptance for the  $\varepsilon$ -bin [0-1 MeV]
- 3) evaluate acceptance correction function for each excitation energy bin
- 4) calculate  $d\sigma/d\Omega = \int d\sigma/d\Omega(\varepsilon) d\varepsilon$

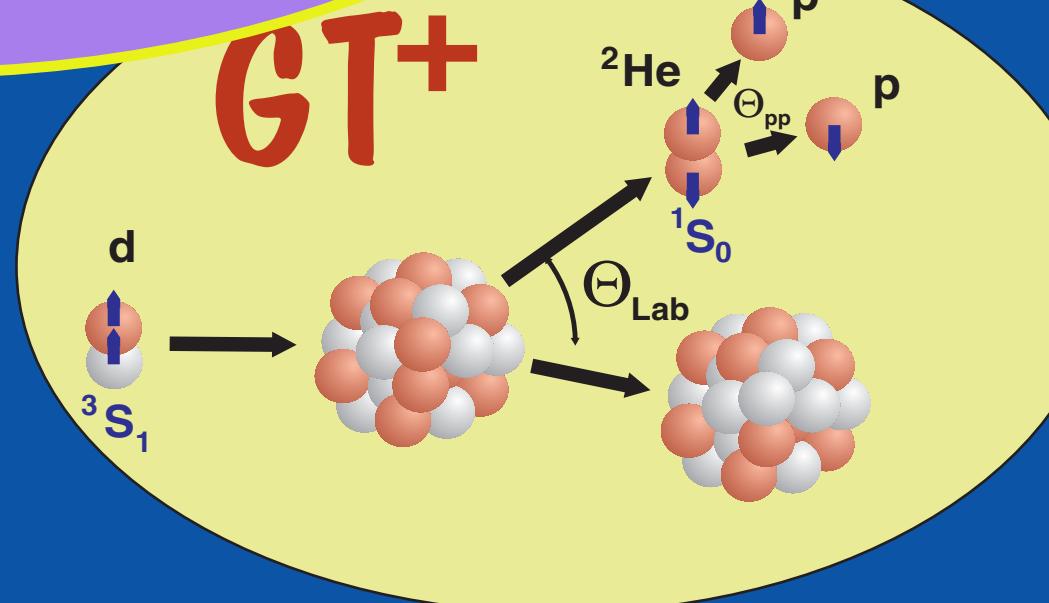
$$\int_{\varepsilon=0 \text{ MeV}}^{\varepsilon=1 \text{ MeV}} d\sigma/d\Omega(\varepsilon) d\varepsilon$$

Calculated 2-proton acceptance as a function of **excitation energy**



# Isospin symmetry

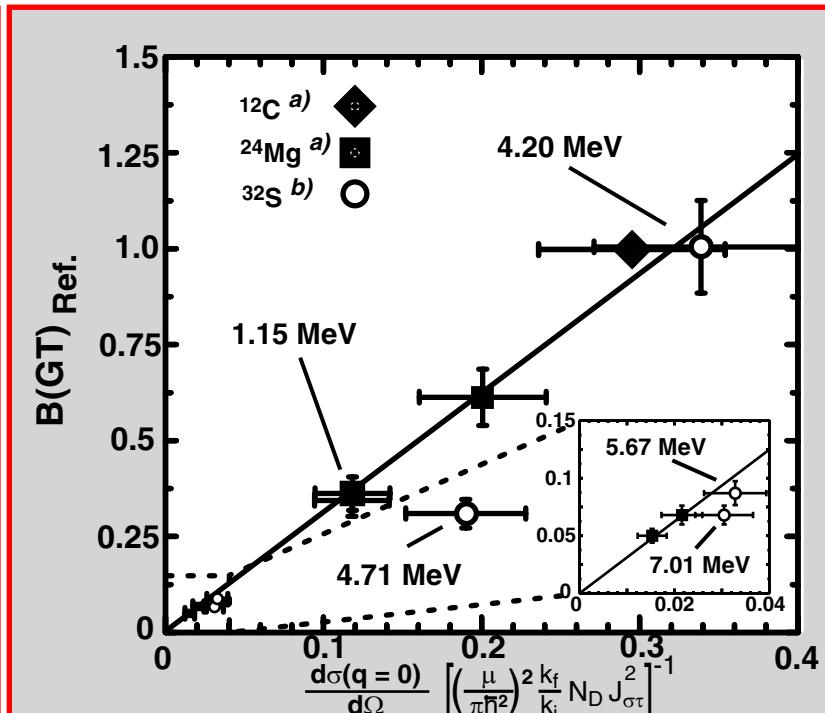
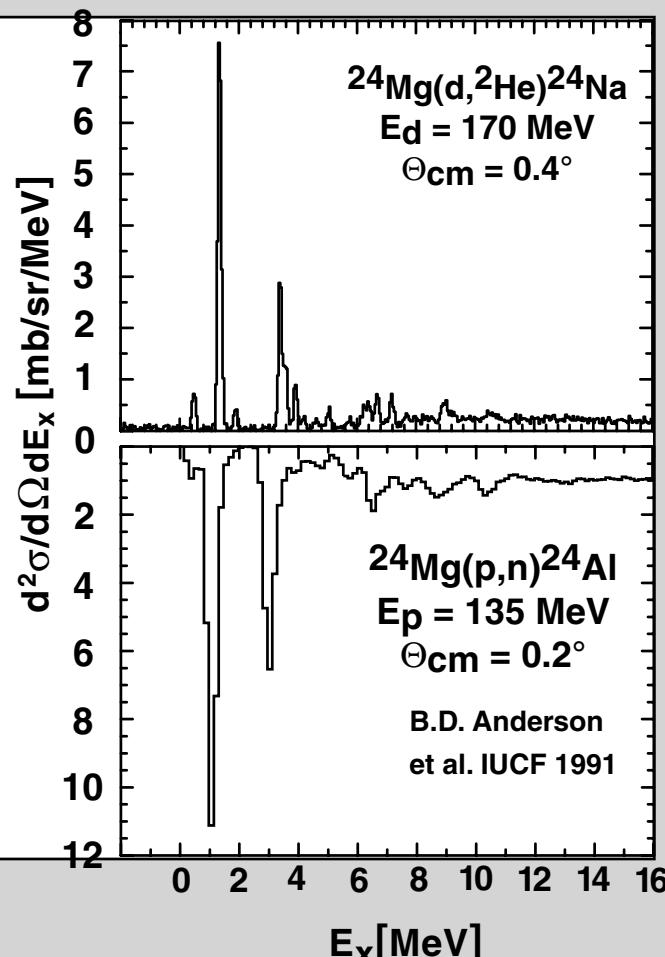
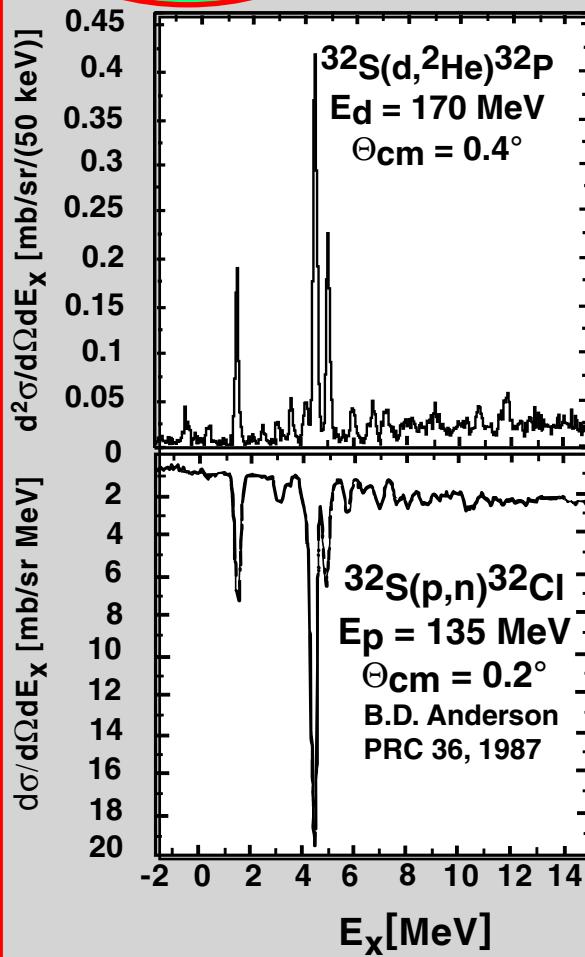
**GT<sup>+</sup>**



# (d, $^2\text{He}$ ) reaction & B(GT) extraction

(comparison with (p,n), (p,p'), (e,e') in N=Z nuclei)

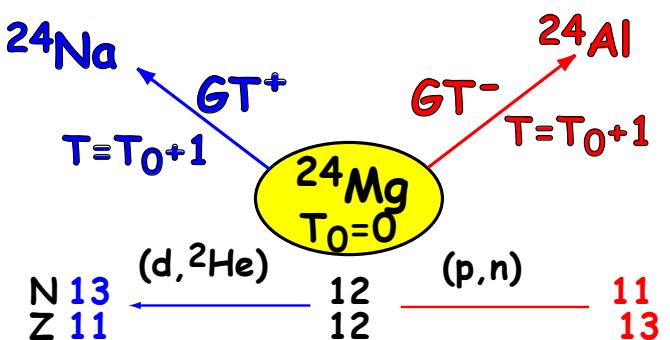
Isospin symmetry



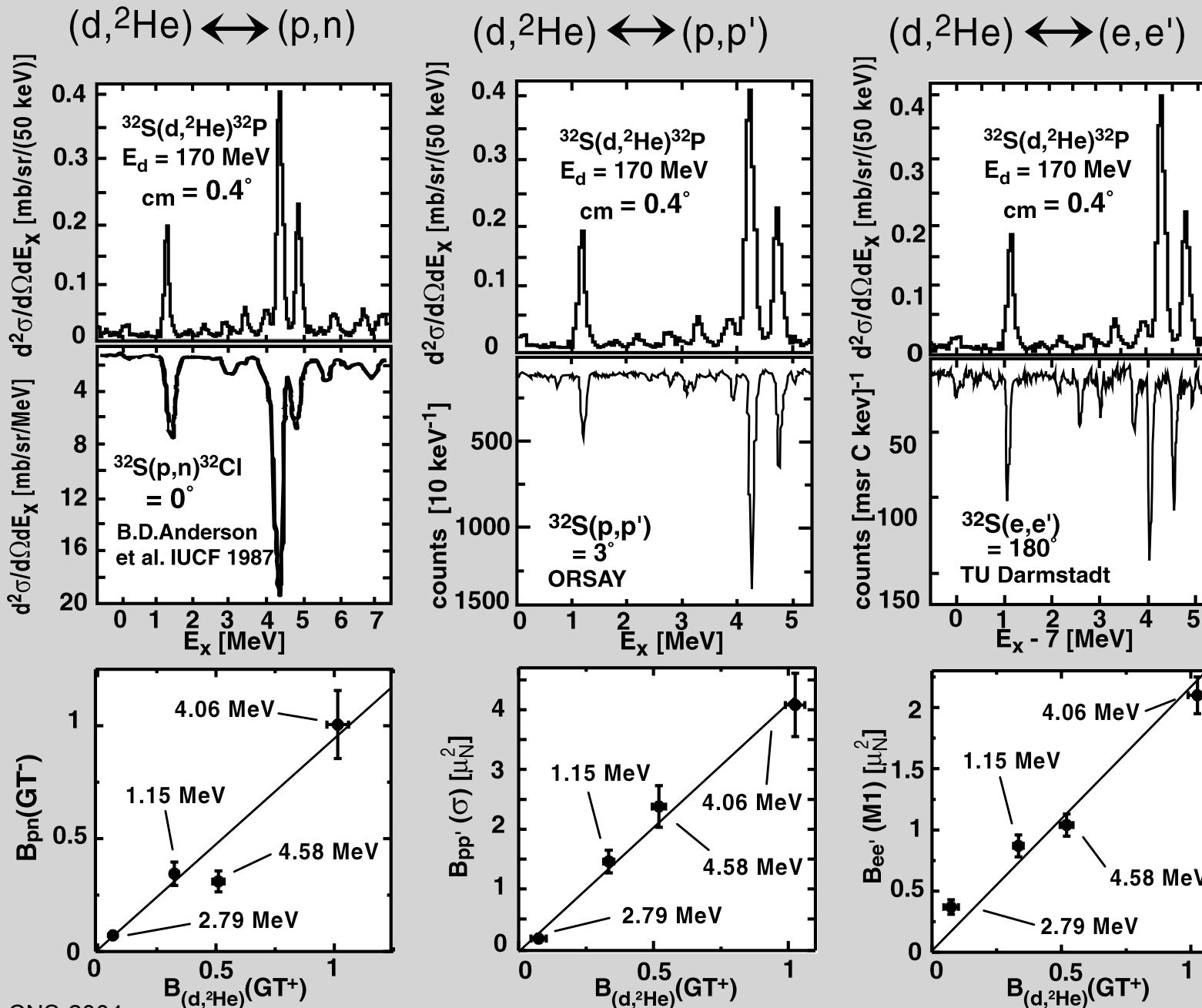
Isospin-symmetrie:

$$B(\text{GT}^+) = B(\text{GT}^-)$$

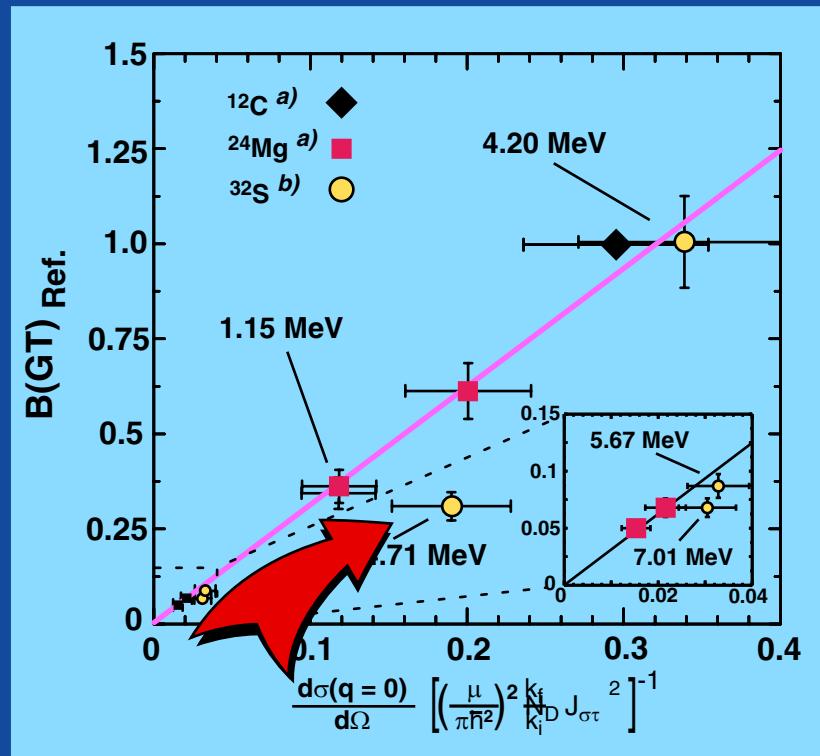
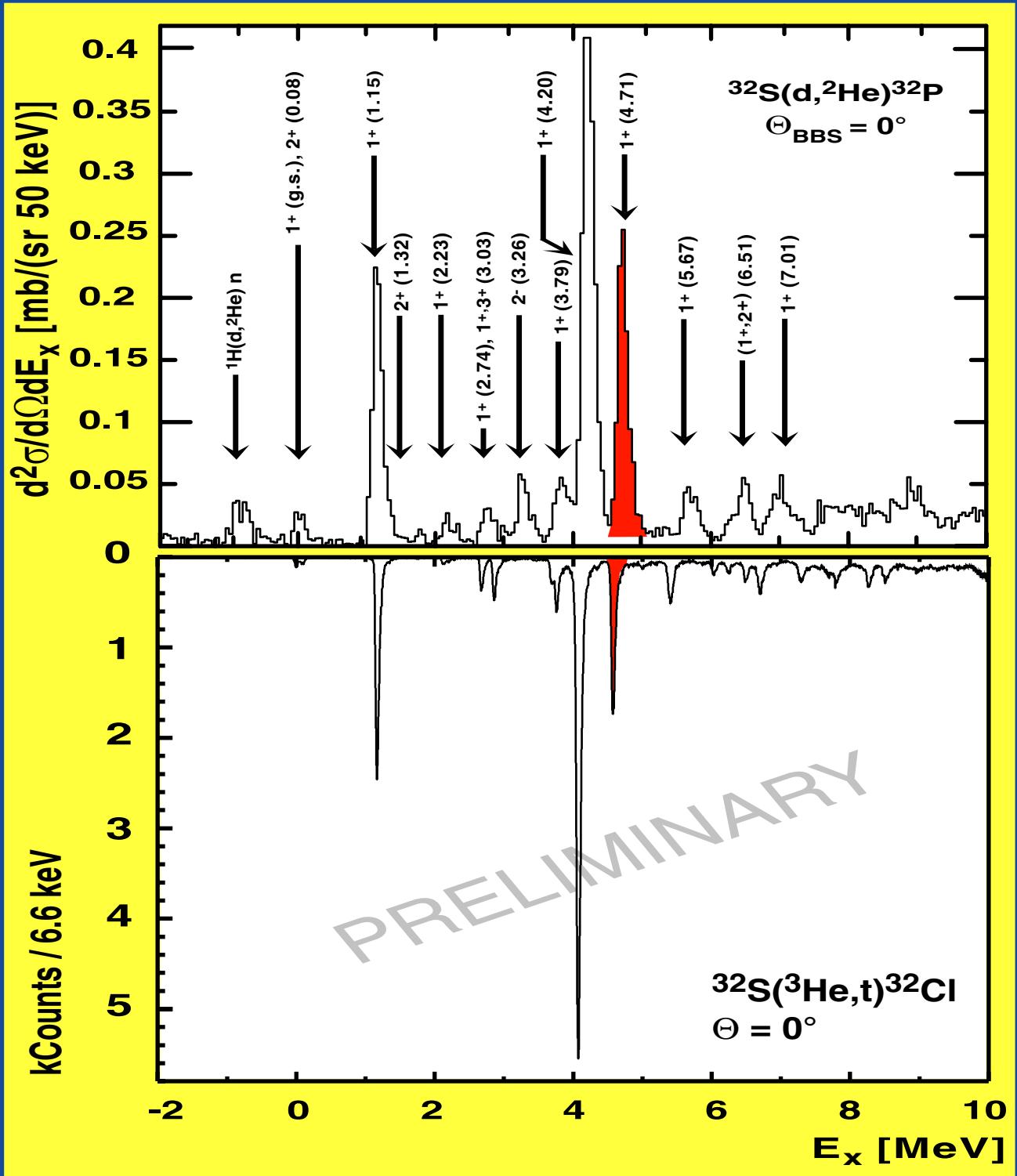
for N=Z nuclei



# B(GT<sup>+</sup>) from $^{32}\text{S}$ and analog transitions



# Isospin breaking in A=32 isobars



**Reason:**  
low proton threshold  
in  $^{32}\text{Cl}$  ?

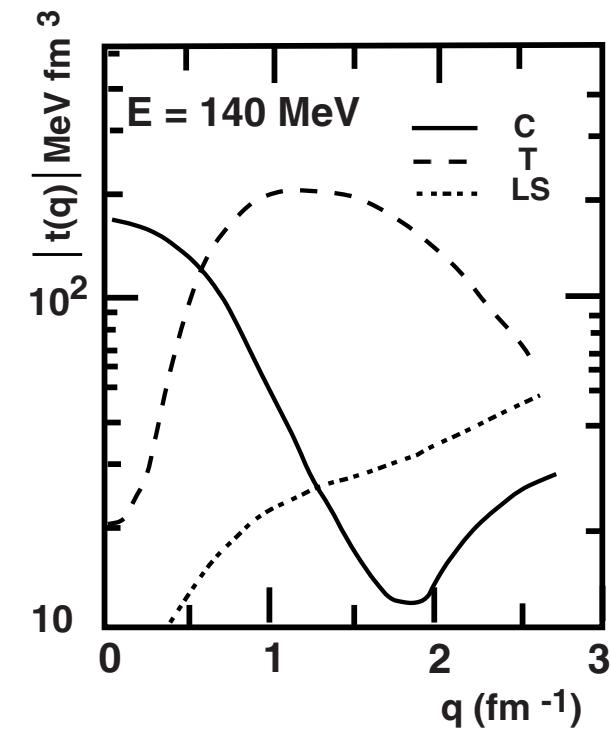
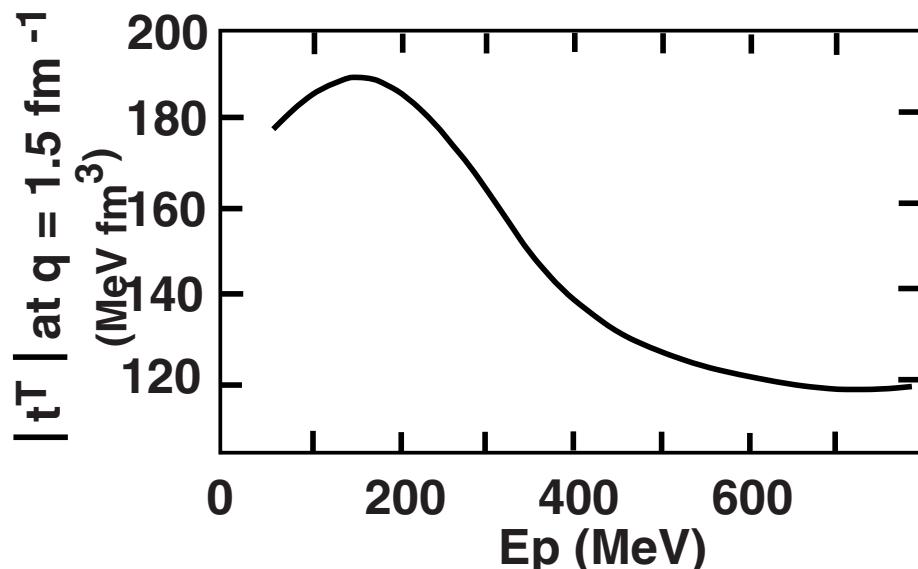
## Stretched states -- another case for ( $d, {}^2\text{He}$ ) ??

The reaction would have to be mediated by the tensor force ( analogue to ( $n, p$ ) )

Stretched states form factors  
peak at  $q_{\text{tr}} = L/R (> 1 \text{ fm}^{-1})$

BUT

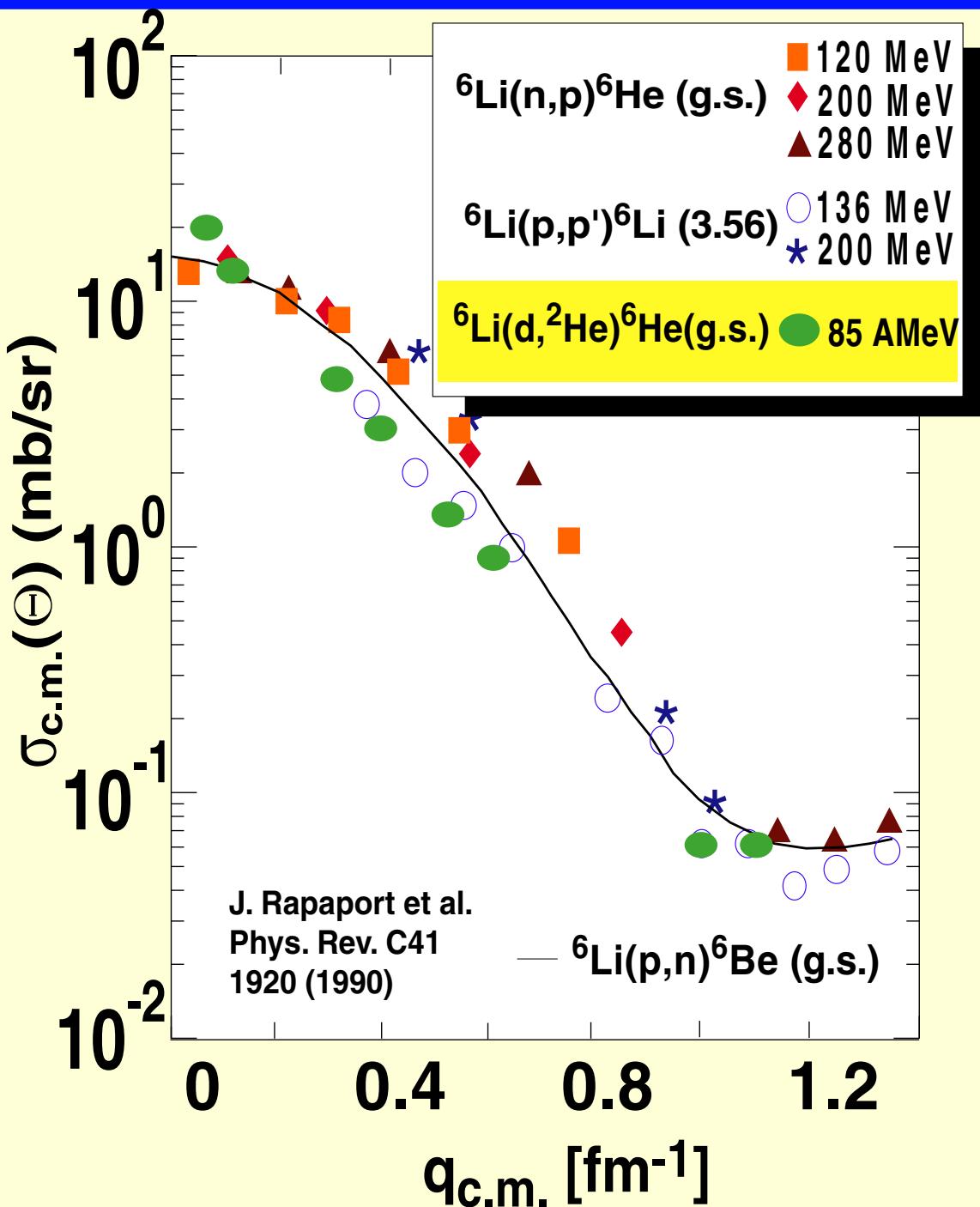
can  ${}^2\text{He}$  survive??



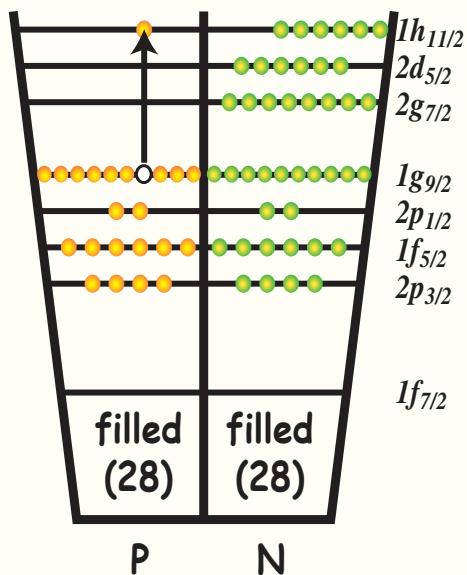
*q*-dependence of  
(d, 2He) reaction

or

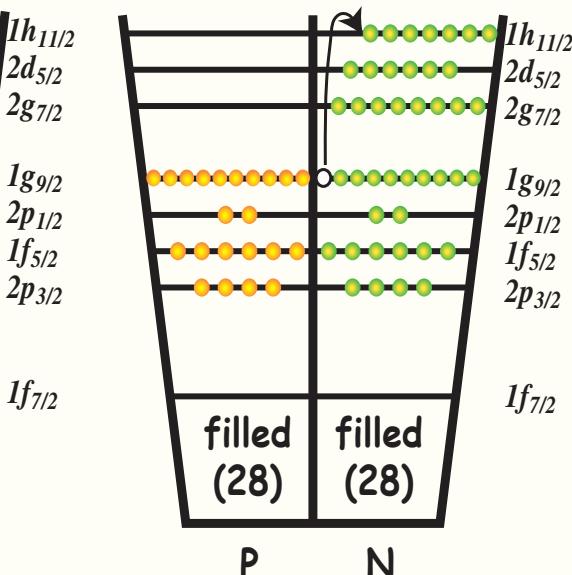
when does the  
2He fall apart?



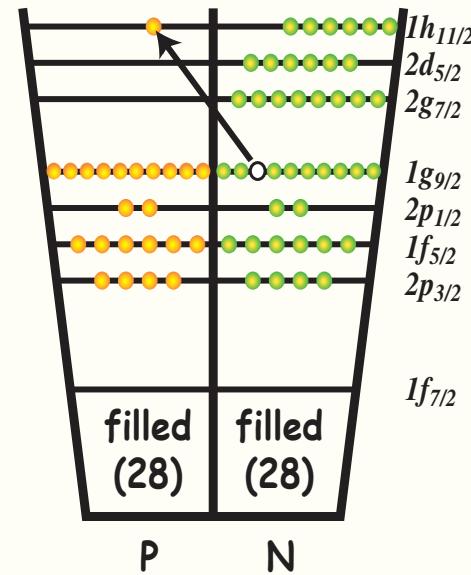
$$J^\pi = 10^- (\pi h_{11/2}, \pi g_{9/2}^{-1})$$



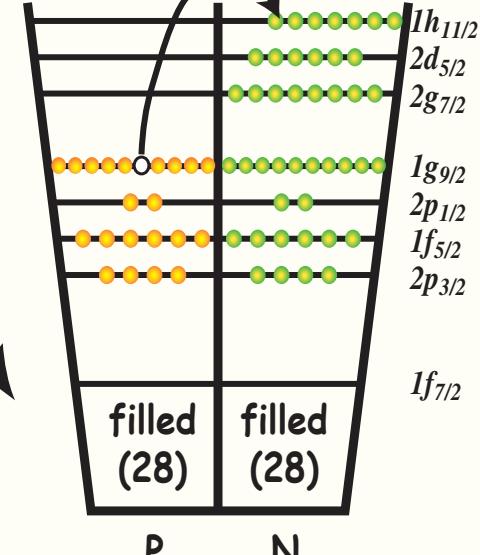
$$J^\pi = 10^- (\nu h_{11/2}, \nu g_{9/2}^{-1})$$



$$J^\pi = 10^- (\pi h_{11/2}, \nu g_{9/2}^{-1})$$



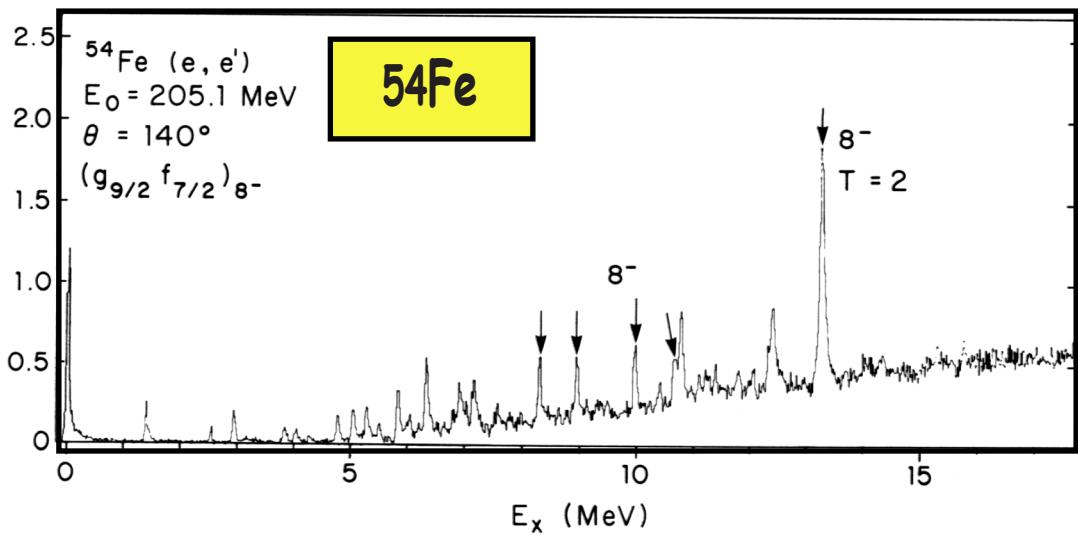
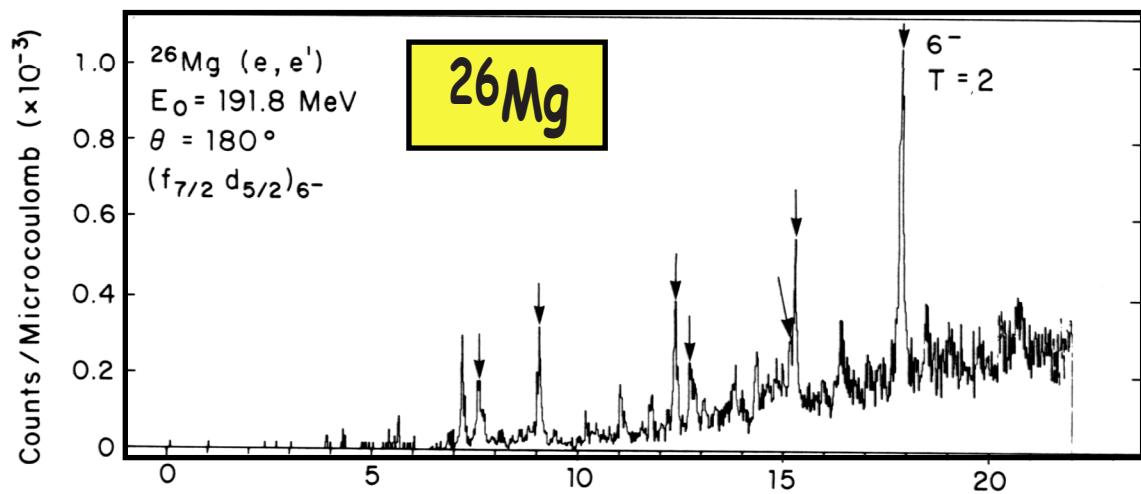
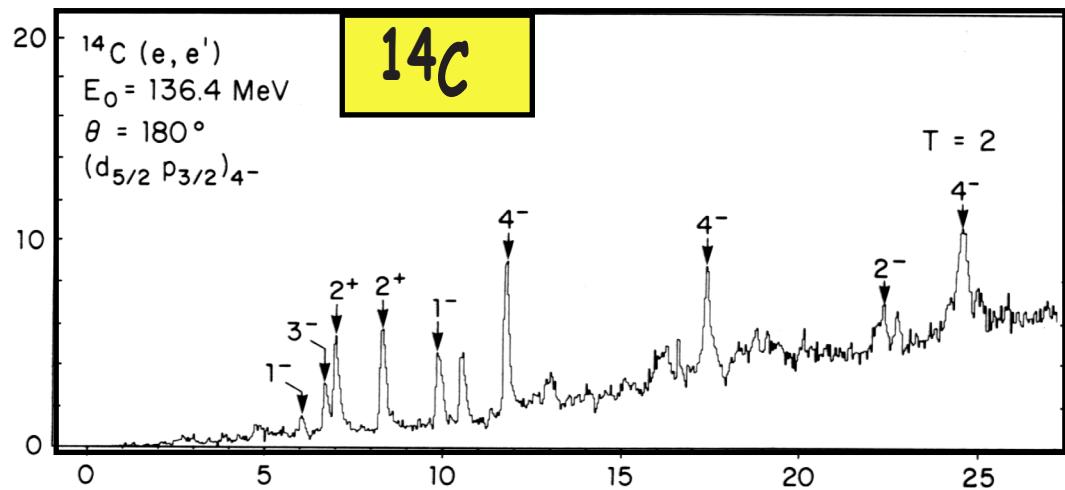
$$J^\pi = 10^- (\nu h_{11/2}, \pi g_{9/2}^{-1})$$

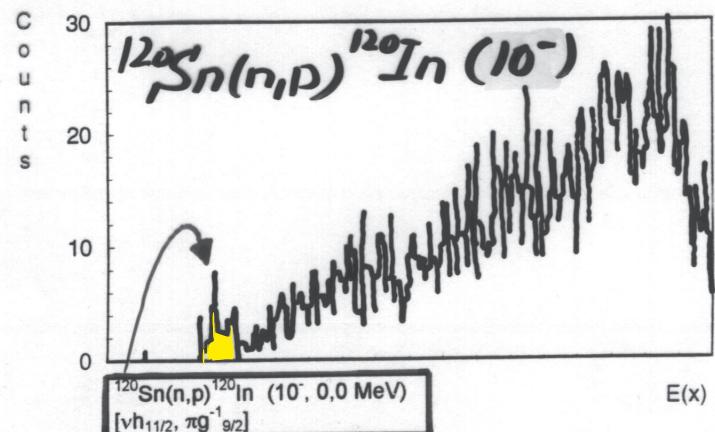
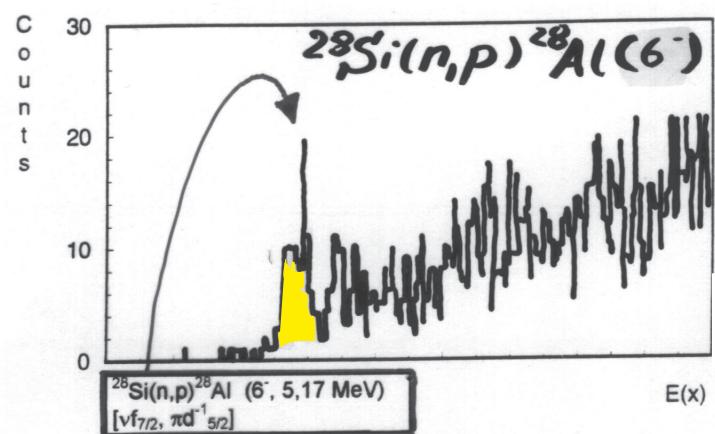
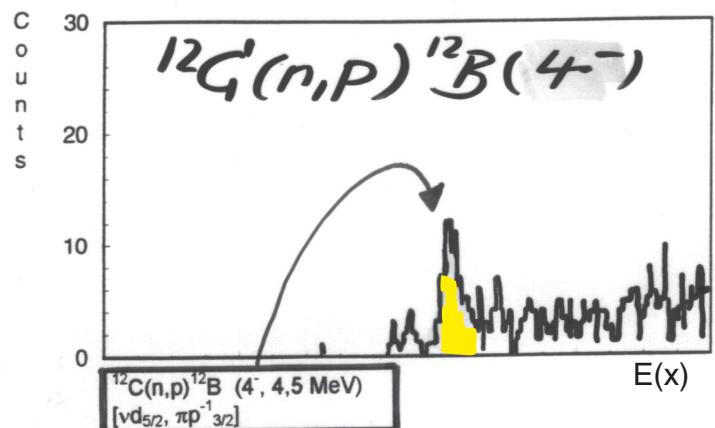


close to Fermi-surface

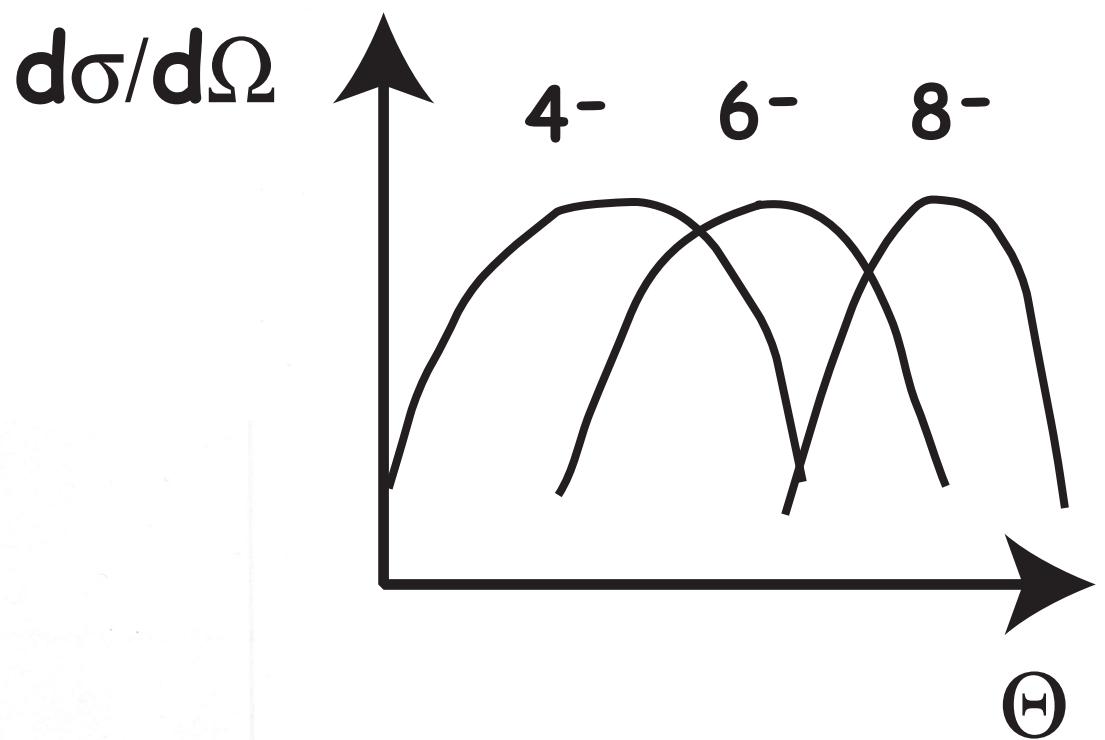
Fragmentation of stretched particle-hole states

# stretched states excitation through (e,e')





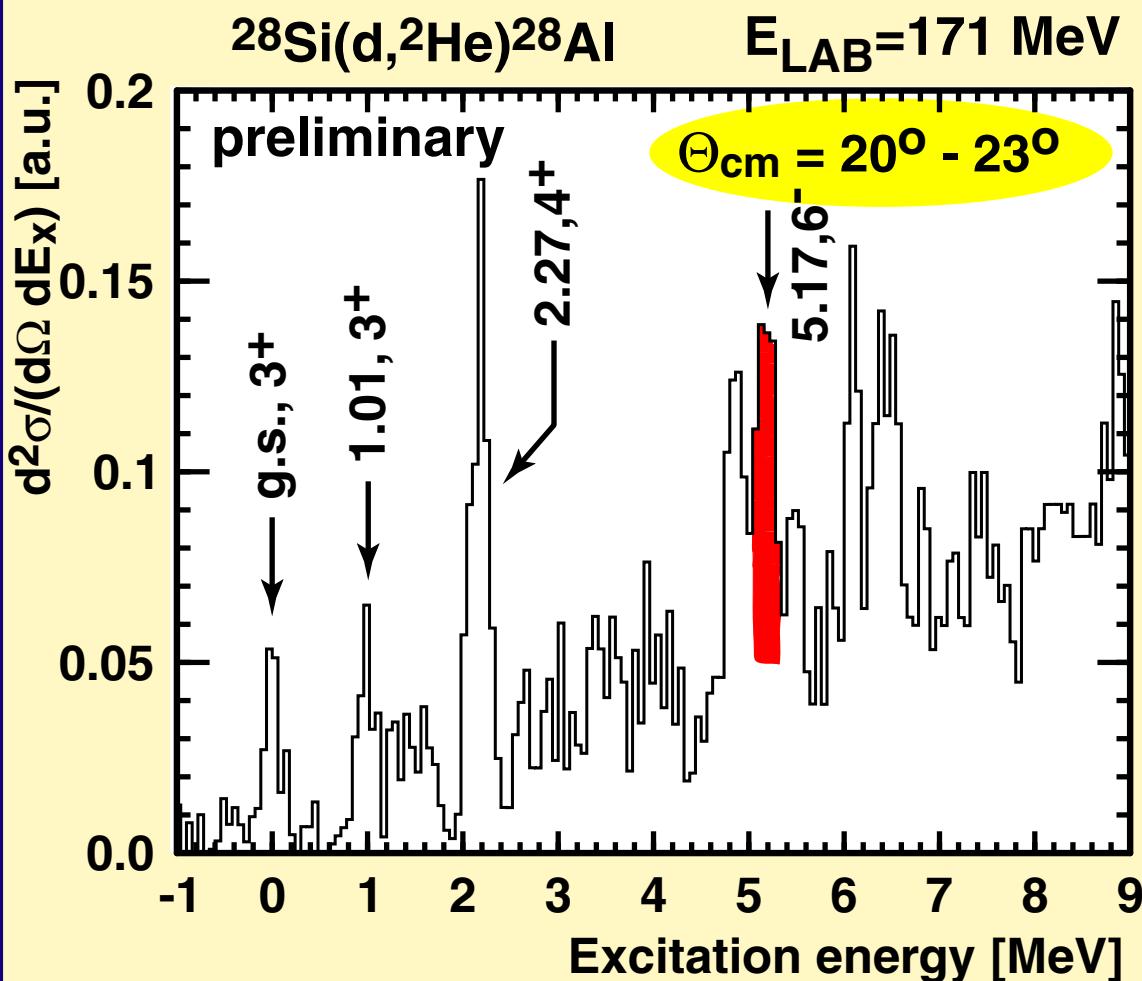
stretched states  
spectroscopy using (n,p)  
at large q



TRIUMF-data

# Study of the tensor force thru excitation of "Stretched States"

(d,  ${}^2\text{He}$ )



6<sup>-</sup> state is not as strong as expected

- q-dependence of tensor force for (d,  ${}^2\text{He}$ )?
- momentum transfer only through one single nucleon?

# Conclude:

## astrophysics:

The  $(d, {}^2\text{He})$  probably the best tool so far to locate GT transitions

GT transition strength need also be known for non-stable nuclei

**experiment:** radioactive beams, inverse kinematics

**theory:** needs to be credible, if to venture into the unstable region;  
credibility will be gained by extended experiments

## halo nuclei spectroscopy:

the  $(d, {}^2\text{He})$  reaction was only a side-effect, the tool may be limited!

## $2\nu-\beta\beta$ decay:

the potential still not fully exploited

need more test cases

need information of phase cancellation of GT states

$2\nu - \beta^+ \beta^+$  (EC-EC) could be a further potential

## further applications:

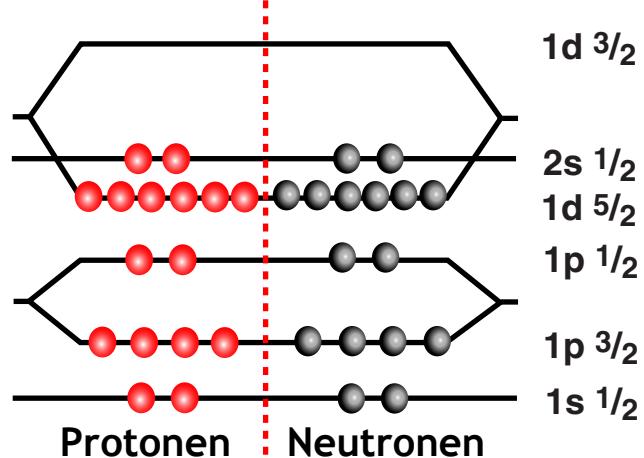
neutron-neutron scattering length

spin correlation of the 2p-system from  ${}^2\text{He}$  decay (EPR) (ongoing KVI-project !!)

stretched state spectroscopy

# The l-forbidden transition

Ground state in  $^{32}\text{S}$   $0^+$



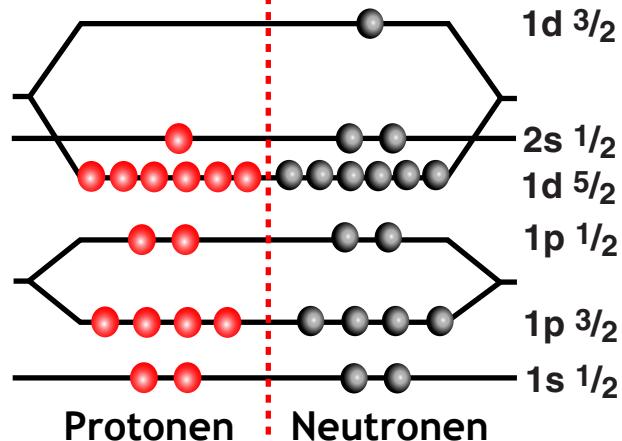
$0^+$

$(\text{d}, {}^2\text{He}) \rightarrow \Delta l=0 !$

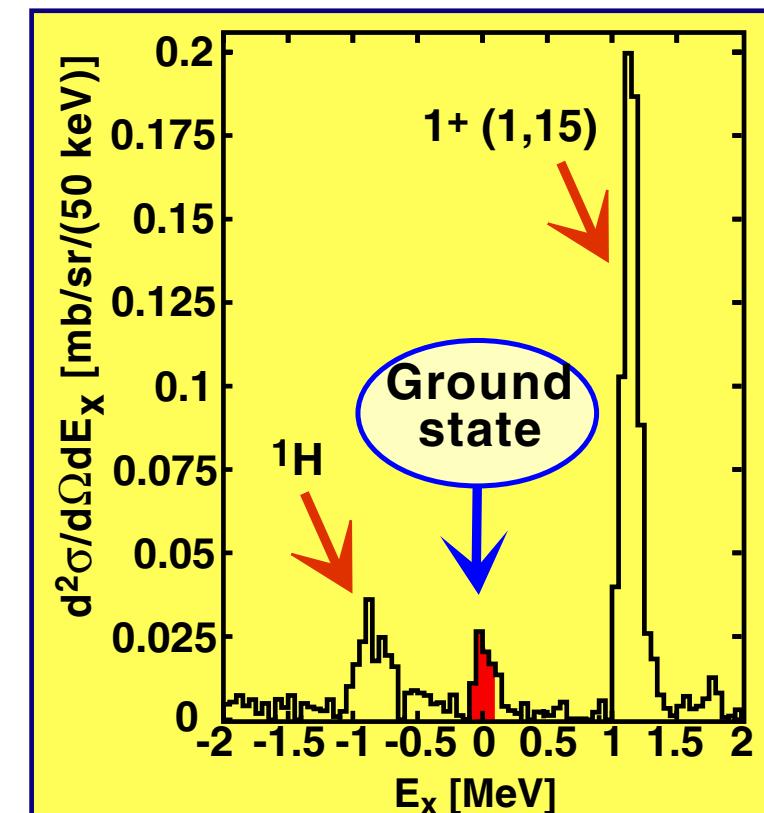
$\log ft = 7.9$

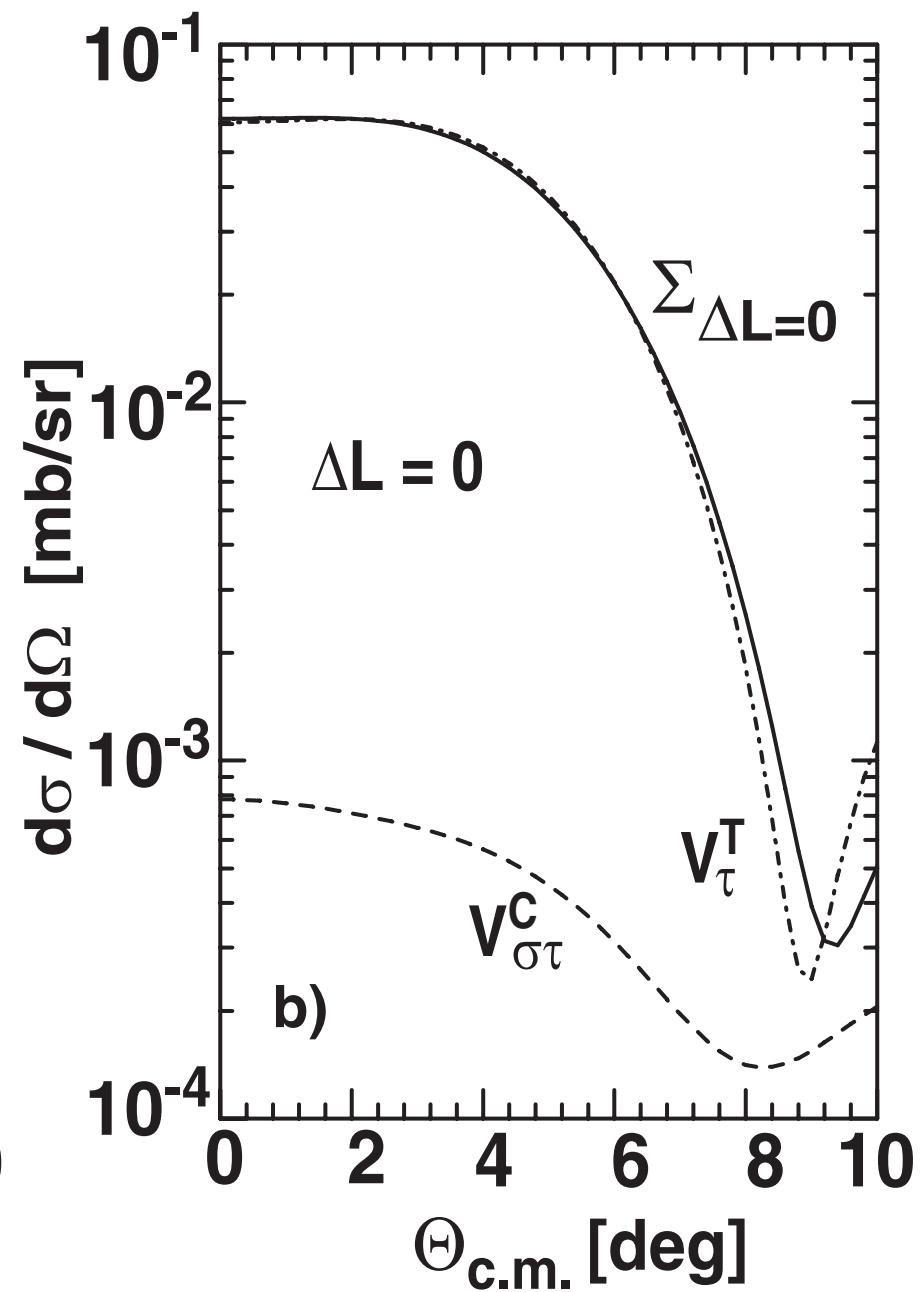
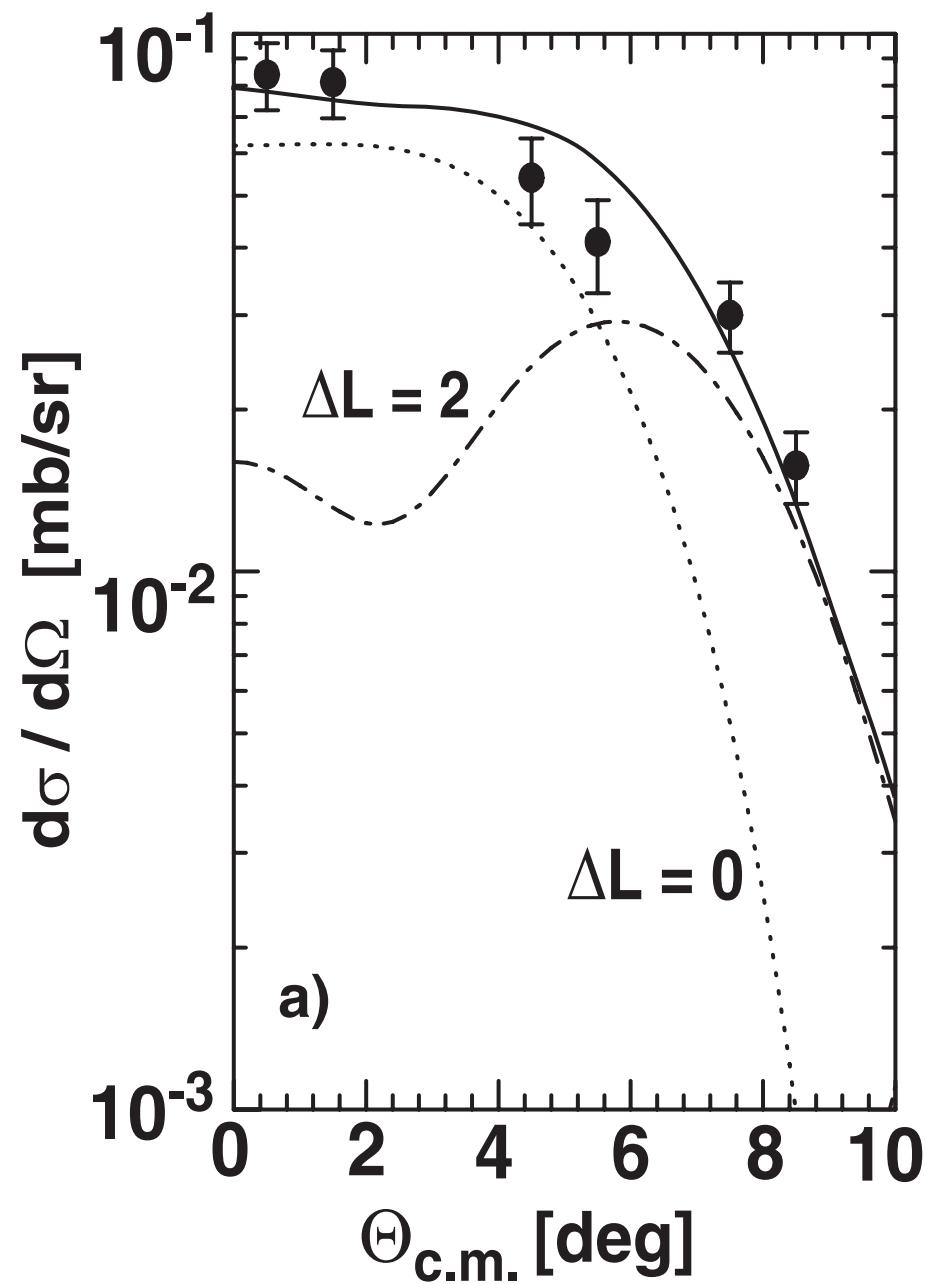
?

Ground state in  $^{32}\text{P}$



$1^+$





# Experimental Background Reduction

