

High-resolution Study of Gamow-Teller Transitions

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Nucleus : 3 active interactions out of 4

Strong, Weak, EM

→ Comparison of Analogous Transitions

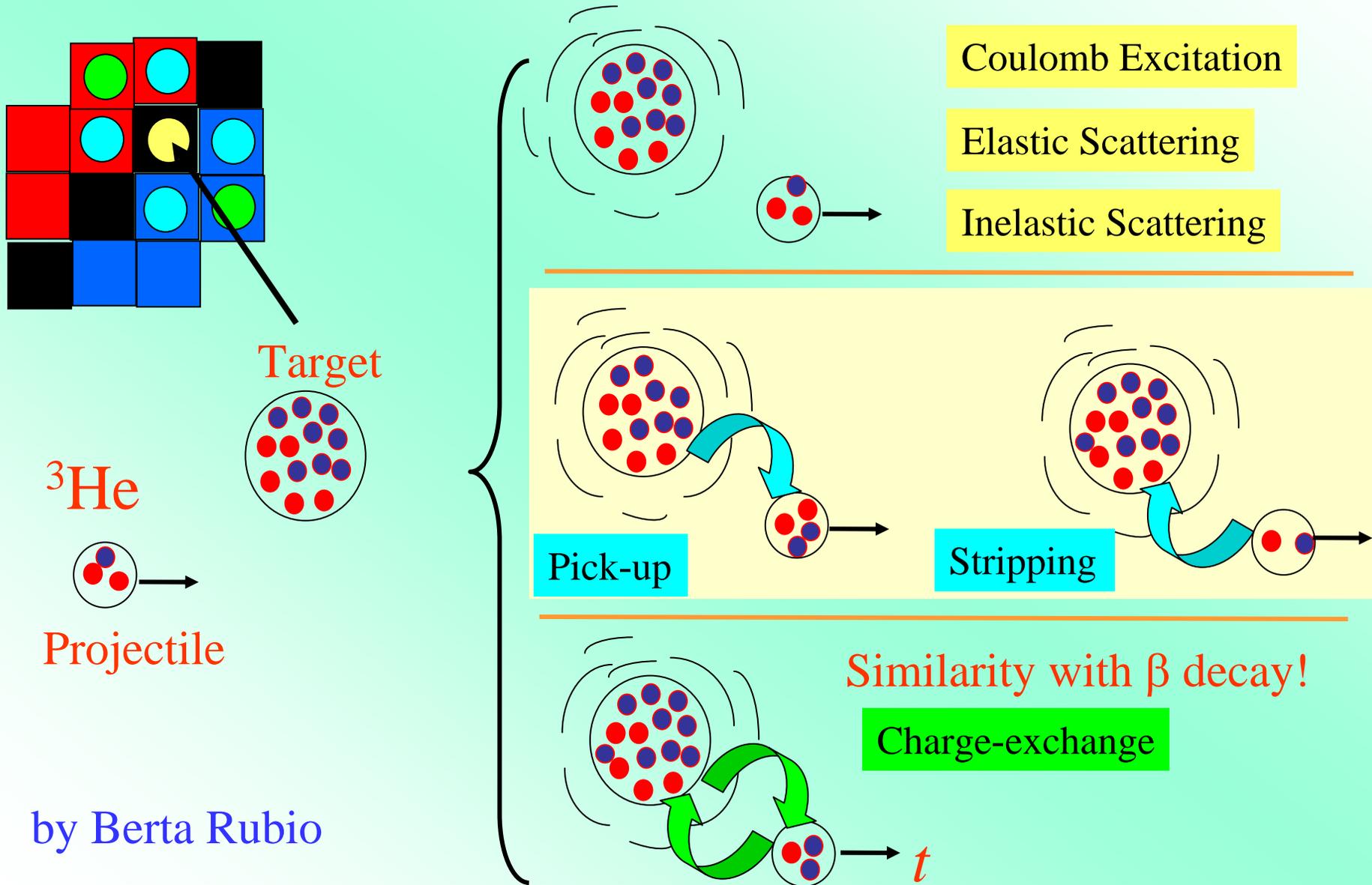
✧ High resolution ($^3\text{He},t$) experiment at 0°

$$\Delta E = 30\text{-}50 \text{ keV}$$

✧ β -decay experiment, γ -decay, (e, e') measurements

→ detailed GT responses up to high excitation energies !

Direct Reactions with Light Projectiles



by Berta Rubio

Resolutions Now and Then

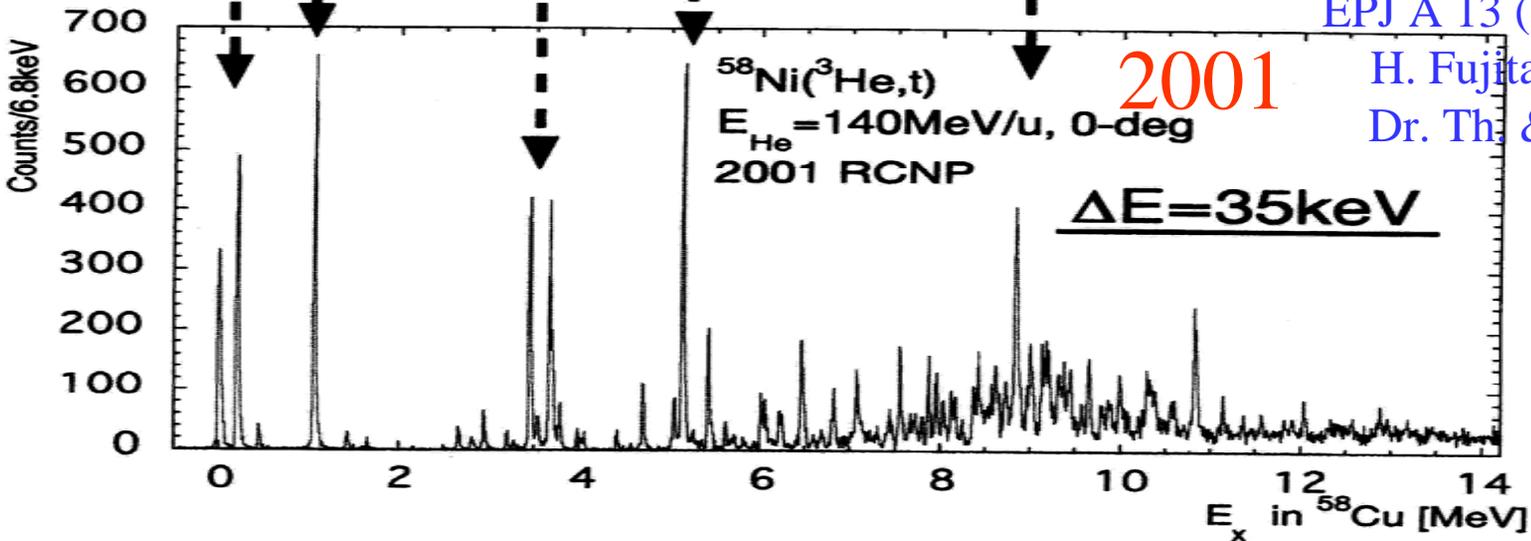
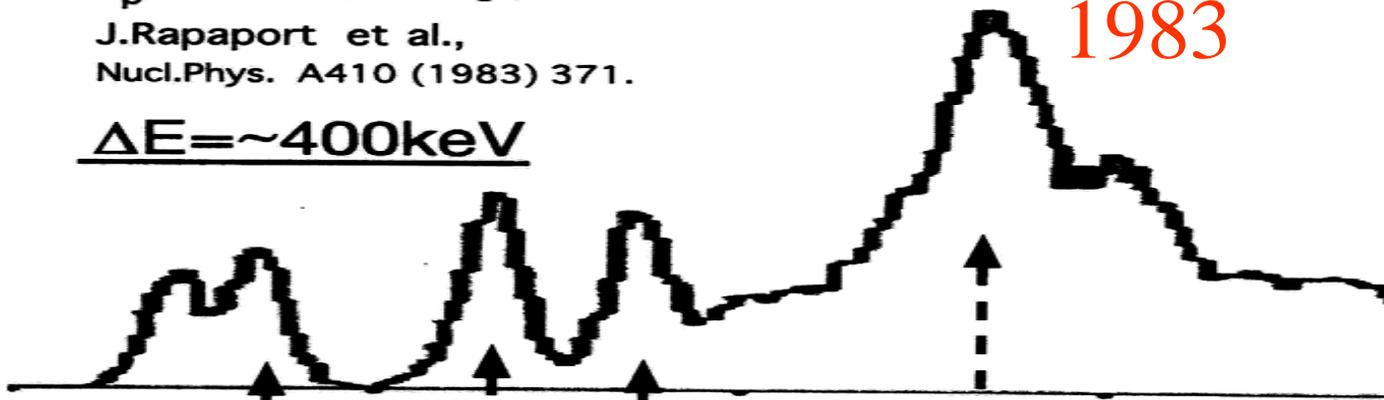
$^{58}\text{Ni}(p,n)$

$E_p=160\text{MeV}$, 0-deg., IUCF

J.Rapaport et al.,
Nucl.Phys. A410 (1983) 371.

$\Delta E \approx 400\text{keV}$

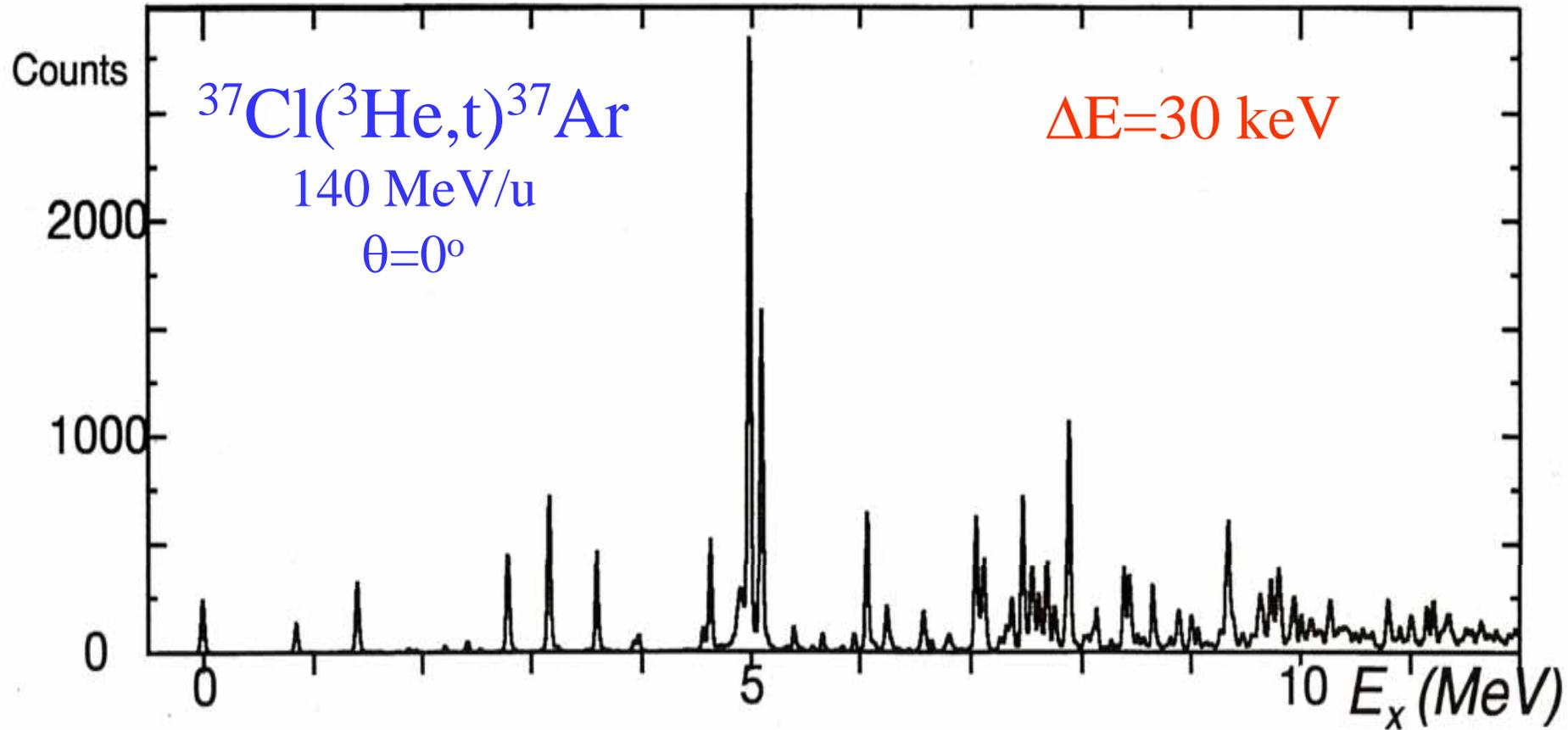
1983



Y. Fujita et al.,
EPJ A 13 ('02) 411.
H. Fujita et al.,
Dr. Th. & PRC

$^{37}\text{Cl}(^3\text{He},t)^{37}\text{Ar}$ spectrum

Y. Shimbara et al.



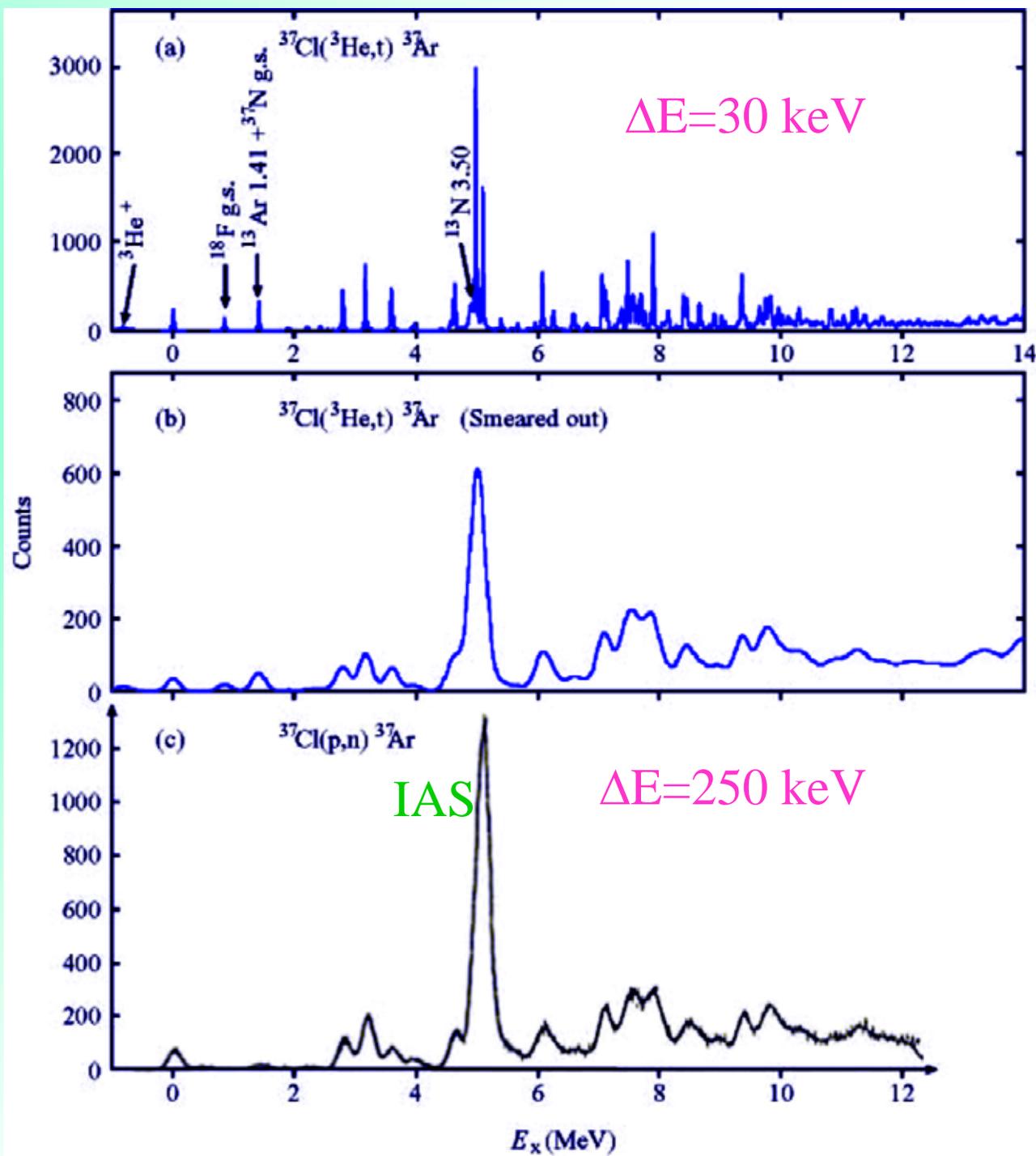
$(^3\text{He},t)$ & (p,n)
on ^{37}Cl

Original $(^3\text{He},t)$

$(^3\text{He},t)$
convoluted with
 (p,n) resolution

Original (p,n)

Convolution
by Y. Shimbara



Key Words

High Resolution

In Charge Exchange Reactions

--at Intermediate Incident Energies--

$(^3\text{He},t)$ reaction : one order better resolution than in a (p,n) reaction

Active Operators

Similarity of Active Operators

Gamow-Teller operator in β decay (weak interaction)

Spin-isospin interaction in reactions (strong interaction)

EM-M1 interaction in γ decay (electro-magnetic int.)

Isospin Symmetry

Analog States, Analogous Transitions

Vibration Modes in Nuclei (Schematic)

	Electric Mode ($\Delta S=0$)		Magnetic Mode ($\Delta S=1$)	
	IS ($\Delta T=0$)	IV ($\Delta T=1$)	IS ($\Delta T=0$)	IV ($\Delta T=1$)
L=0				
L=1				
L=2				
L=3				

IS-M1

IV-M1

GT

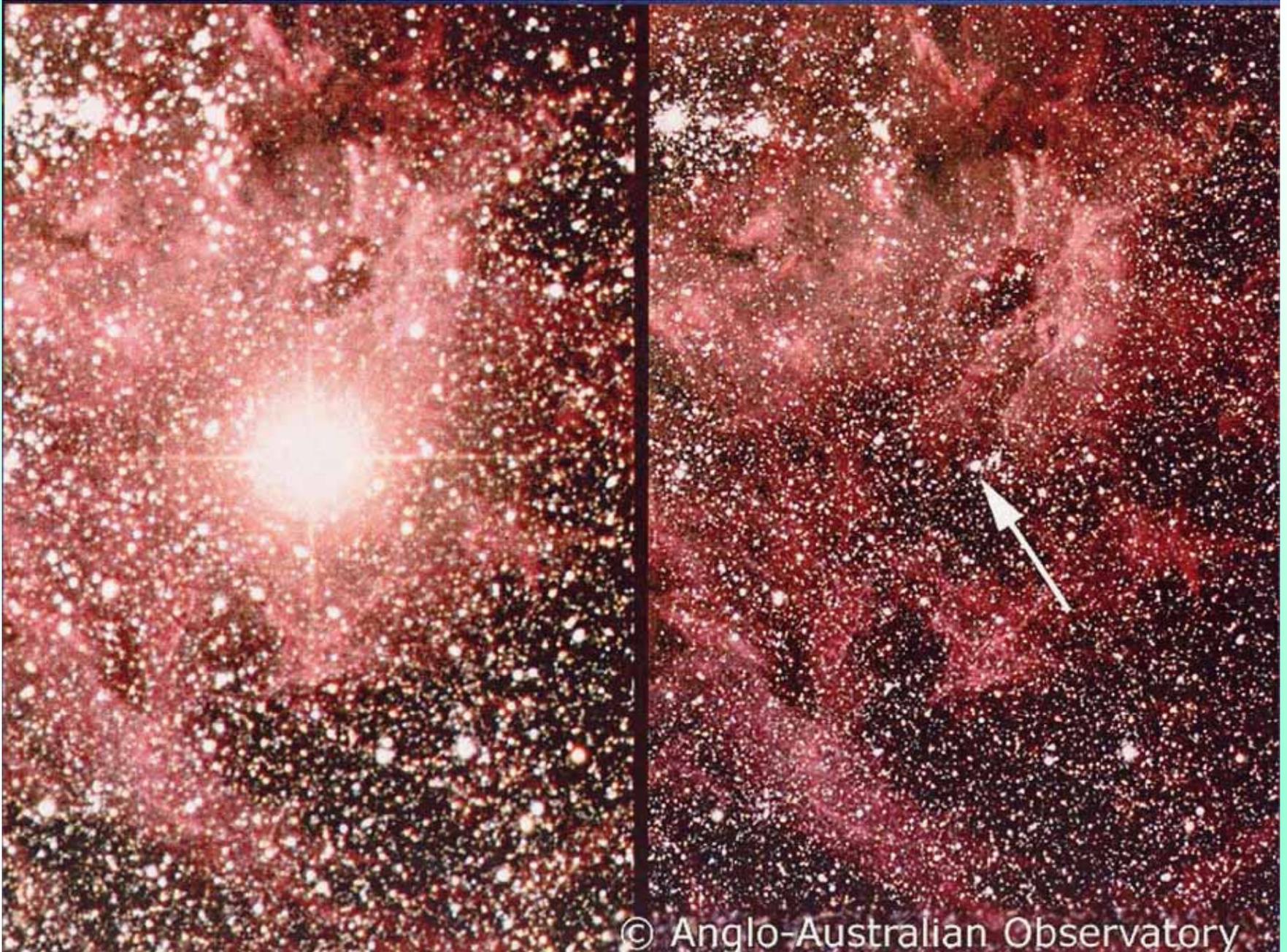
Vibration Modes in Nuclei (Operators)

Microscopic classification of giant resonances

An operator is
a hammer
to excite
nuclei !

	$\Delta S = 0$ $\Delta T = 0$	$\Delta S = 0$ $\Delta T = 1$	$\Delta S = 1$ $\Delta T = 0$	$\Delta S = 1$ $\Delta T = 1$
$L = 0$		$\sum \tau_i$ IAS		$\sum \vec{\sigma}_i \tau_i$ GTR
2 nd order	$\sum r_i^2$ ISGMR	$\sum r_i^2 \tau_i$ IVGMR	$\sum r_i^2 \vec{\sigma}_i$ ISSMR	$\sum r_i^2 \vec{\sigma}_i \tau_i$ IVSMR
$L = 1$		$\sum r_i Y_m^1 \tau_i$ IVGDR	$\sum r_i Y_m^1 \vec{\sigma}_i$ ISSDR	$\sum r_i Y_m^1 \vec{\sigma}_i \tau_i$ IVSDR
2 nd order	$\sum r_i^3 Y_m^1$ ISGDR			
$L = 2$	$\sum r_i^2 Y_m^2$ ISGQR	$\sum r_i^2 Y_m^2 \tau_i$ IVGQR	$\sum r_i^2 Y_m^2 \vec{\sigma}_i$ ISSQR	$\sum r_i^2 Y_m^2 \vec{\sigma}_i \tau_i$ IVSQR
$L = 3$	$\sum r_i^3 Y_m^3$ ISGOR	$\sum r_i^3 Y_m^3 \tau_i$ IVGOR	$\sum r_i^3 Y_m^3 \vec{\sigma}_i$ ISSOR	$\sum r_i^3 Y_m^3 \vec{\sigma}_i \tau_i$ IVSOR

Supernova SN1987A



Crucial Weak Processes during the Collapse

(A,Z)=nuclei of Fe Ni region

mainly by $\sigma\tau$



can be studied by ($^3\text{He},t$)

K.L &G.M-P

Rev.Mod.Phys.75('04)819

$$p + e^- \rightleftharpoons n + \nu_e,$$

$$n + e^+ \rightleftharpoons p + \bar{\nu}_e,$$

$$(A, Z) + e^- \rightleftharpoons (A, Z-1) + \nu_e,$$

$$(A, Z) + e^+ \rightleftharpoons (A, Z+1) + \bar{\nu}_e,$$

$$\nu + N \rightleftharpoons \nu + N,$$

$$N + N \rightleftharpoons N + N + \nu + \bar{\nu},$$

$$\nu + (A, Z) \rightleftharpoons \nu + (A, Z),$$

$$\nu + e^\pm \rightleftharpoons \nu + e^\pm,$$

$$\nu + (A, Z) \rightleftharpoons \nu + (A, Z)^*,$$

$$e^+ + e^- \rightleftharpoons \nu + \bar{\nu},$$

$$(A, Z)^* \rightleftharpoons (A, Z) + \nu + \bar{\nu}.$$

$B(\text{GT})$ derivation

β decay :fundamental, but E_x range :limited "Q-window limitation"

(p, n) reaction at intermediate energies ($E = 100\text{-}500$ MeV)

"proportionality" : $B(\text{GT})$ and $\sigma(0^\circ)$

$$\sigma(0^\circ) = KN_{\sigma\tau} |J_{\sigma\tau}(0^\circ)|^2 B(\text{GT})$$

Breakthrough against "Q-window limitation"

but resolution : rather poor ($\Delta E = 200\text{-}400$ keV)

$(^3\text{He}, t)$ reaction at intermediate energies ($E = 130\text{-}150$ MeV/u)

"high resolution" ($\Delta E < 50$ keV)

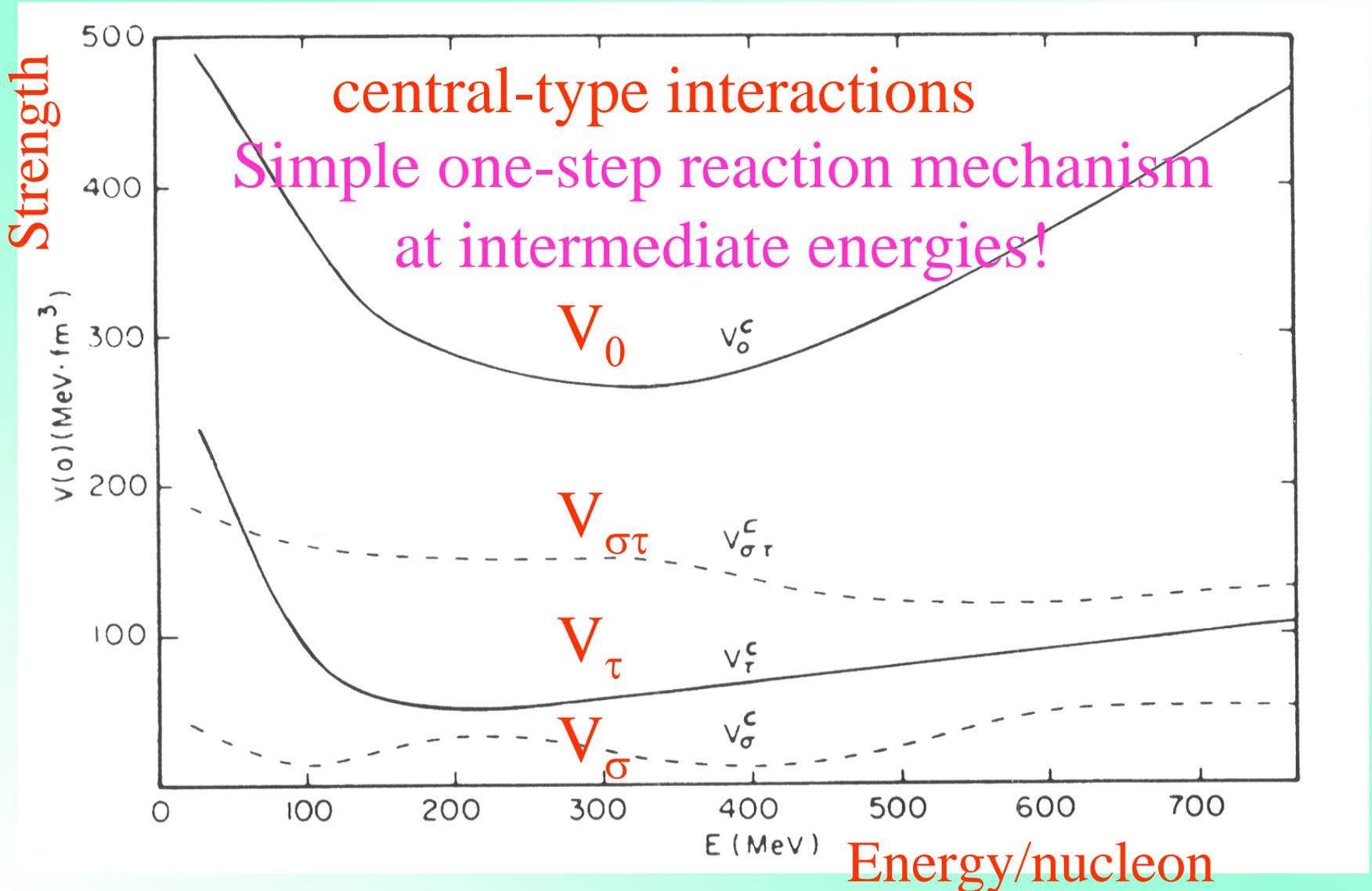
magnetic spectrometer, matching techniques

"proportionality" : good ($B(\text{GT}) > 0.03$)

Breakthrough against "Energy resolution limitation"

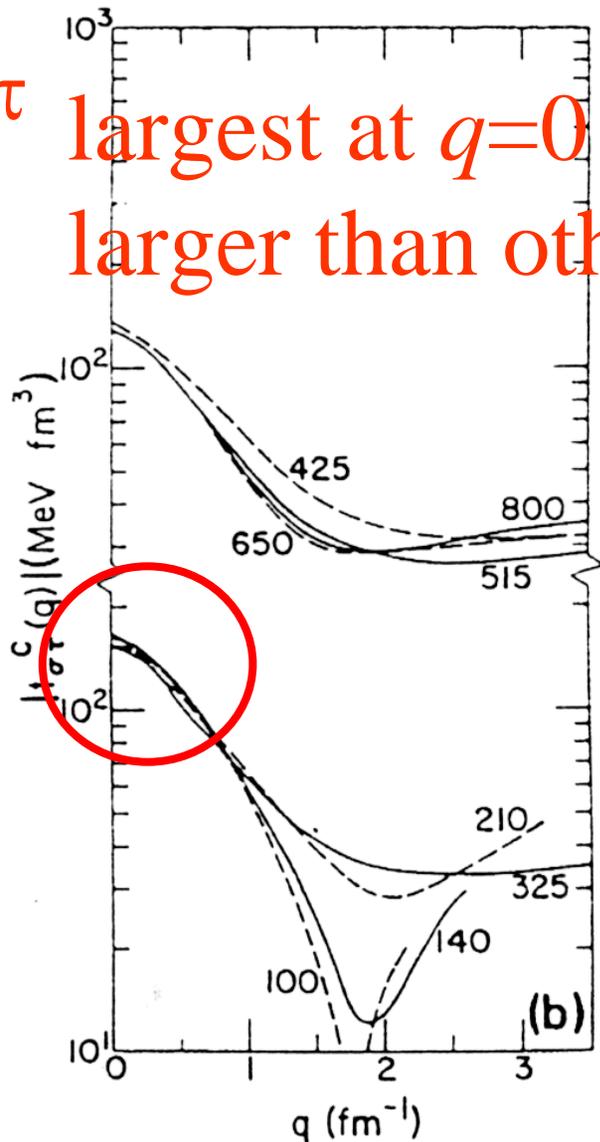
Reliable $B(\text{GT})$ values for individual transitions

Nucleon-Nucleon Int. : E_{in} dependence at $q = 0$

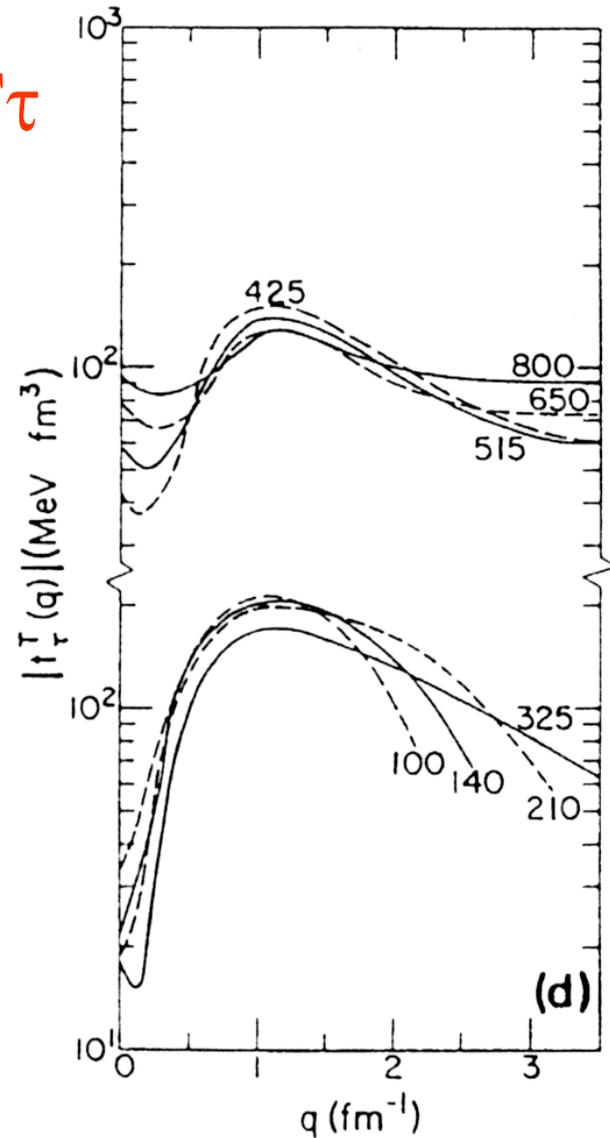


N.-N. Int. : $\sigma\tau$ & Tensor- τ q -dependence

$\sigma\tau$ largest at $q=0$!
larger than others !

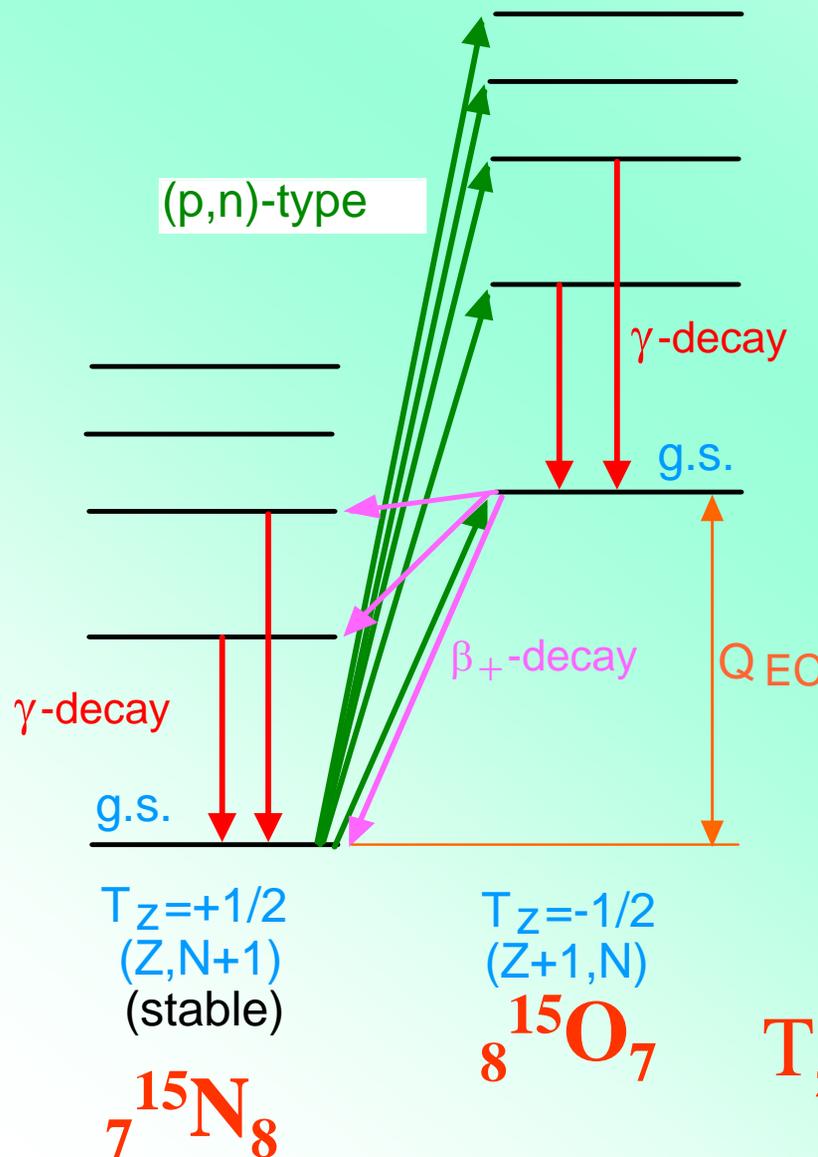


$T\tau$

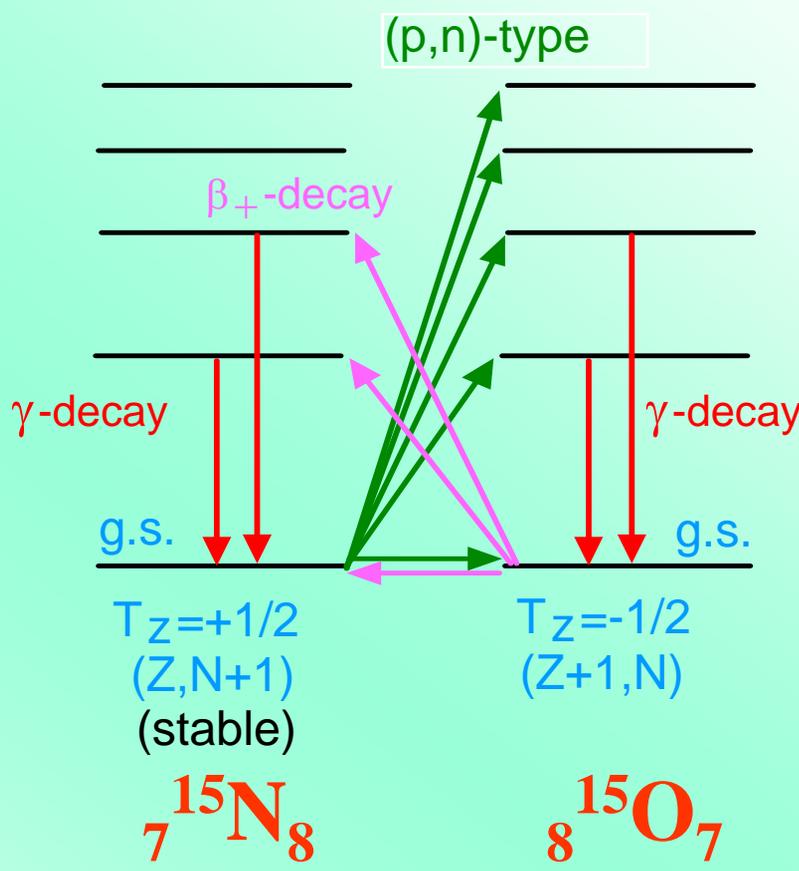


Analogous Structures and Transitions in T=1/2 System

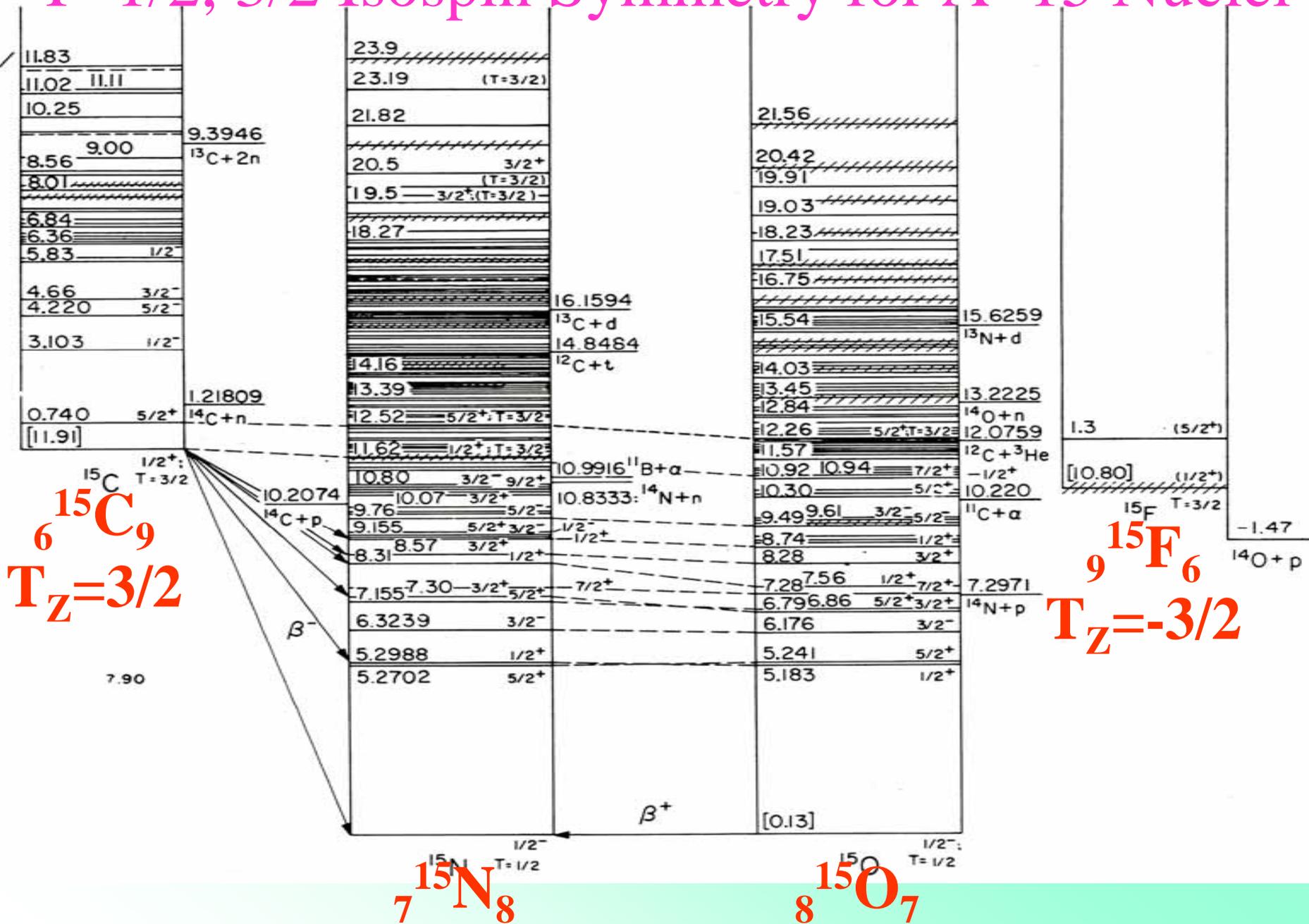
Real Energy Space



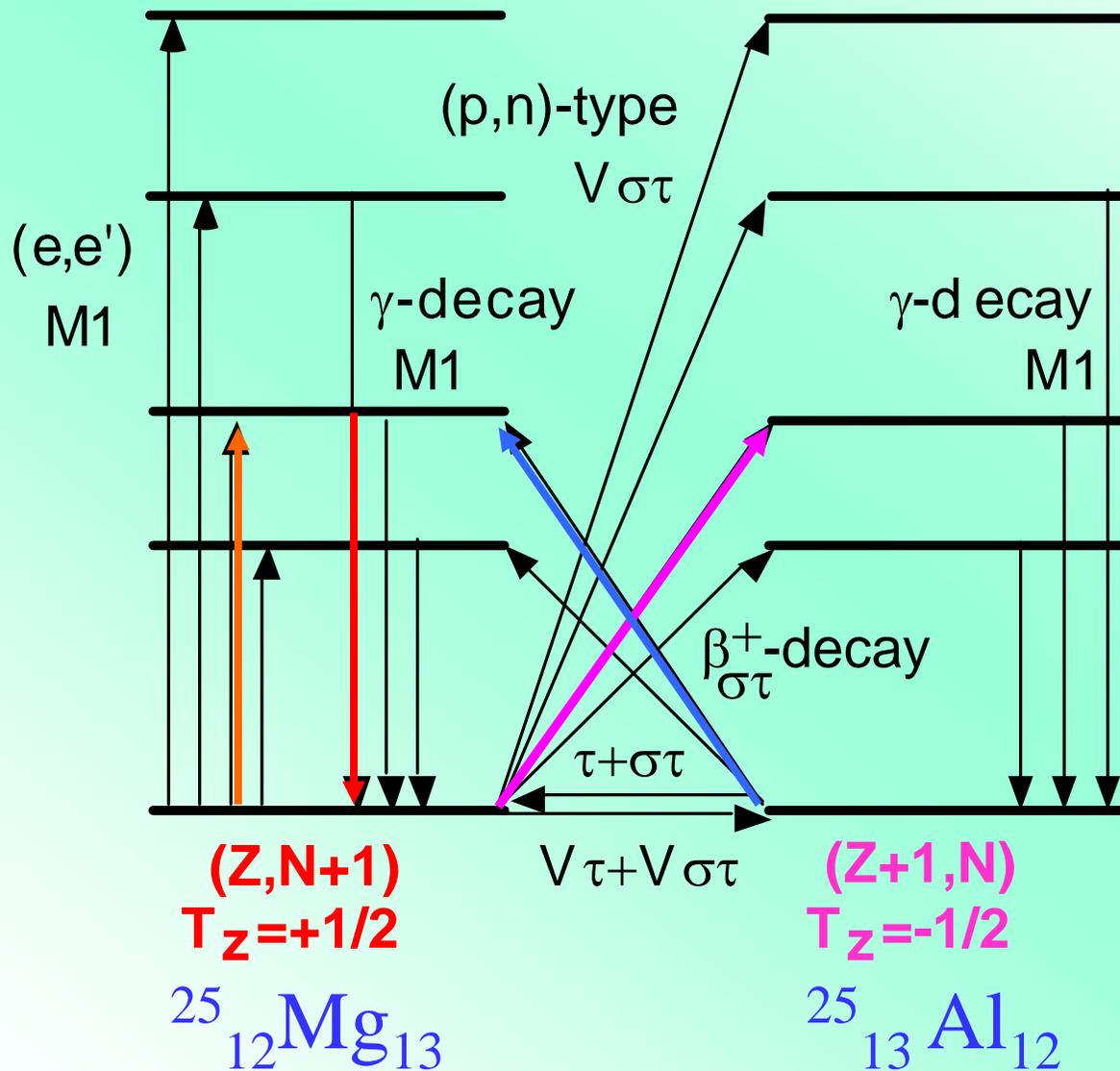
Isospin Symmetry Space



T=1/2, 3/2 Isospin Symmetry for A=15 Nuclei



$T=1/2$ Mirror Nuclei : Structures & Transitions



Analogous
Transitions
in β decay
in CE reaction
in γ -decay
in IE reaction

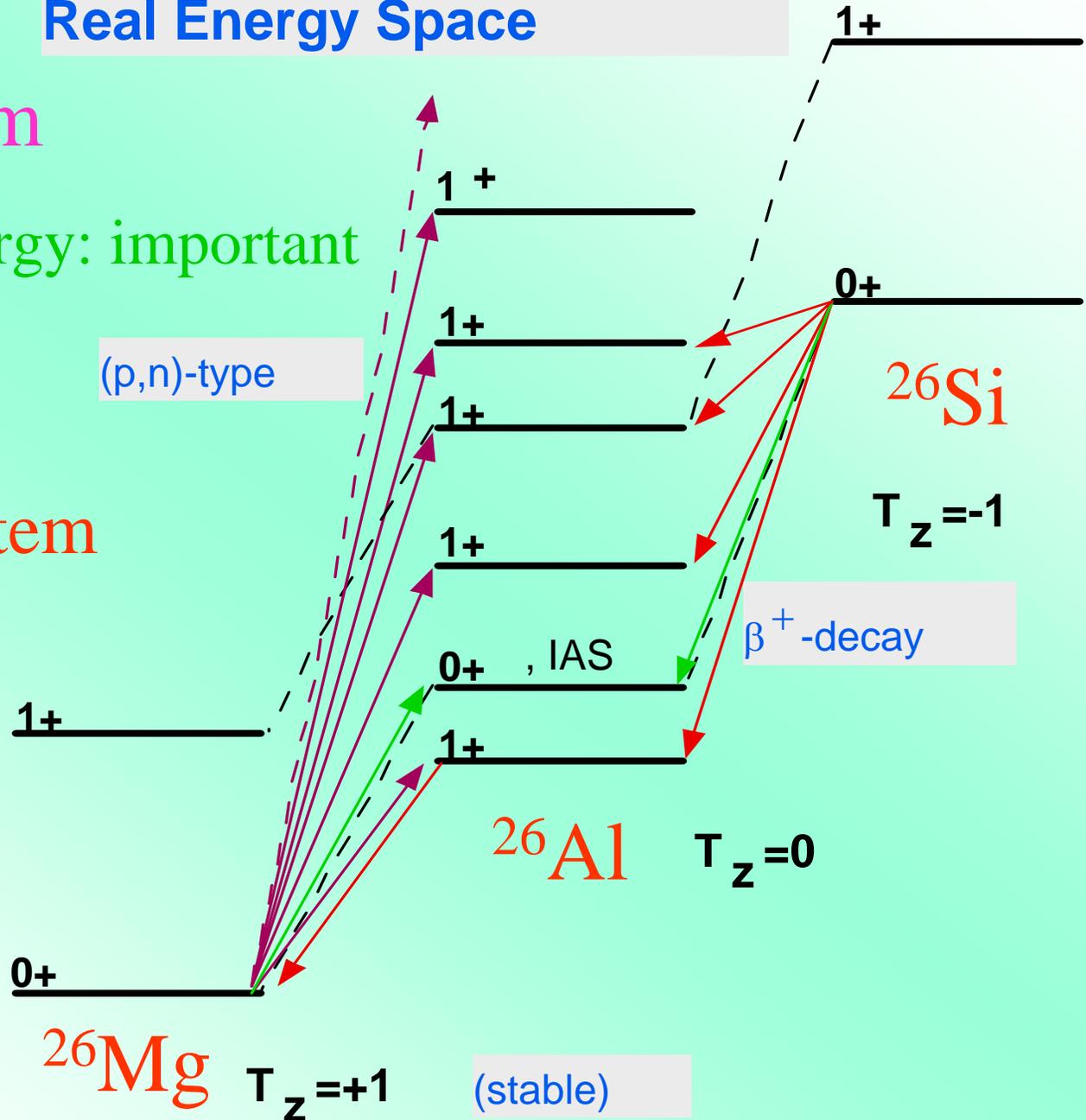
Real Energy Space

T=1 system

Coulomb Energy: important

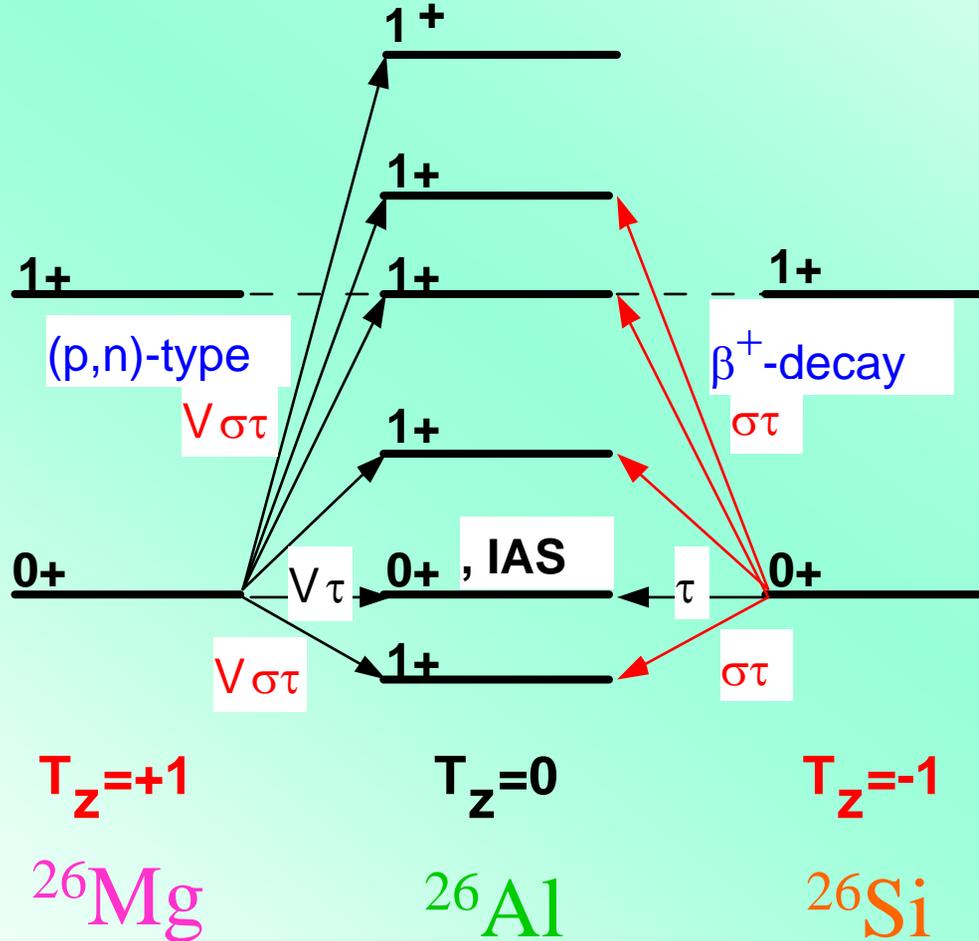
(p,n)-type

A=26 system

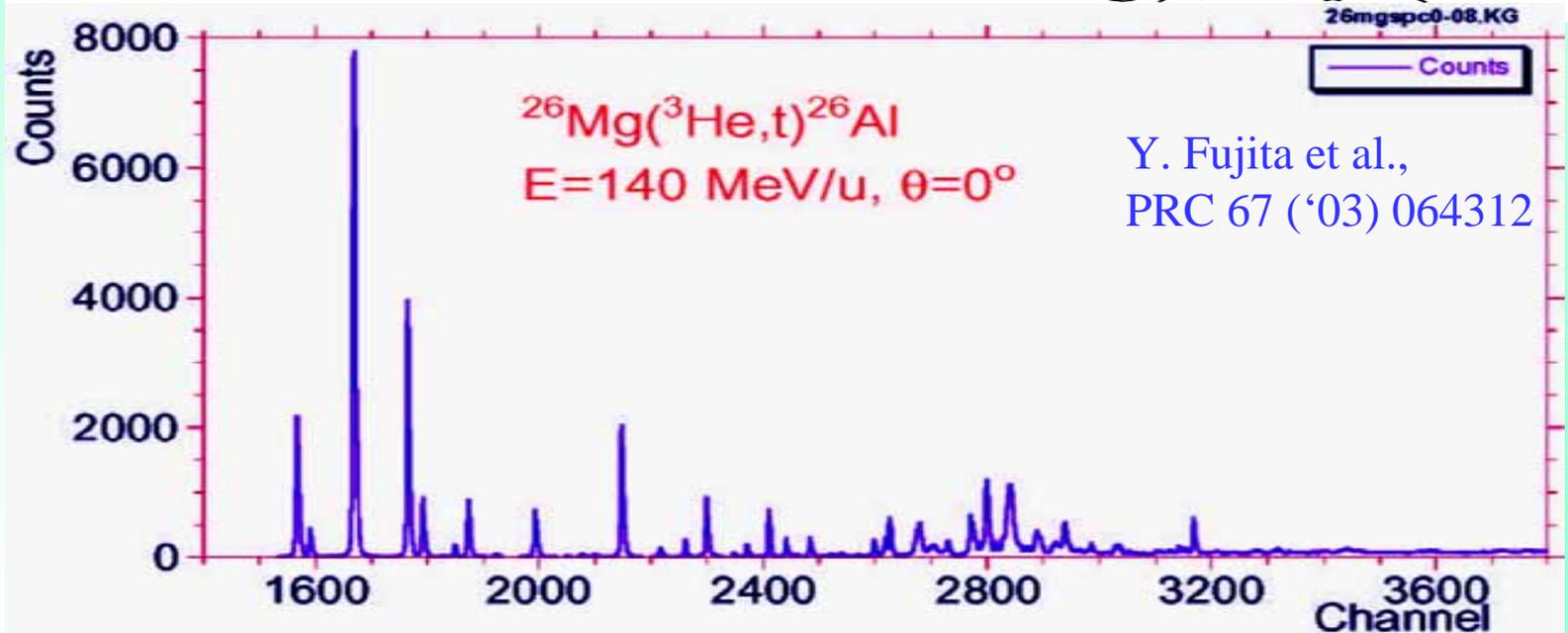
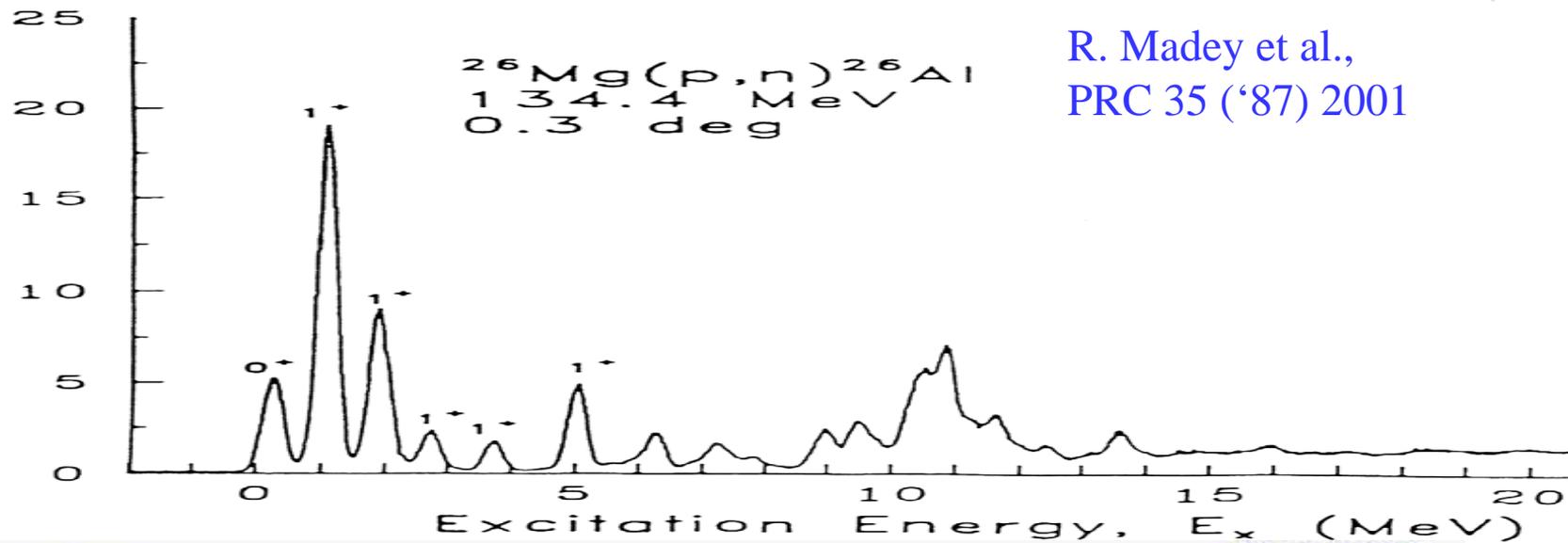


T=1 symmetry : Structures & Transitions

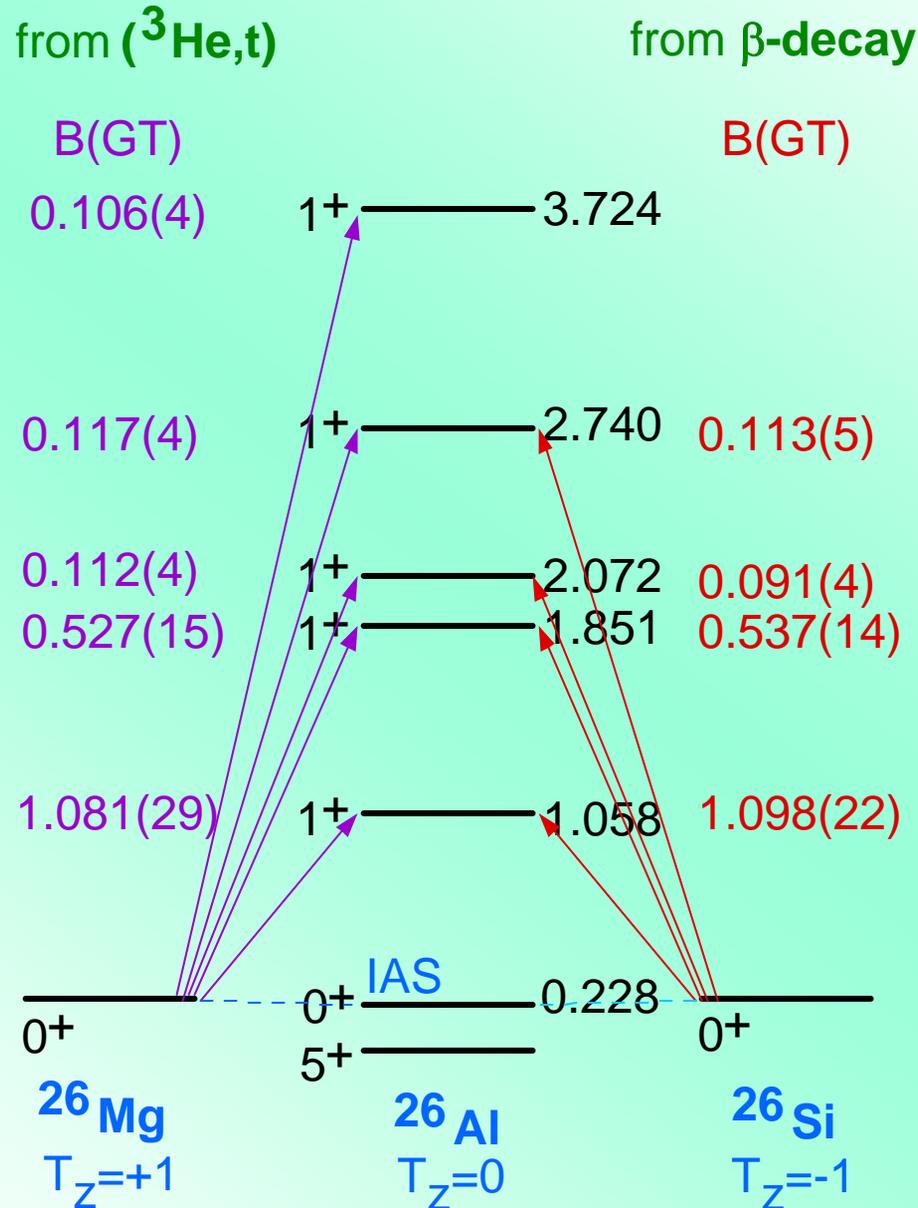
$T_z=+1 \quad \longrightarrow \quad T_z=0 \quad \longleftarrow \quad T_z=-1$
 (in isospin symmetry space*)



$^{26}\text{Mg}(p, n)^{26}\text{Al}$ & $^{26}\text{Mg}(^3\text{He}, t)^{26}\text{Al}$ spectra

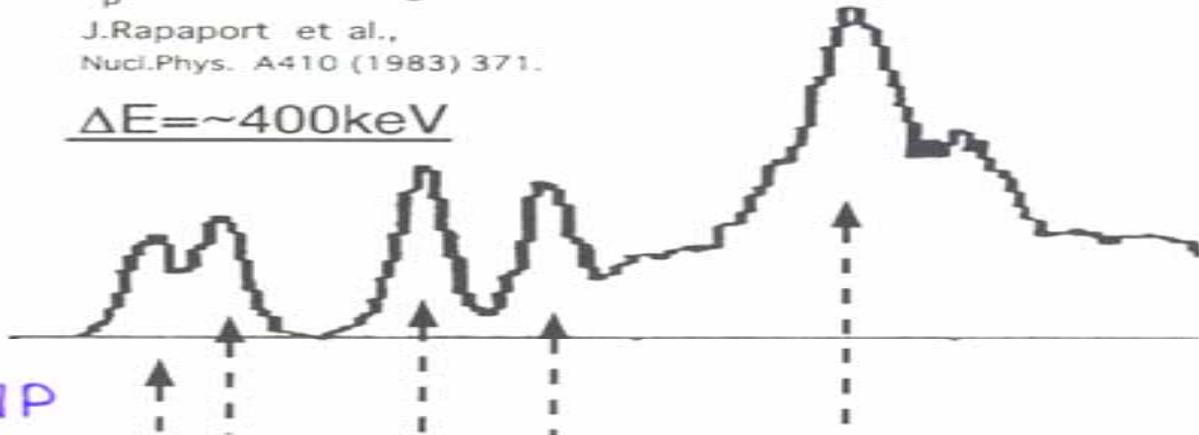


B(GT) values from Symmetry Transitions (A=26)



$E_p = 160 \text{ MeV}$, 0-deg., 10CP
 J.Rapaport et al.,
 Nucl.Phys. A410 (1983) 371.

$\Delta E = \sim 400 \text{ keV}$



RCNP

counts
 1000
 800
 600
 400
 200
 0

before
 WS

$^{58}\text{Ni}({}^3\text{He}, t)^{58}\text{Cu}$
 $E({}^3\text{He}) = 450 \text{ MeV}, \theta = 0$

Y.Fujita et al.
 Phys. Lett. B365
 (1996) 29

Rome is not made in one day!

WS

Counts/6.8keV
 700
 600
 500
 400
 300
 200
 100
 0

$^{58}\text{Ni}({}^3\text{He}, t)$
 $E_{\text{He}} = 140 \text{ MeV/u}, 0\text{-deg}$
 2001 RCNP

$\Delta E = 35 \text{ keV}$

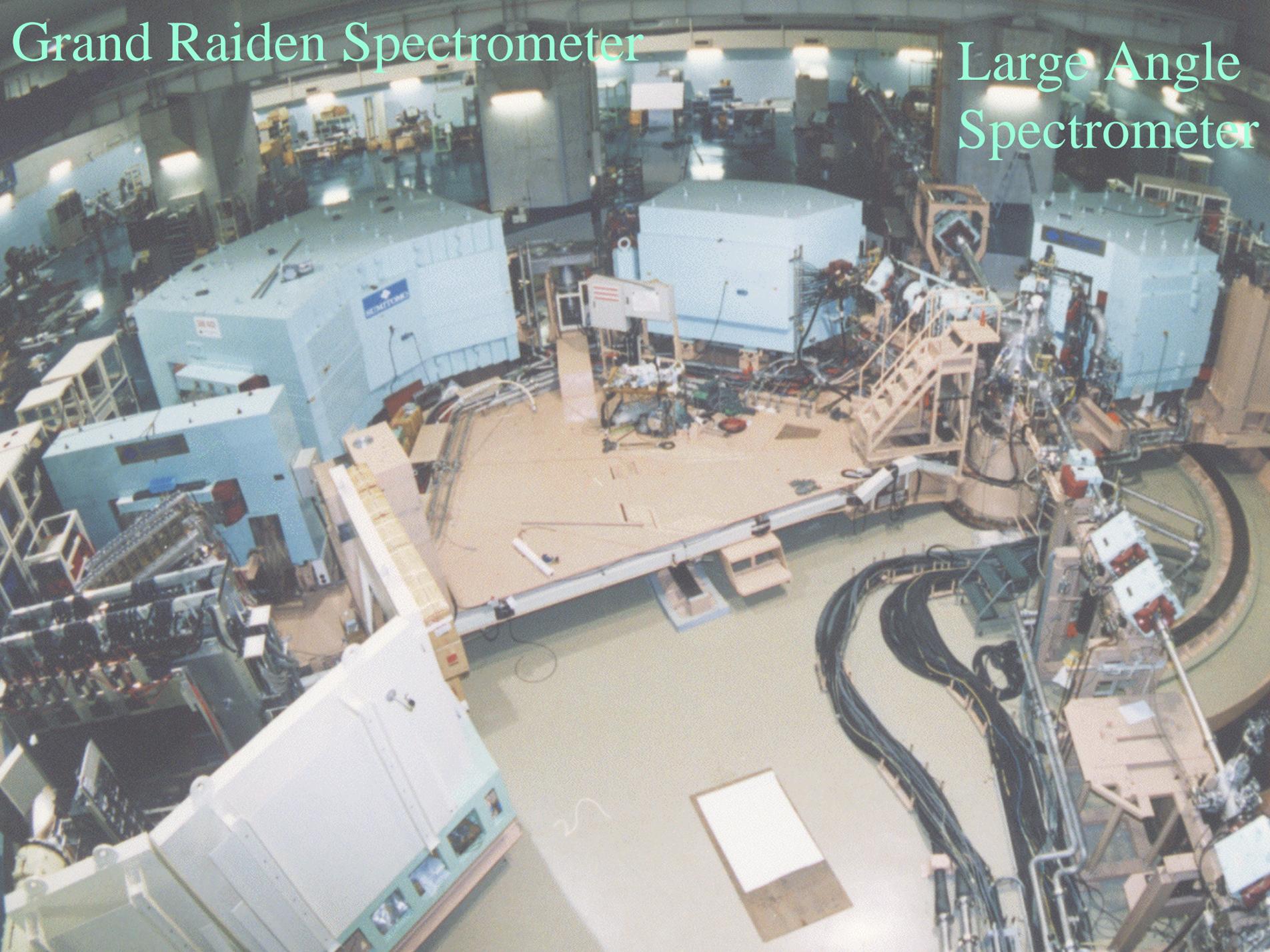
H.Fujita et al.
 PhD thesis

Y.Fujita et al.
 Euro. Phys. J. A
 13 (2002) 411
 ($E_x \leq 8 \text{ MeV}$)

E_x in ^{58}Cu [MeV]

Grand Raiden Spectrometer

Large Angle Spectrometer



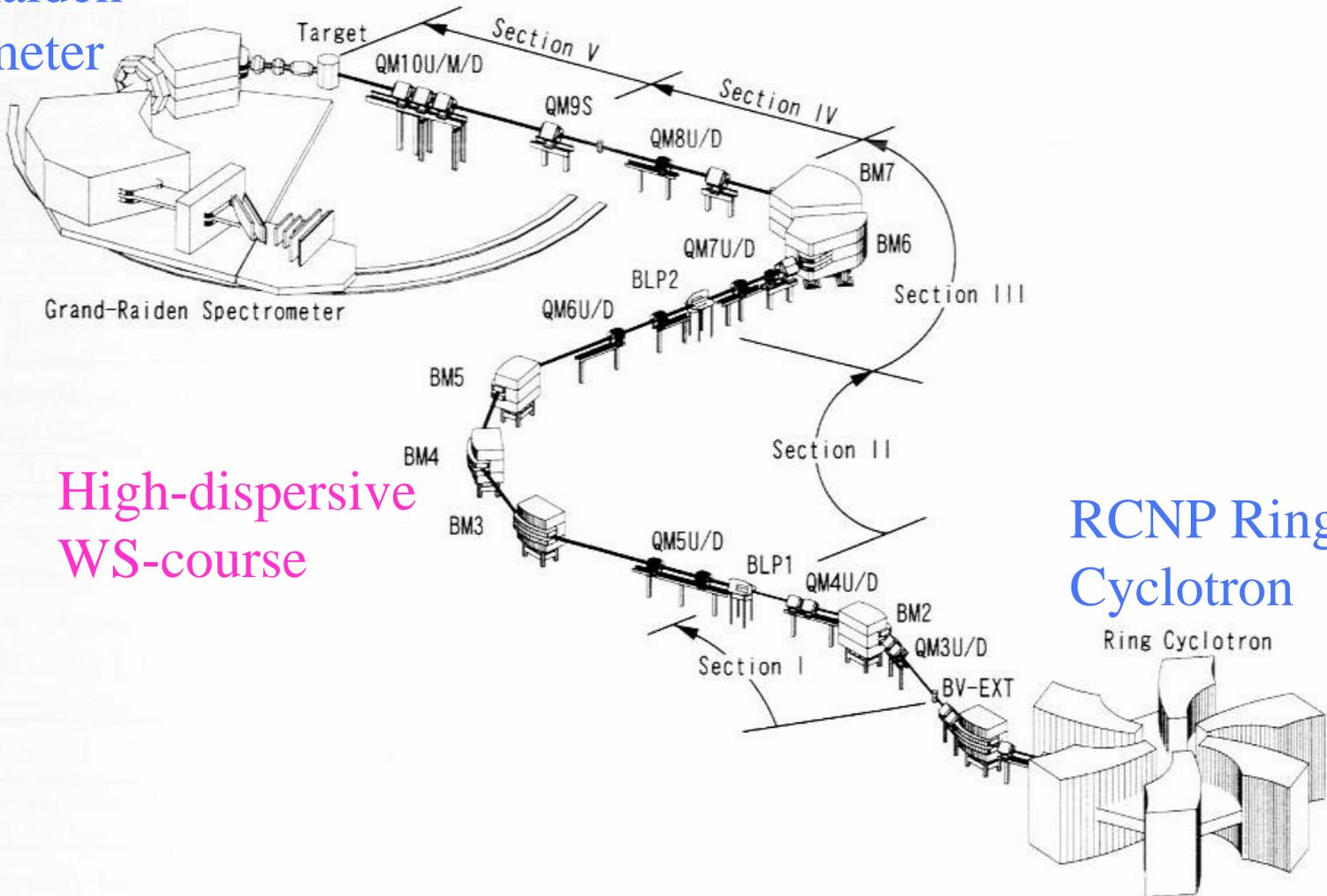
RCNP Ring Cyclotron



Beam line WS-course

T. Wakasa et al., NIM A482 ('02) 79.

Grand-Raiden
Spectrometer



High-dispersive
WS-course

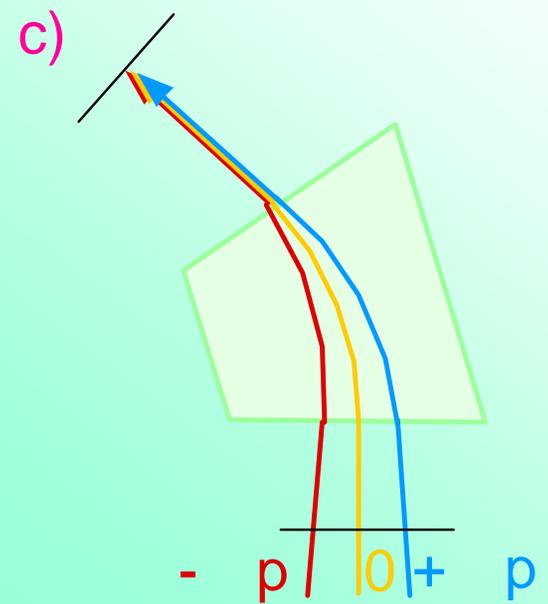
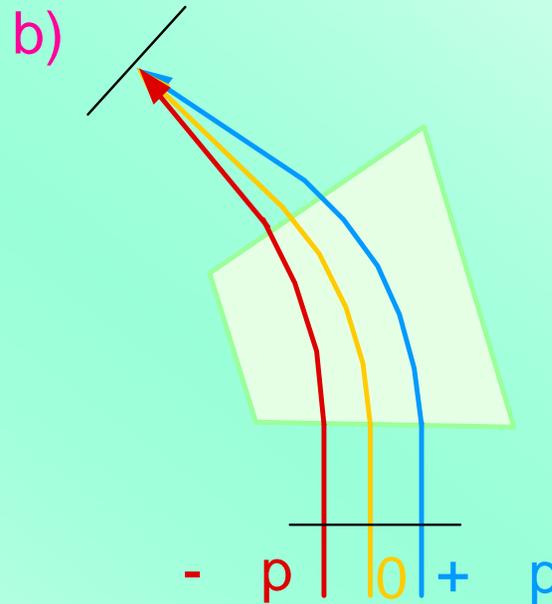
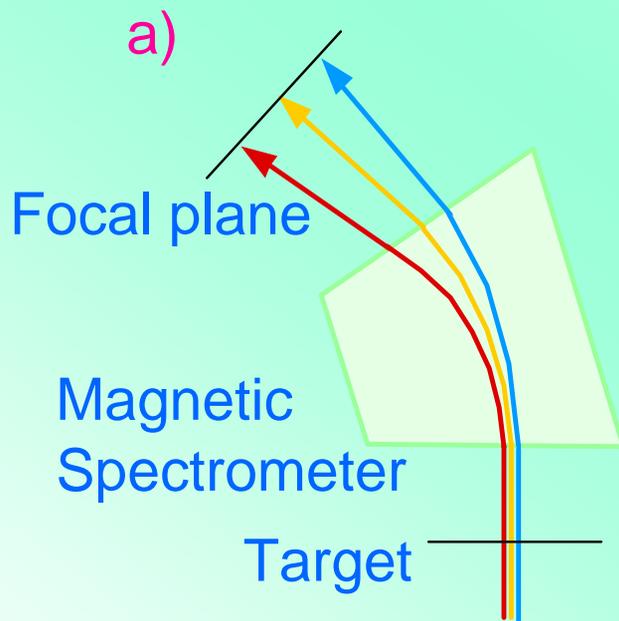
RCNP Ring
Cyclotron

Ring Cyclotron

Matching Techniques

Y. Fujita et al., N.I.M. B 126 (1997) 274.

H. Fujita et al., N.I.M. A 484 (2002) 17.



Achromatic beam transportation

$\Delta E \sim 200$ keV
for 140MeV/u³He beam

Lateral dispersion matching

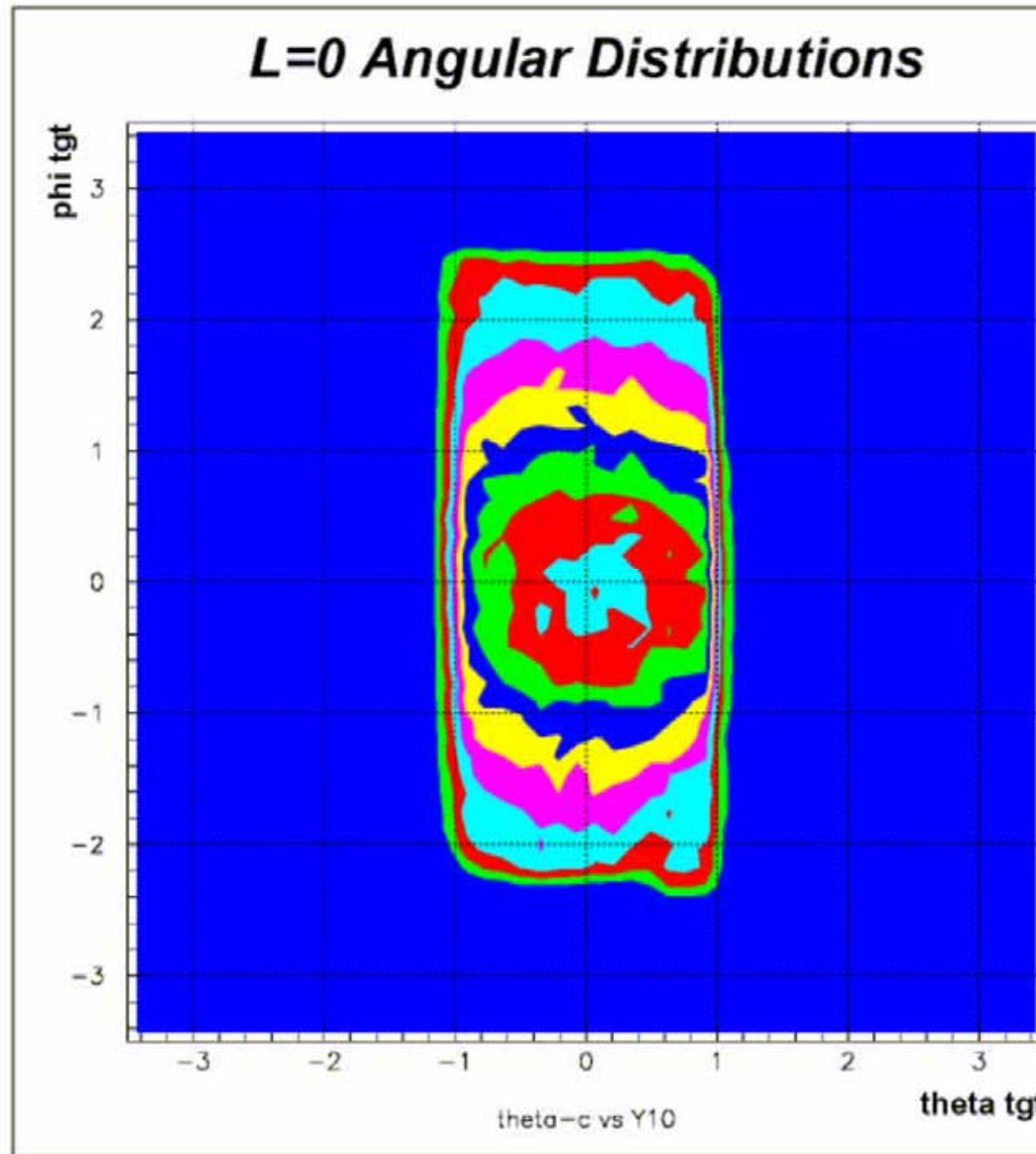
$\Delta E \sim 35$ keV
Horiz. angle resolution
 $\Delta\theta_{sc} > 15$ mrad

Angular dispersion matching

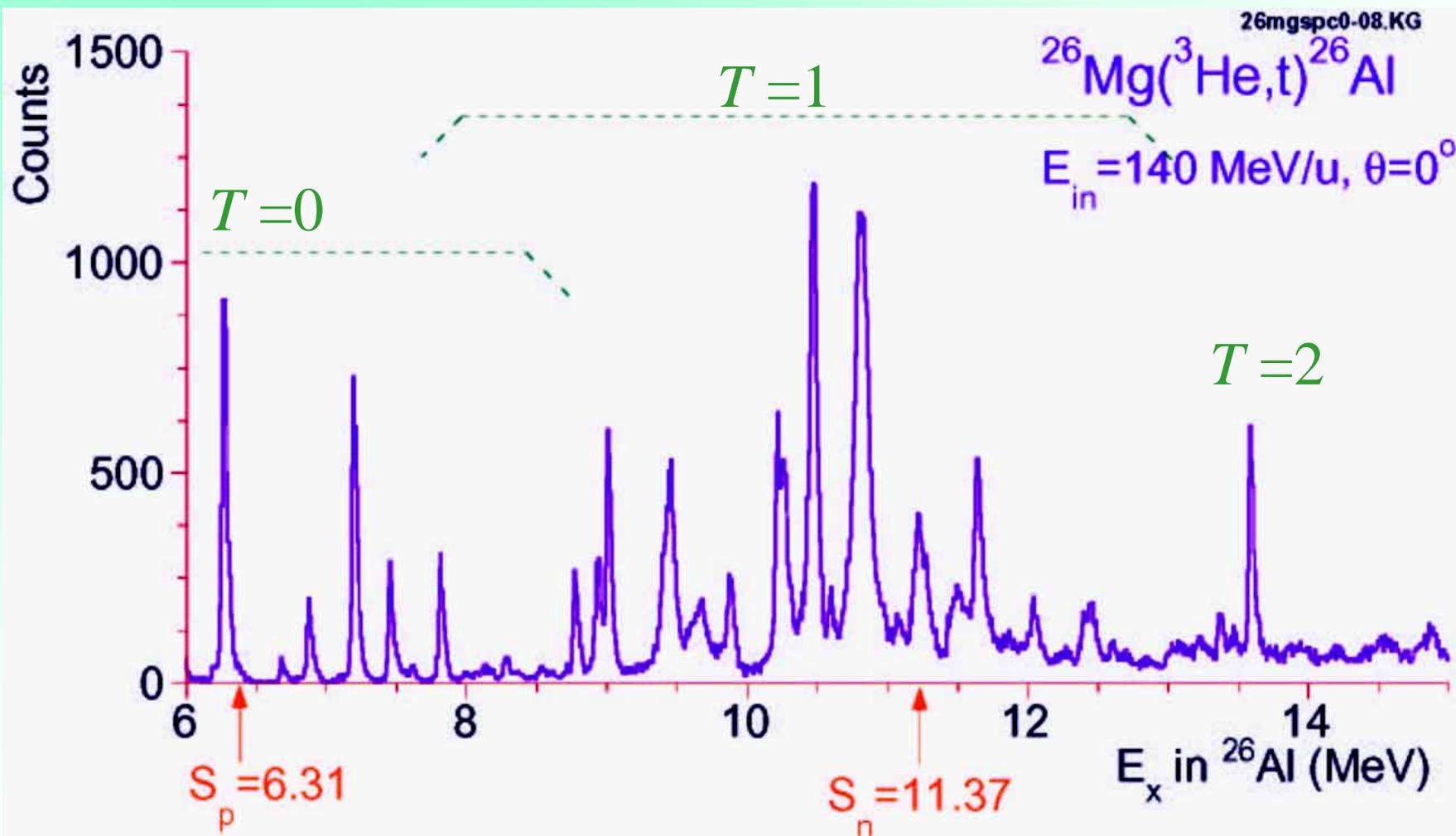
$\Delta\theta_{sc} \sim 5$ mrad

Contour Map within the Acceptance

Concentric L=0 angular
distribution around 0°

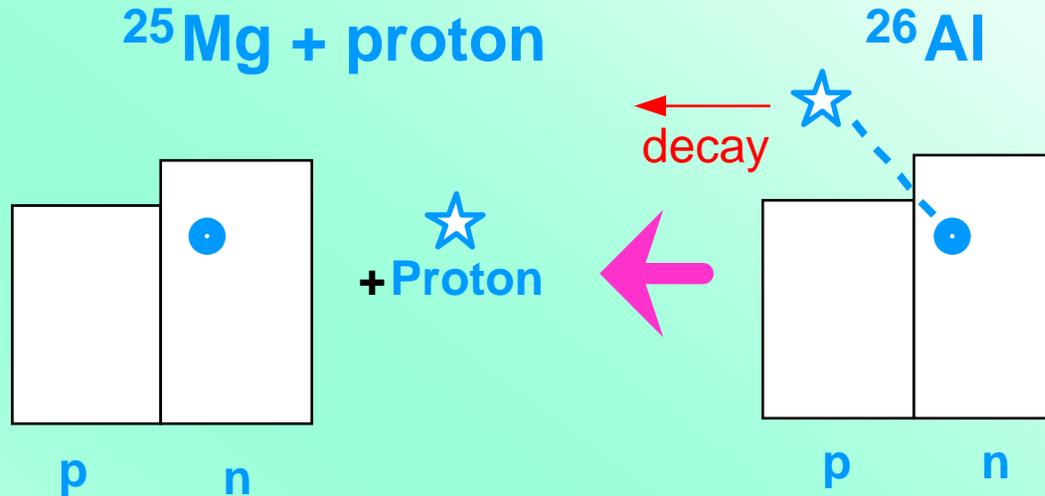


Higher- E_x region in ^{26}Al : $T=1$ & $T=2$ states



Width of a state: observed ! $\Delta E \Delta t \sim h$

Importance of Isospin : in p -decay of ^{26}Al



$$T_z : 1/2 + (-1/2) = 0$$

$$T : 1/2 + 1/2 = 0 \text{ or } 1$$

$$3/2 + 1/2 = 1 \text{ or } 2$$

S_p (p-sep. energy) in ^{26}Al : 6.31 MeV

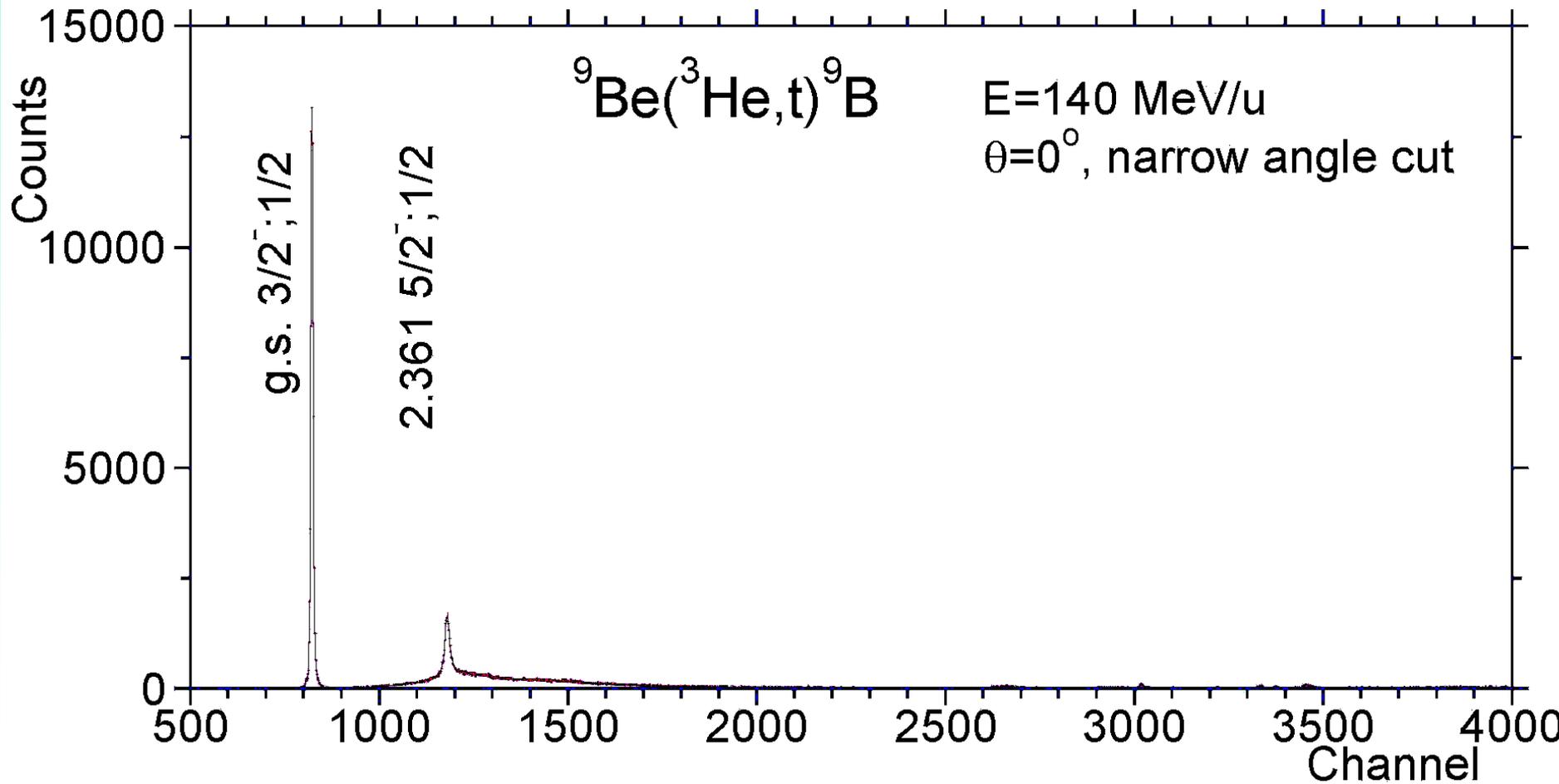
$T=3/2$ state in ^{25}Mg : $E_x > 7.79$ MeV

➔ effective S_p in ^{26}Al

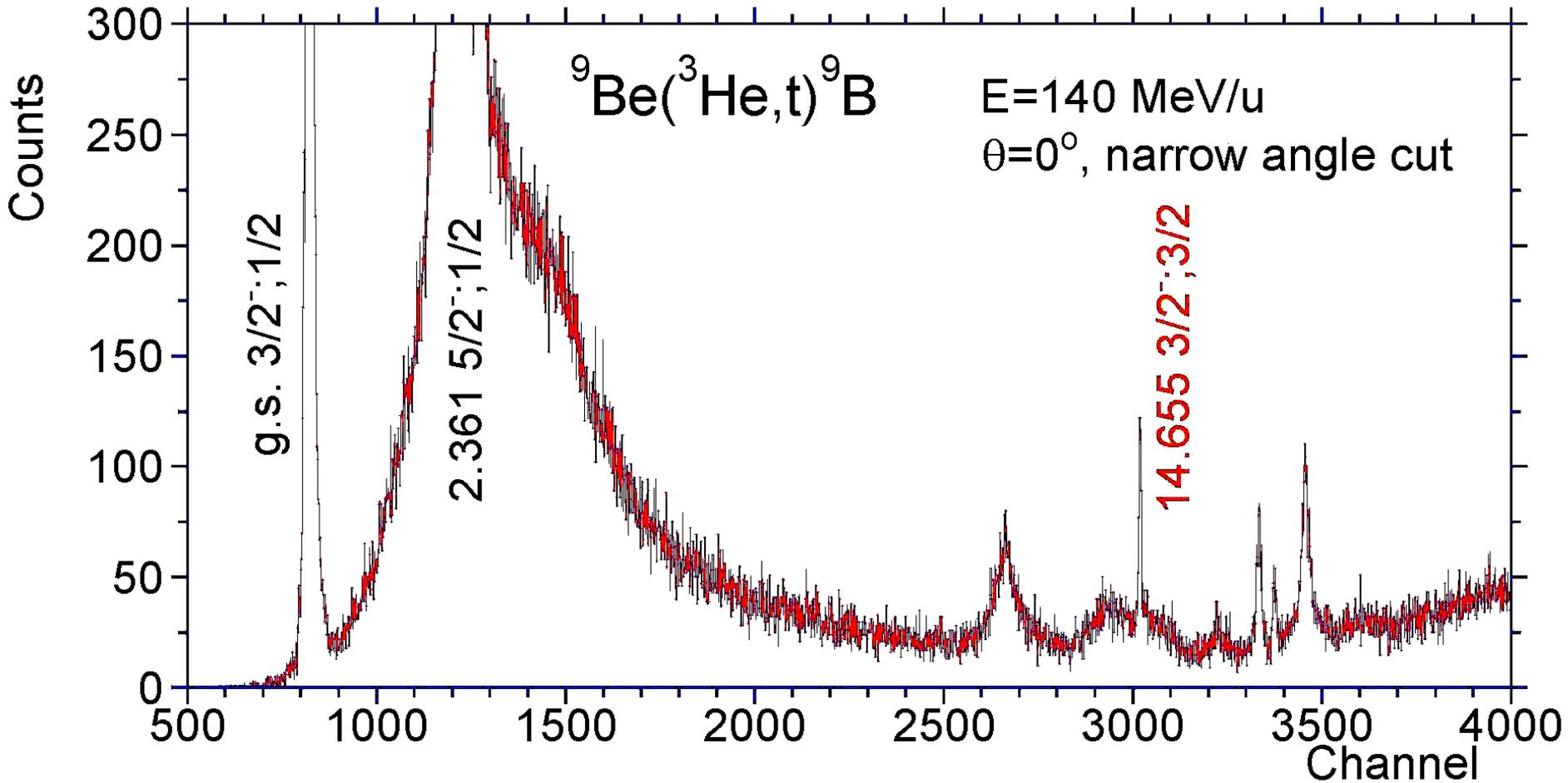
for $T = 0, 1$ states : $E_x = 6.31$ MeV

for $T = 2$ states : $E_x = 14.1$ MeV

${}^9\text{Be}({}^3\text{He},t){}^9\text{B}$ spectrum (I)

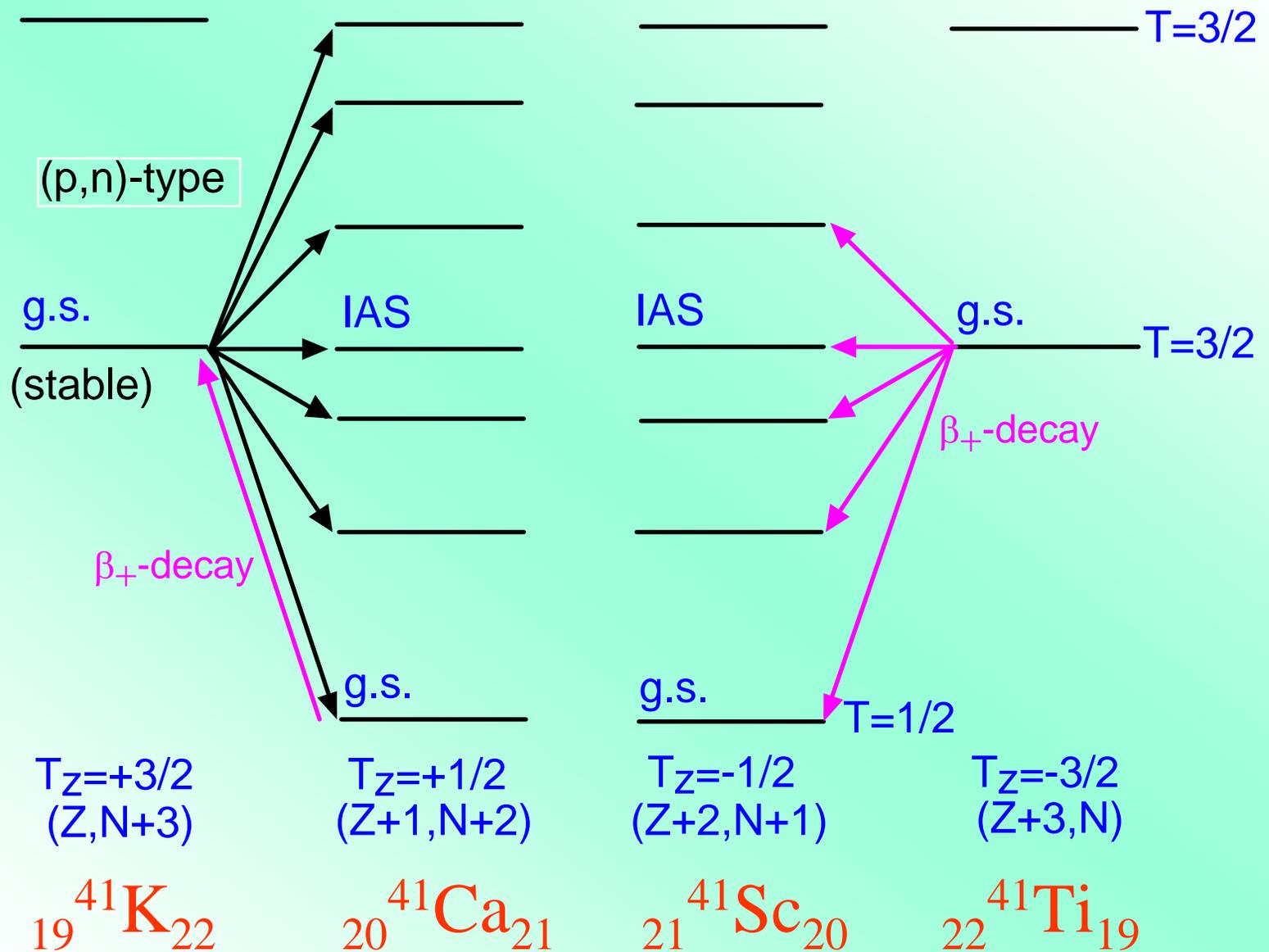


${}^9\text{Be}({}^3\text{He},t){}^9\text{B}$ spectrum (II) x50

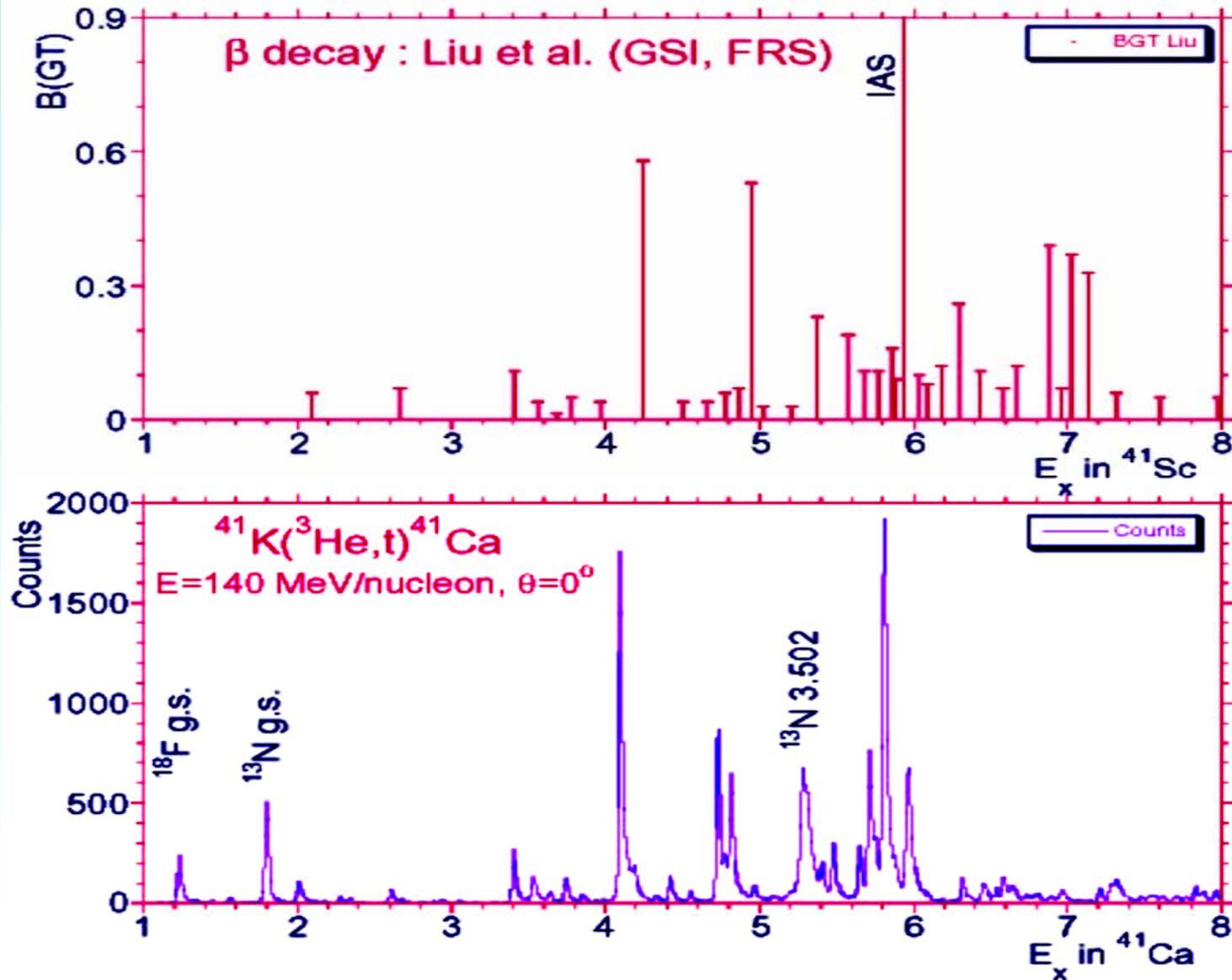


Isospin selection rule allows no particle decay of $T_>$ state

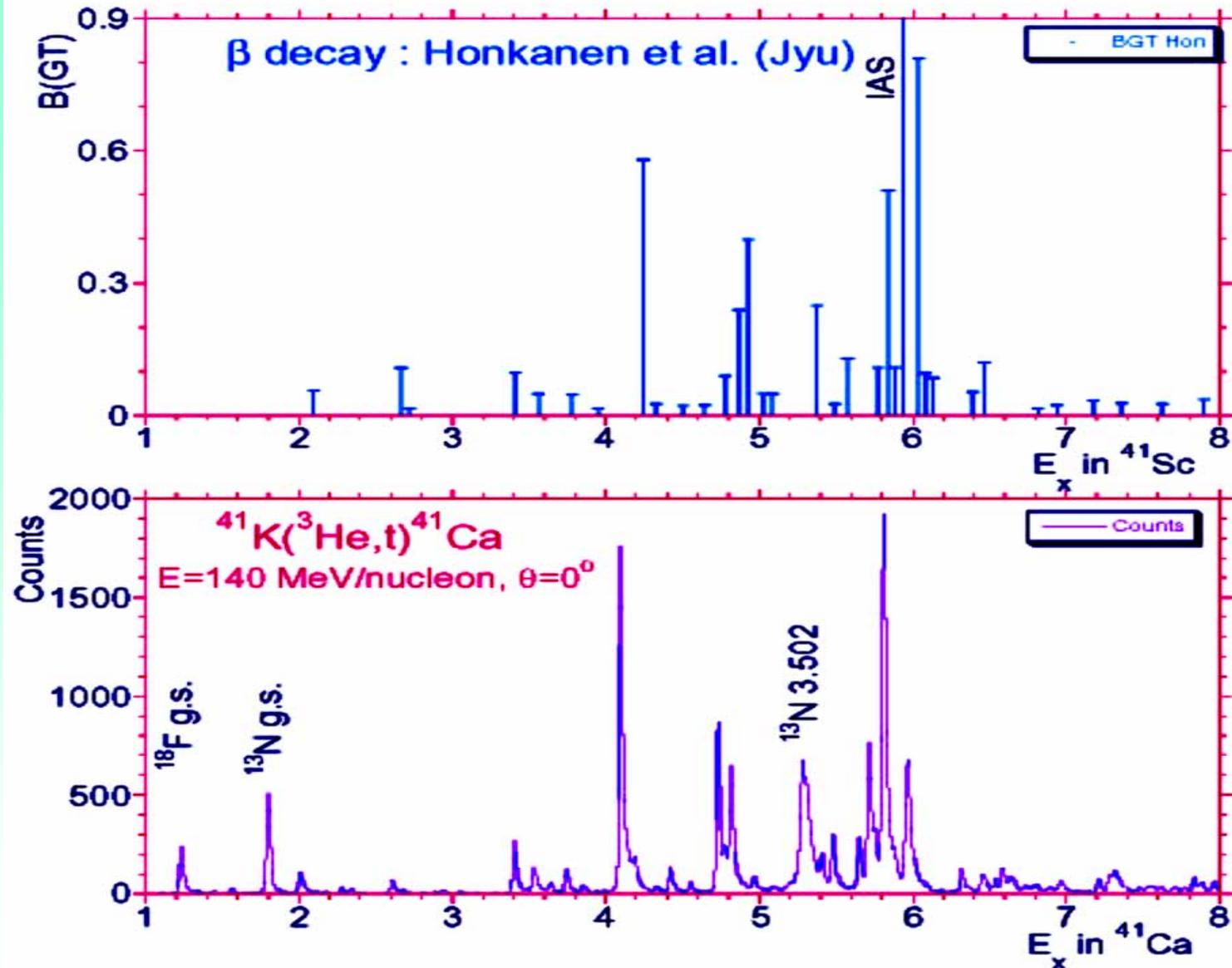
T=3/2 system: structures & transitions



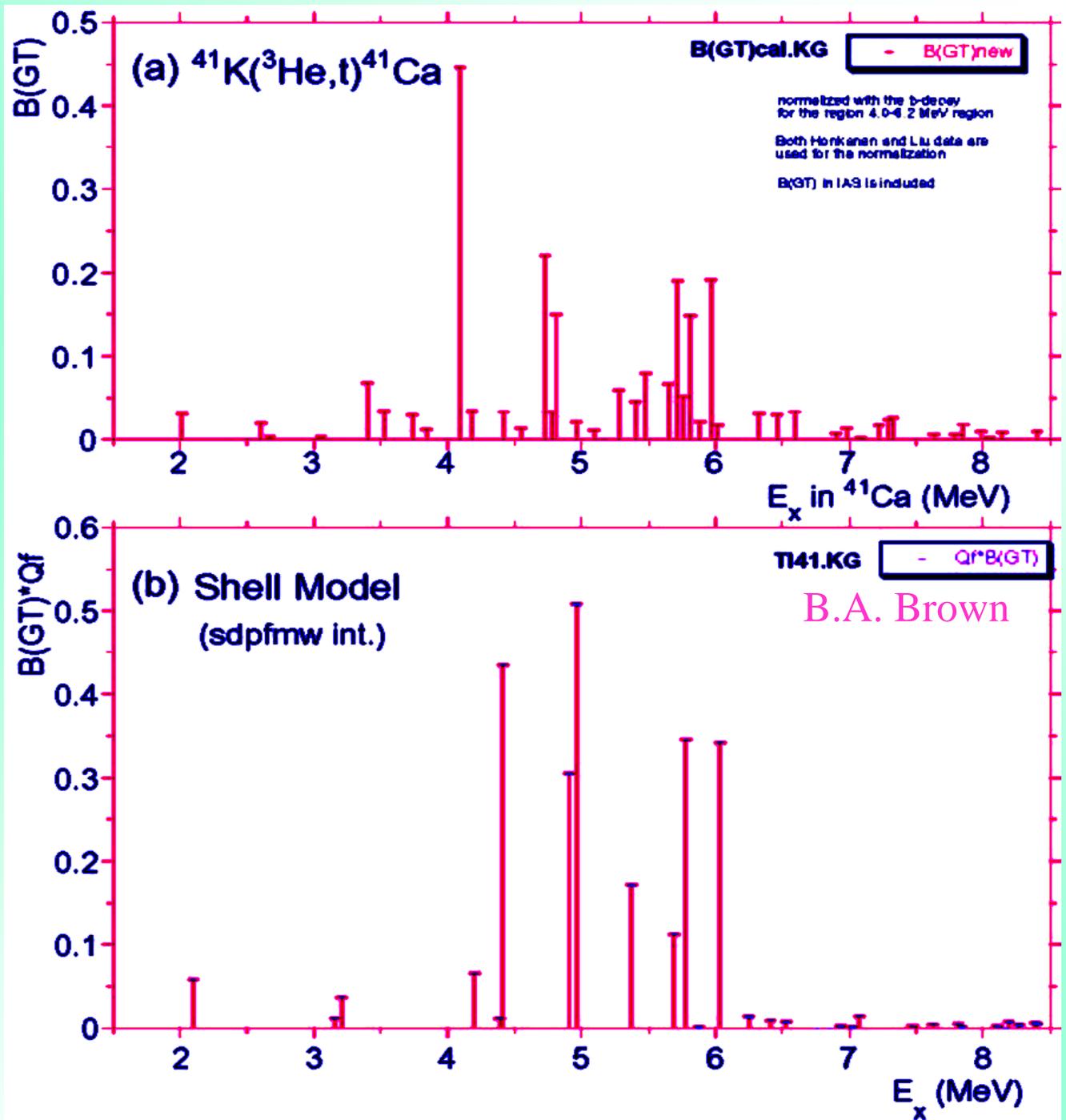
Comparison with $^{41}\text{K}(^3\text{He},t)^{41}\text{Ca}$ (I)



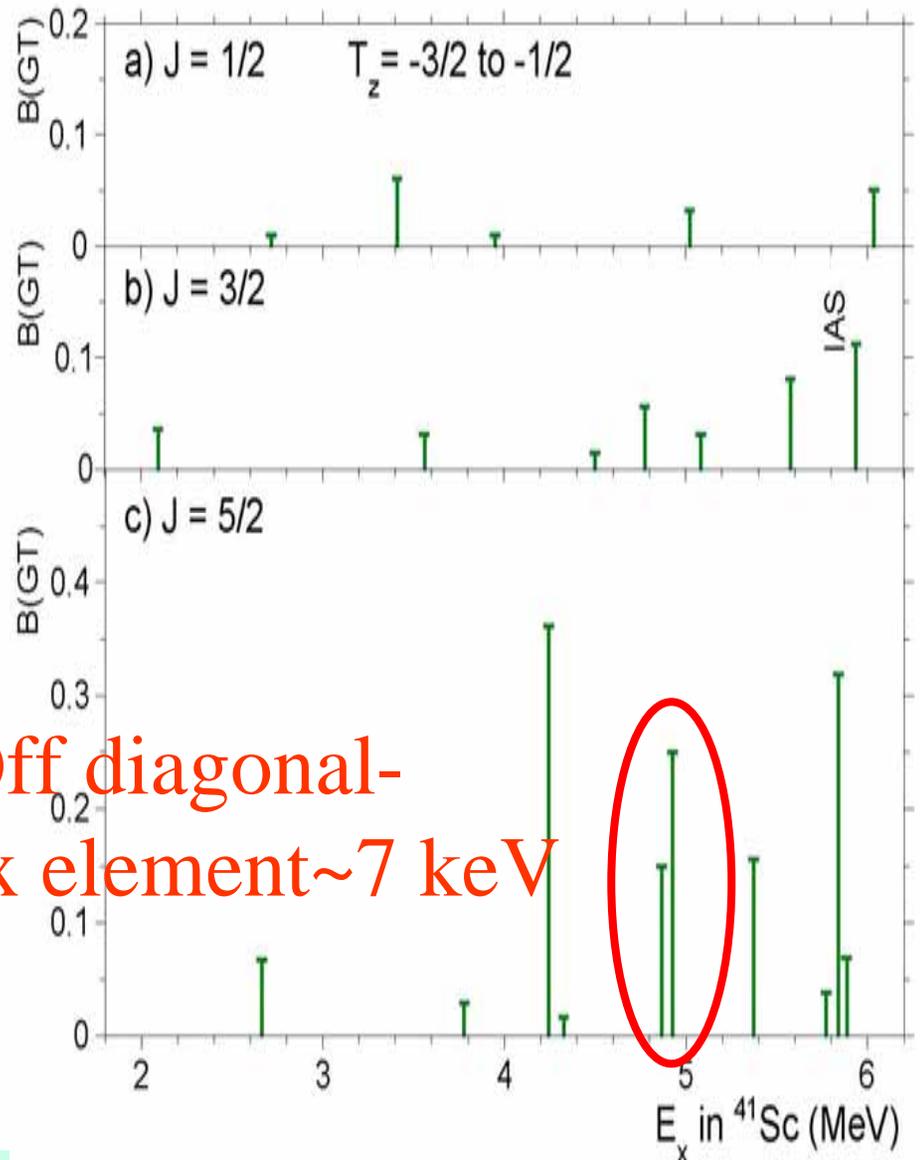
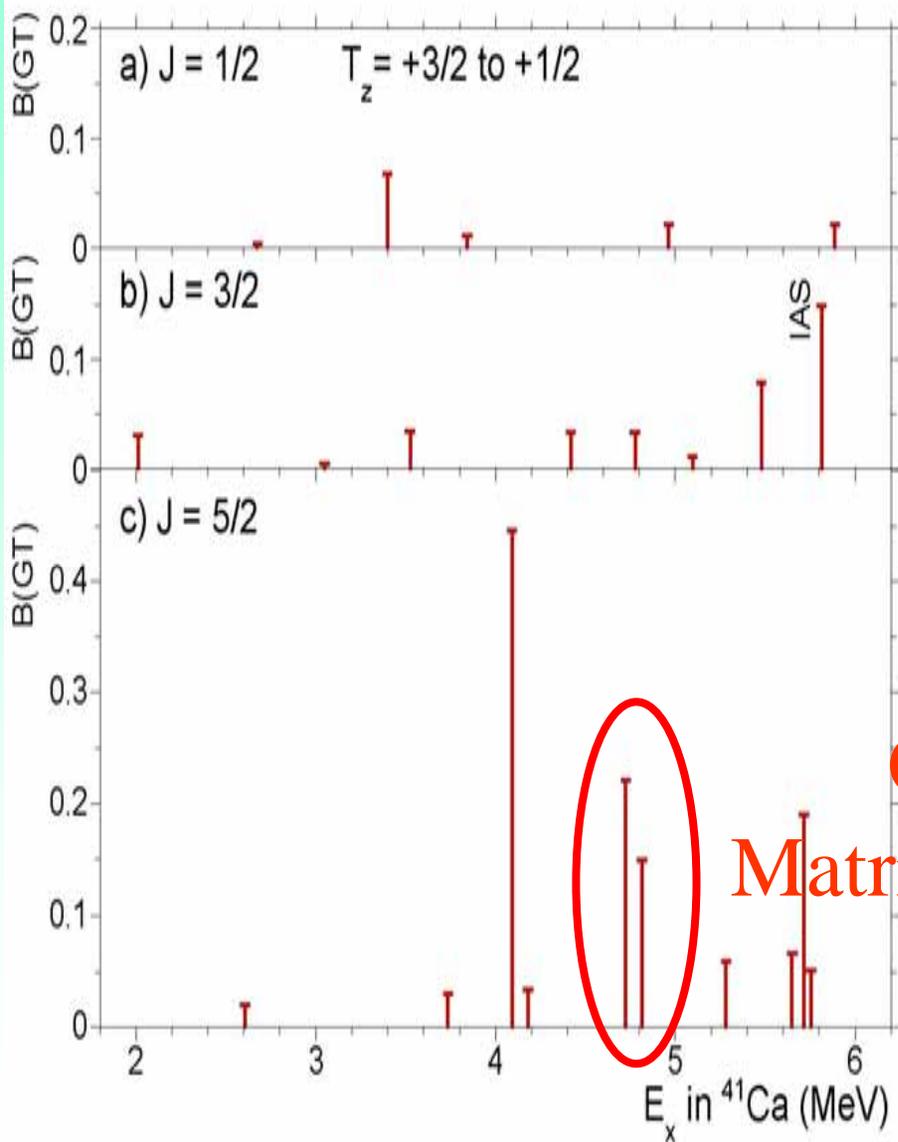
Comparison with $^{41}\text{K}(^3\text{He},t)^{41}\text{Ca}$ (II)



Comparison: $^{41}\text{K}(^3\text{He},t)^{41}\text{Ca}$ & Shell Model



Reversed Strength in $T_z = \pm 1/2$



Off diagonal-
Matrix element ~ 7 keV

(p, n) spectra for $A > 90$ Nuclei

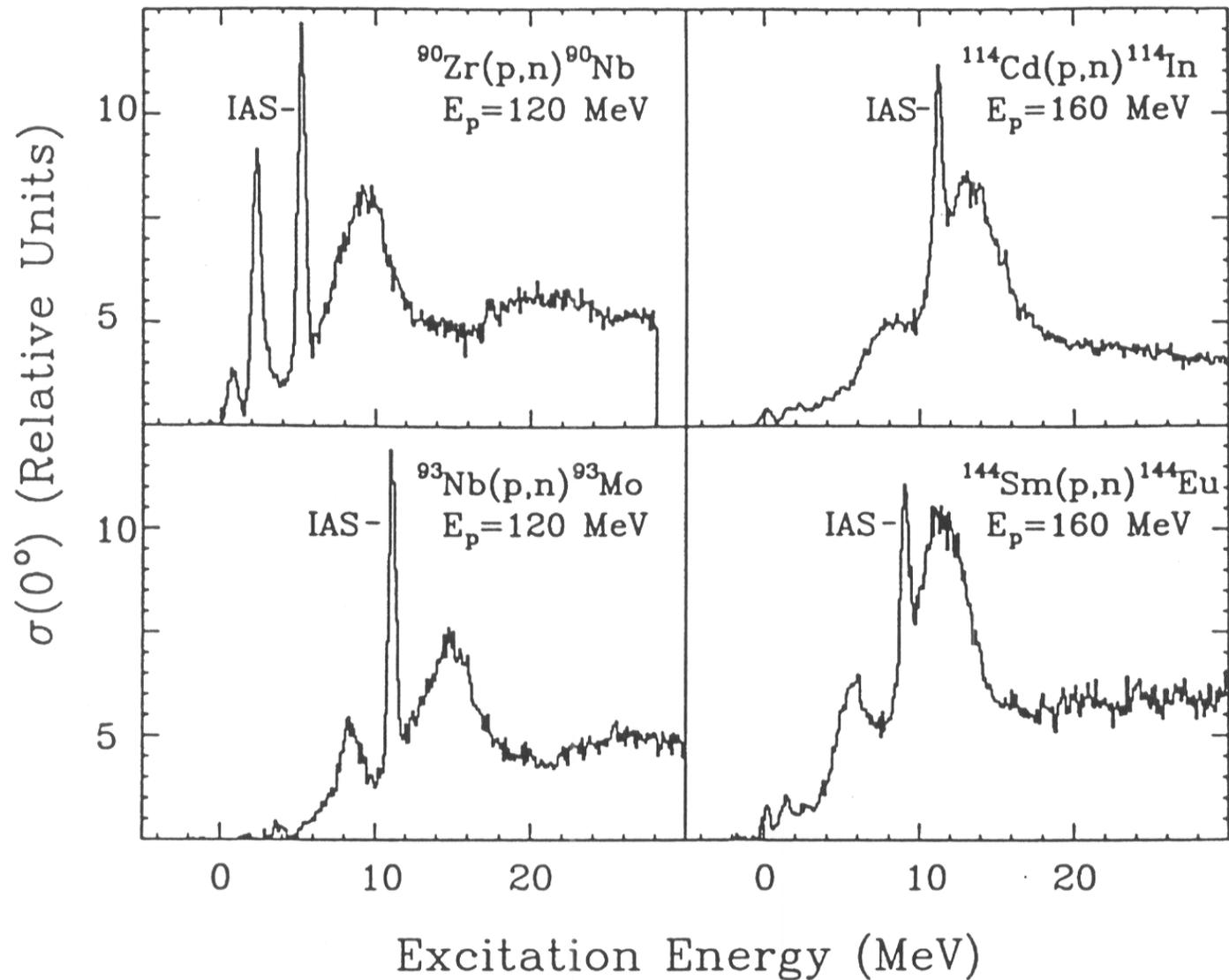
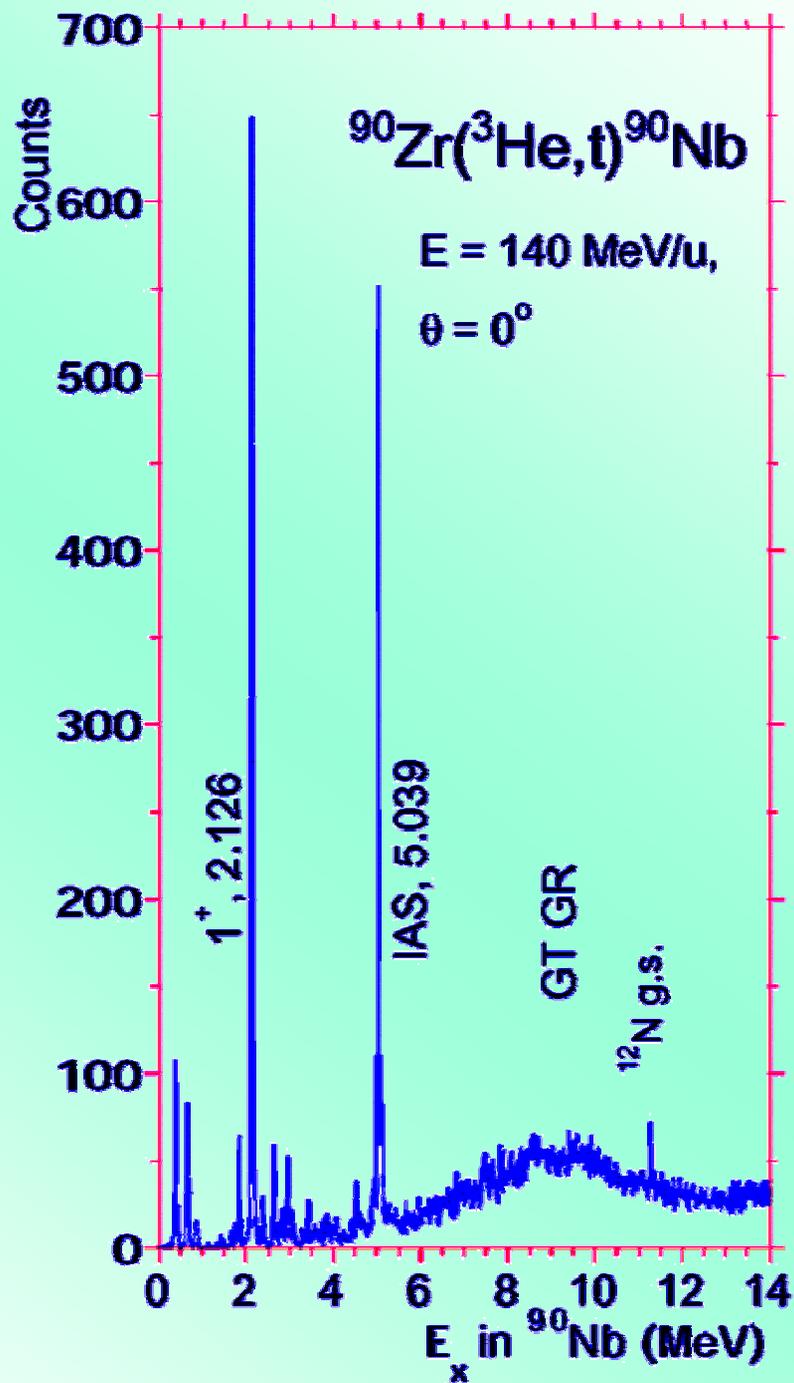
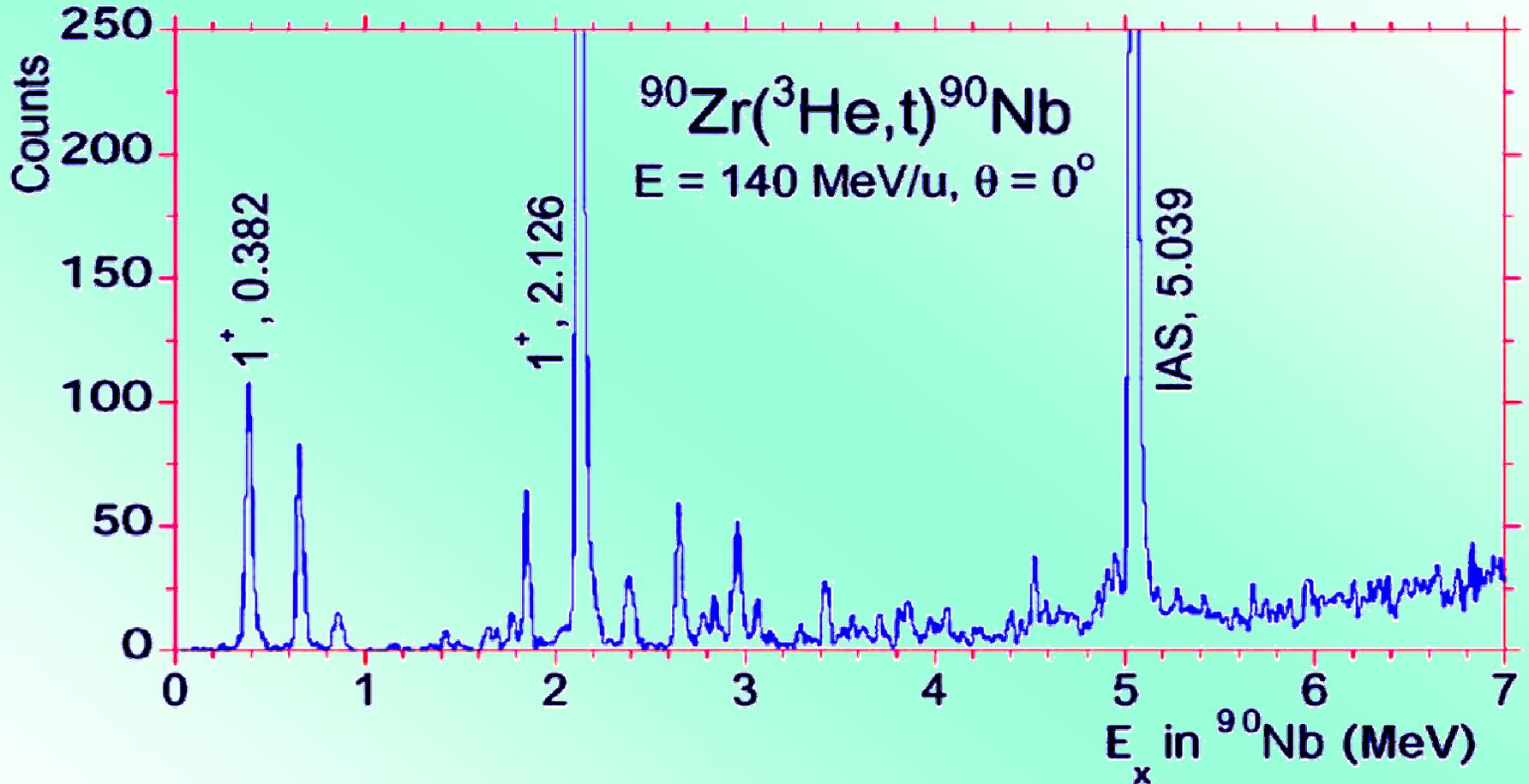


Figure 10 Zero-degree (p, n) spectra for medium A -mass nuclei at the indicated incident energies.

Discrete States
and
GT GR
in ^{90}Nb (II)

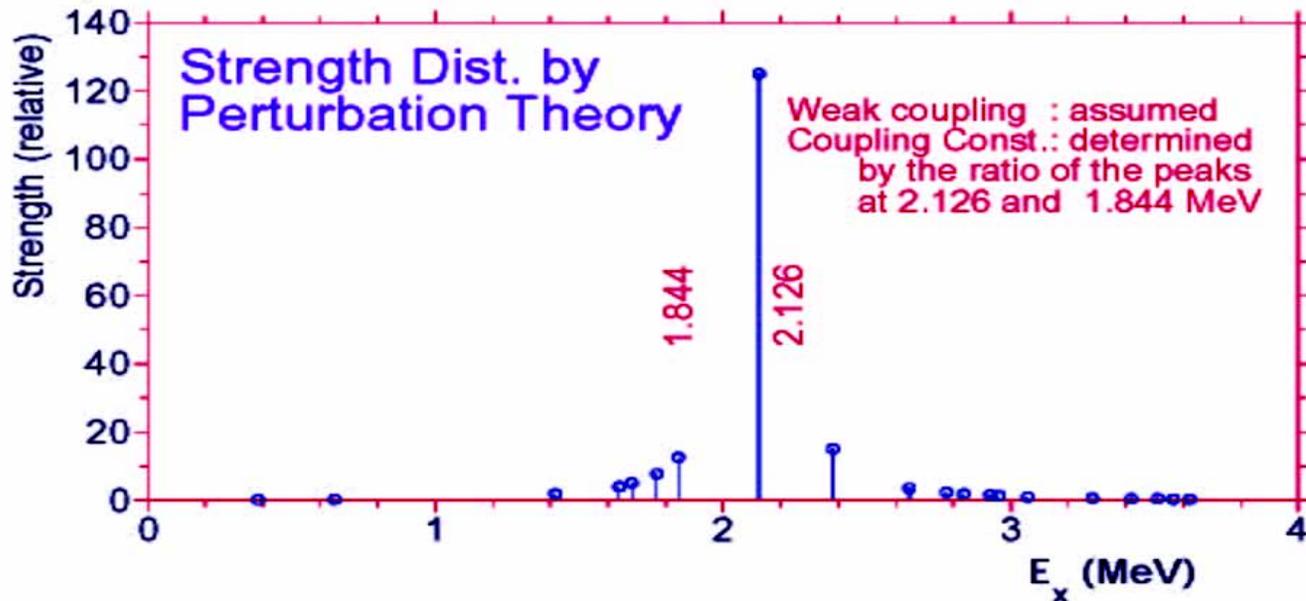
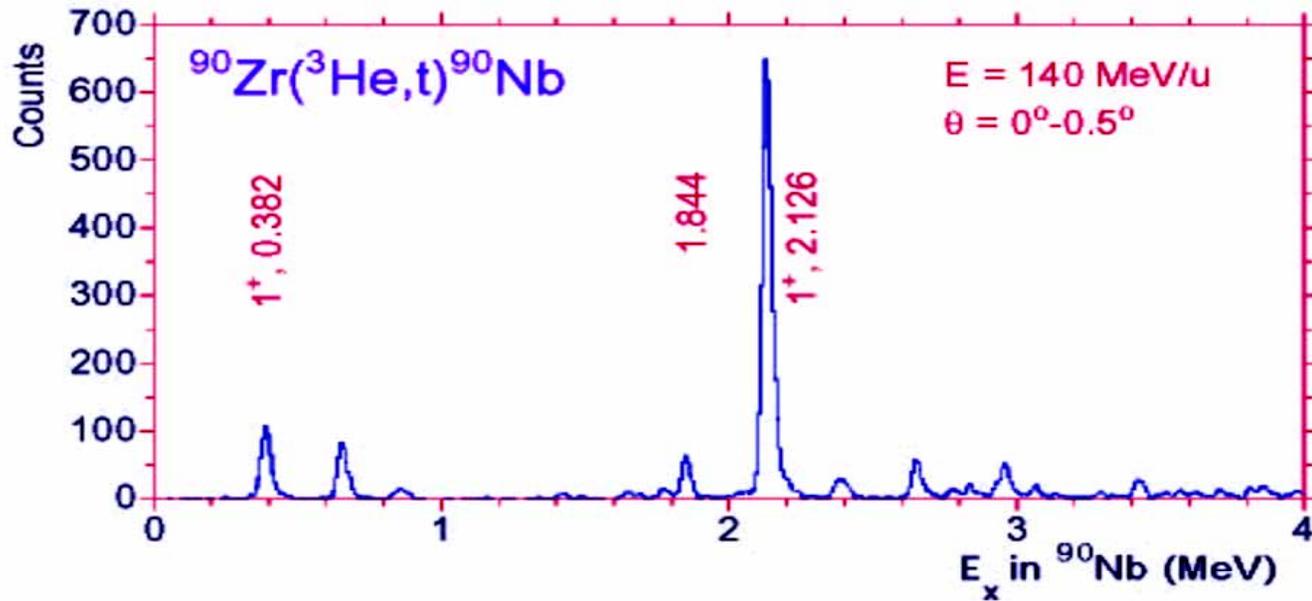


Fragmented low-lying states in ^{90}Nb



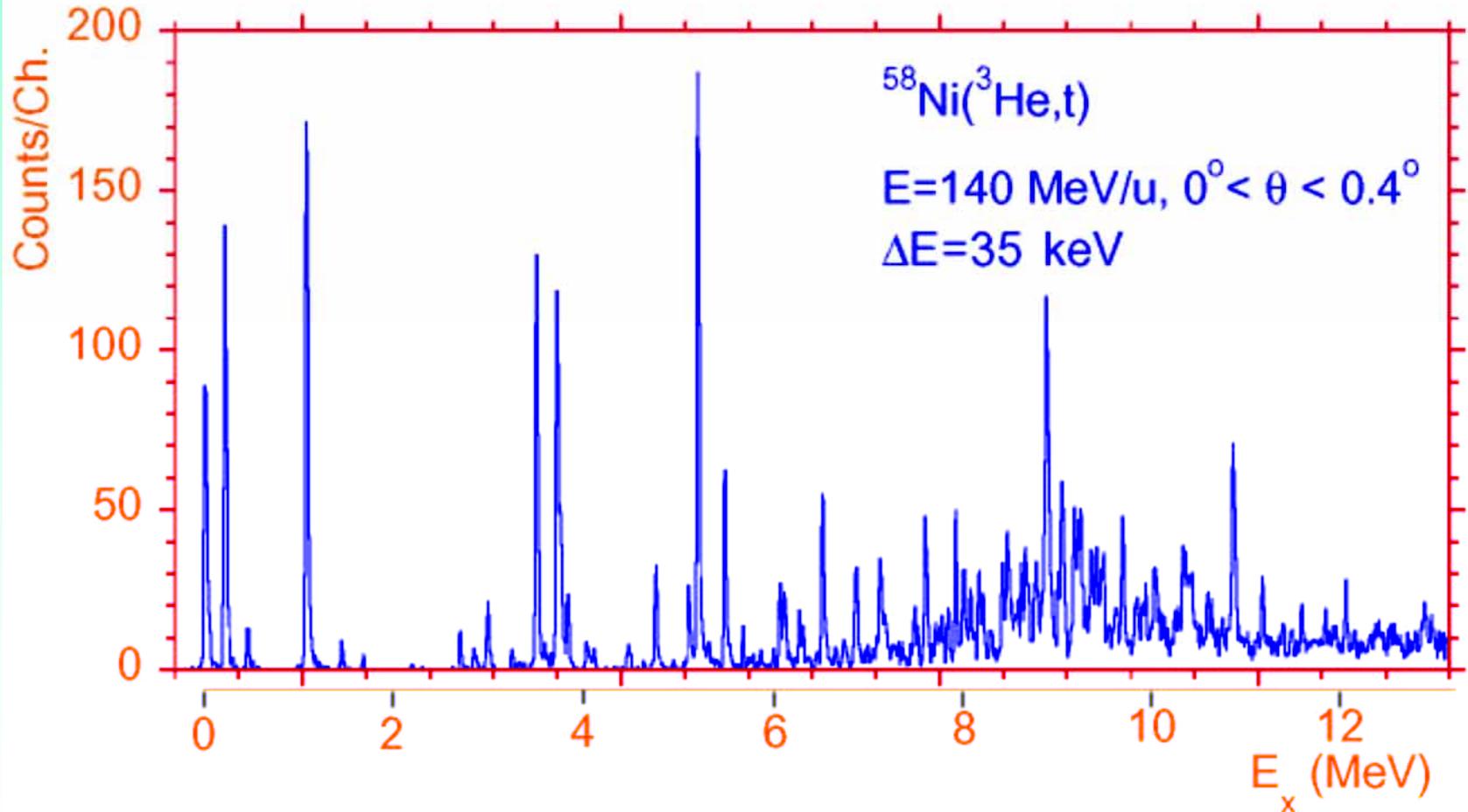
$S_p = 5.08 \text{ MeV}$

Strengths: Exp. & Perturbation Th.



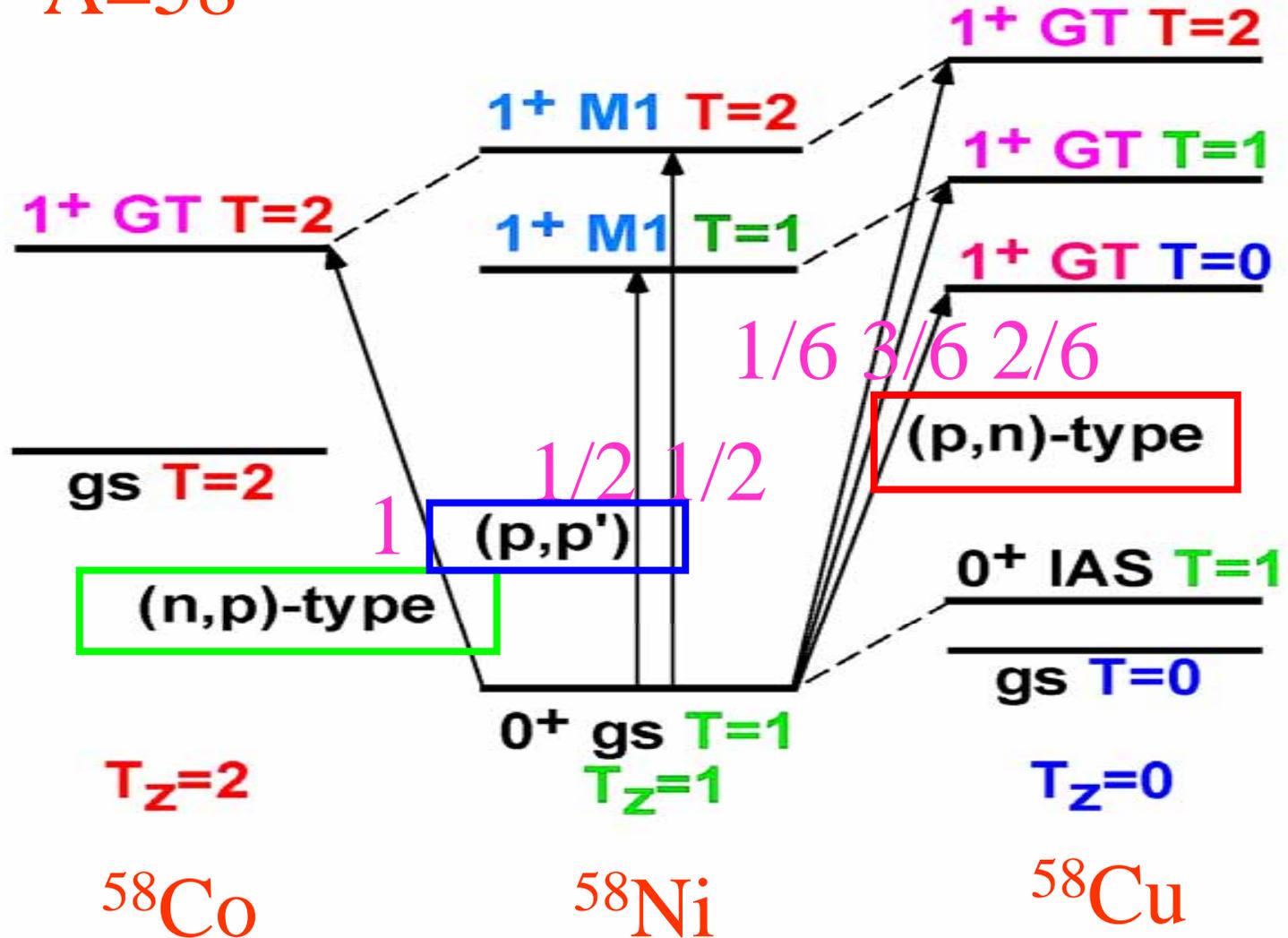
High resolution ($^3\text{He},t$) spectrum

H. Fujita PhD thesis

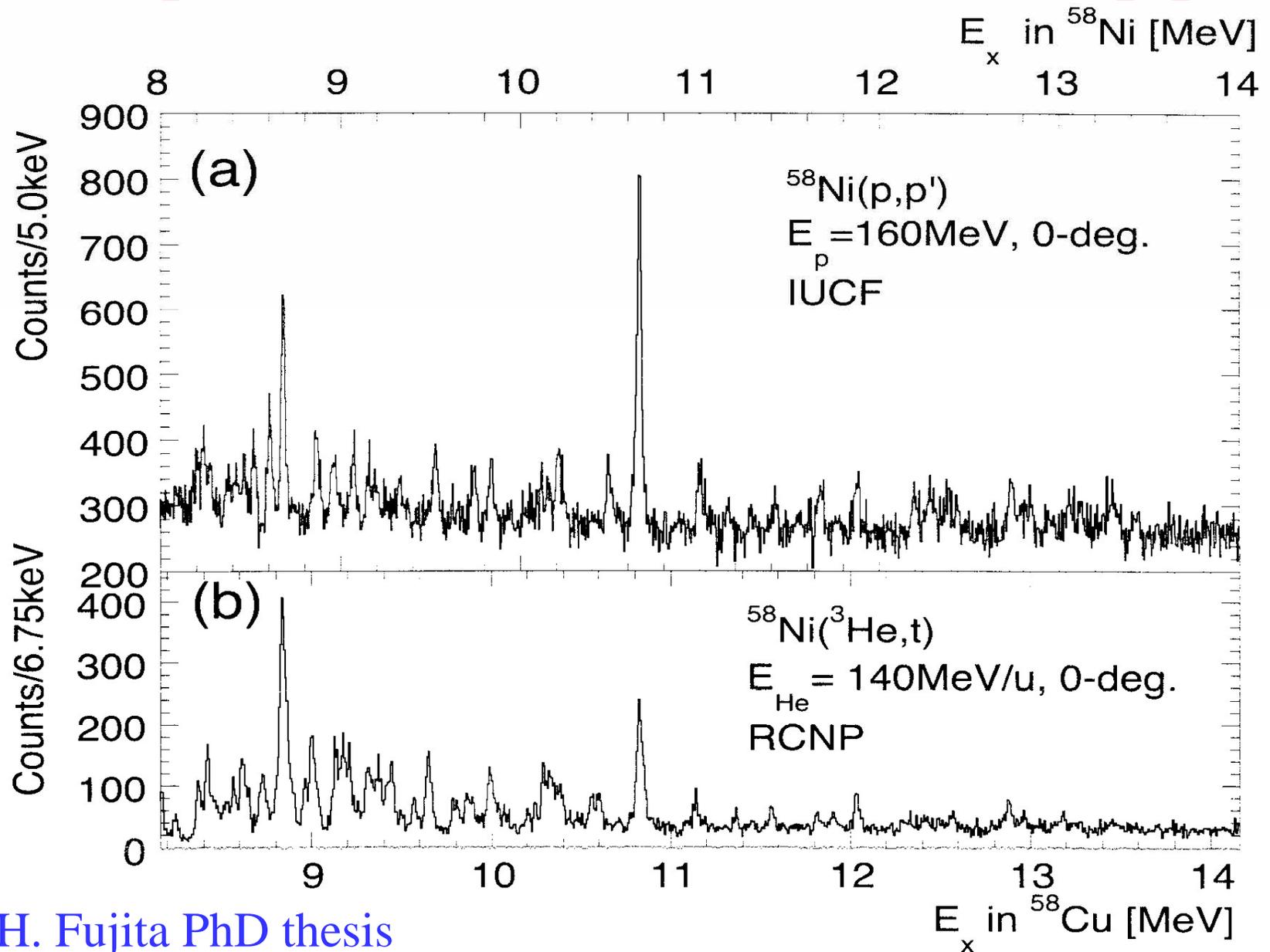


Isospin symmetry structure & $\sigma\tau$ operator

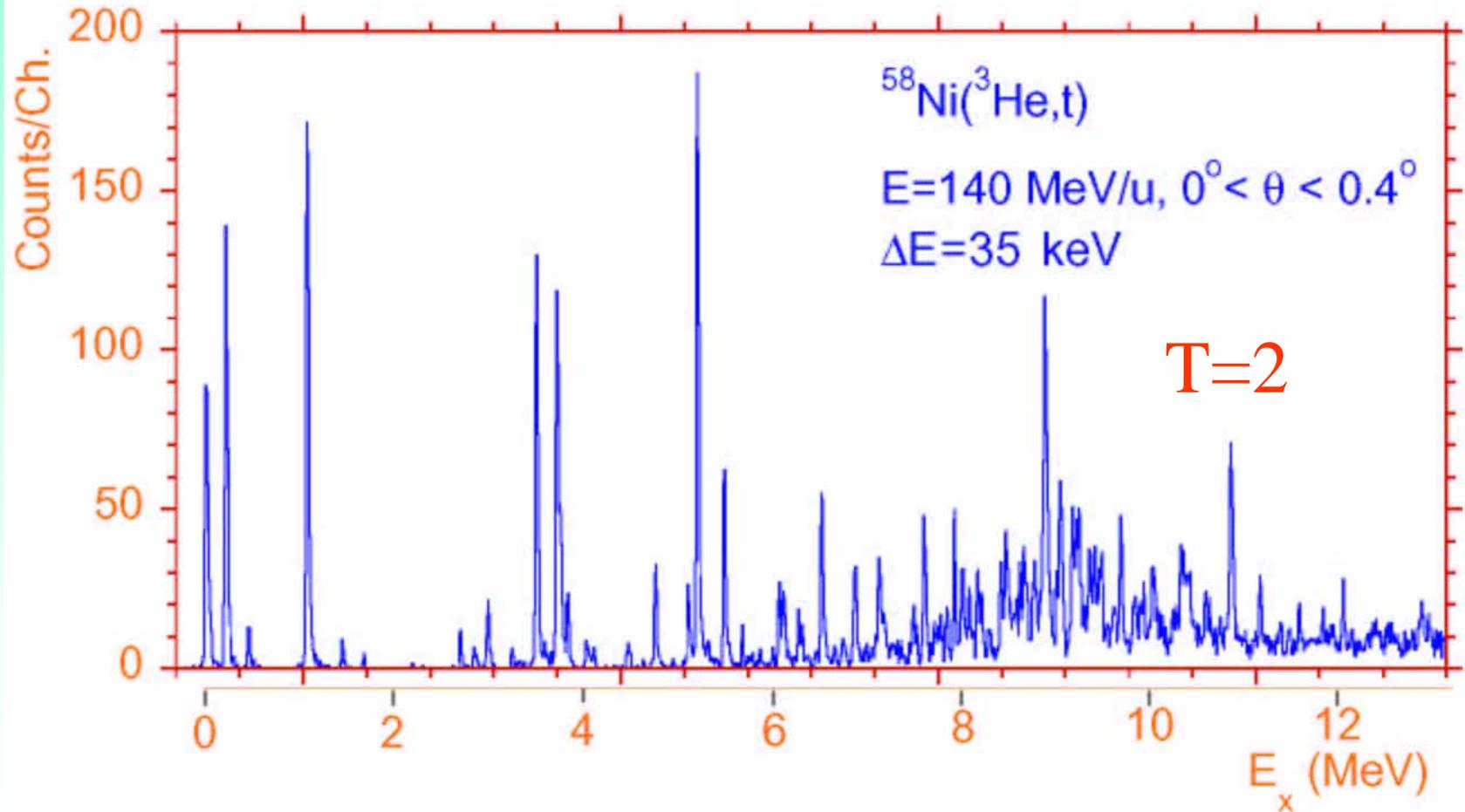
$A=58$



Comparison: $^{58}\text{Ni}(^3\text{He},t)^{58}\text{Cu}$ & $^{58}\text{Ni}(p,p')$

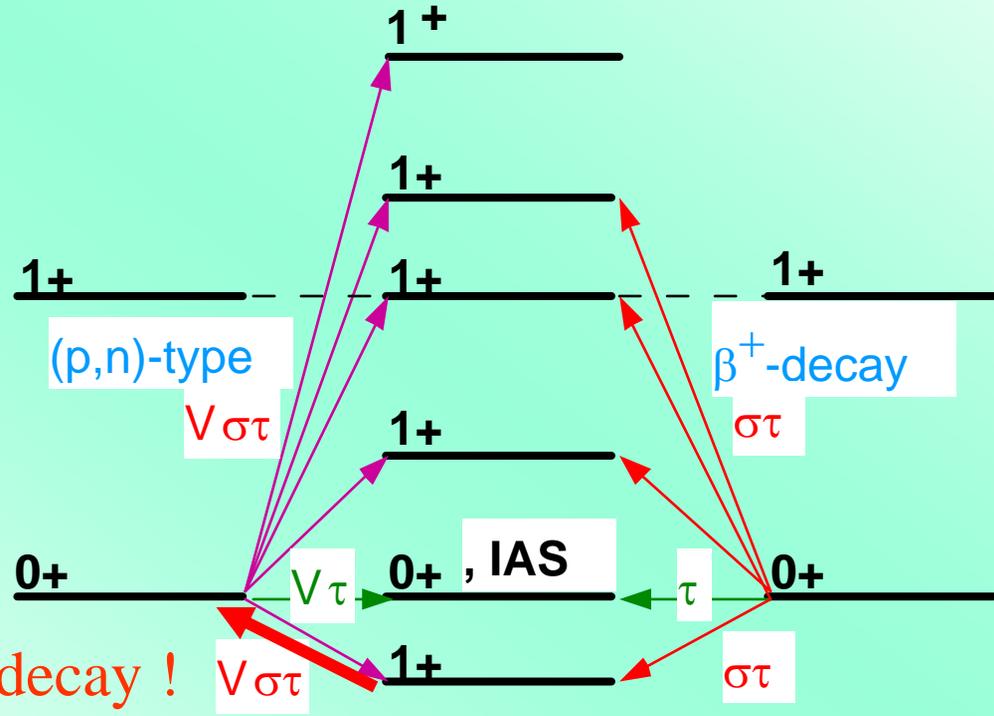


High resolution $^{58}\text{Ni}(^3\text{He},t)^{58}\text{Cu}$ spectrum



A=58, T=1 symmetry : Structures & Transitions

$T_z=+1 \quad \longrightarrow \quad T_z=0 \quad \longleftarrow \quad T_z=-1$
 (in isospin symmetry space*)



known from β decay !

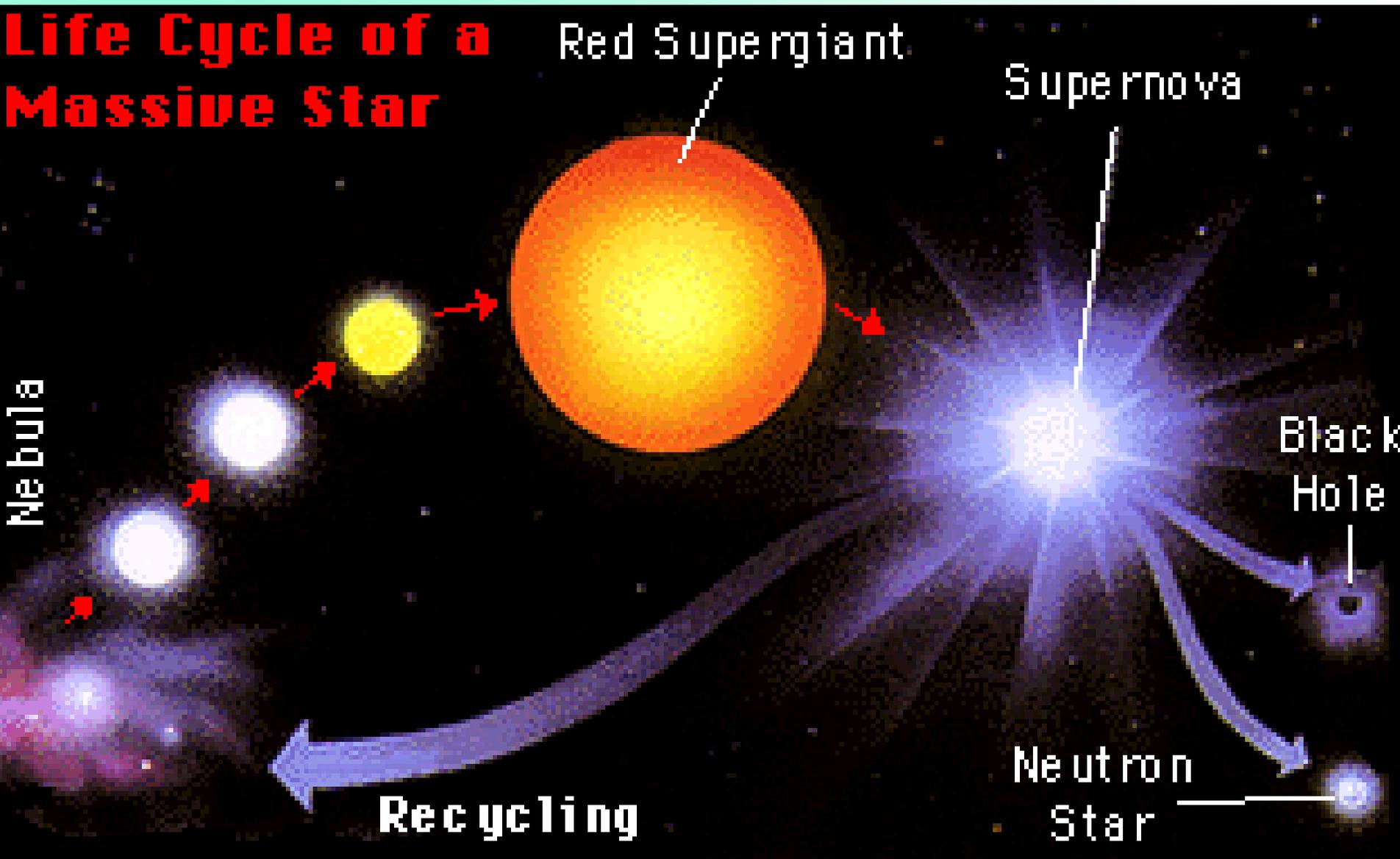
$T_z=+1$
 ^{58}Ni

$T_z=0$
 ^{58}Cu

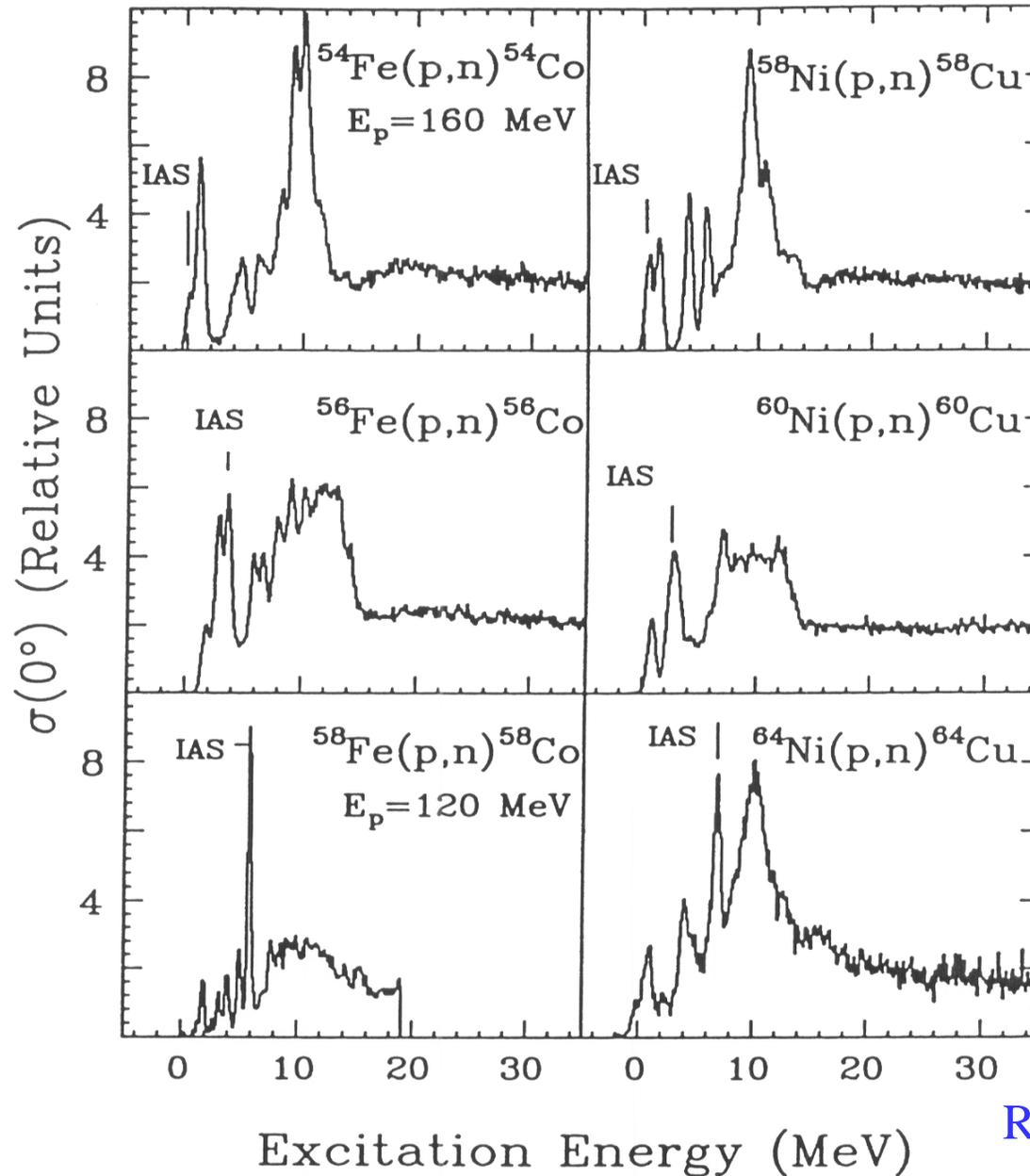
$T_z=-1$
 ^{58}Zn

Supernova Cycle

Life Cycle of a Massive Star



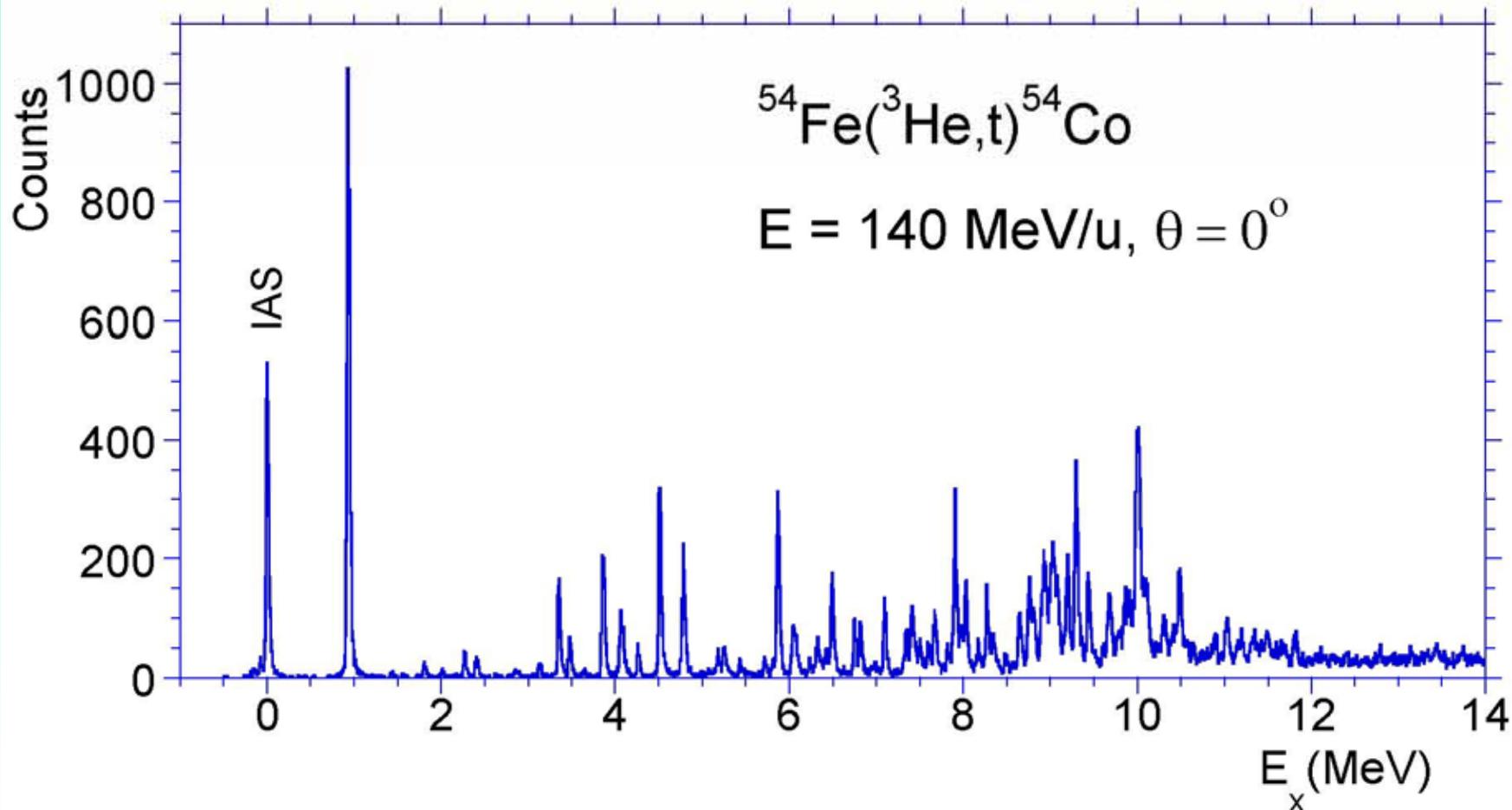
(p, n) spectra for Fe and Ni Isotopes



Rapaport
&
Sugarbaker
Rev. Mod. Phys. ('94)

High resolution $^{54}\text{Fe}(^3\text{He},t)$ spectrum

T. Adachi et al.



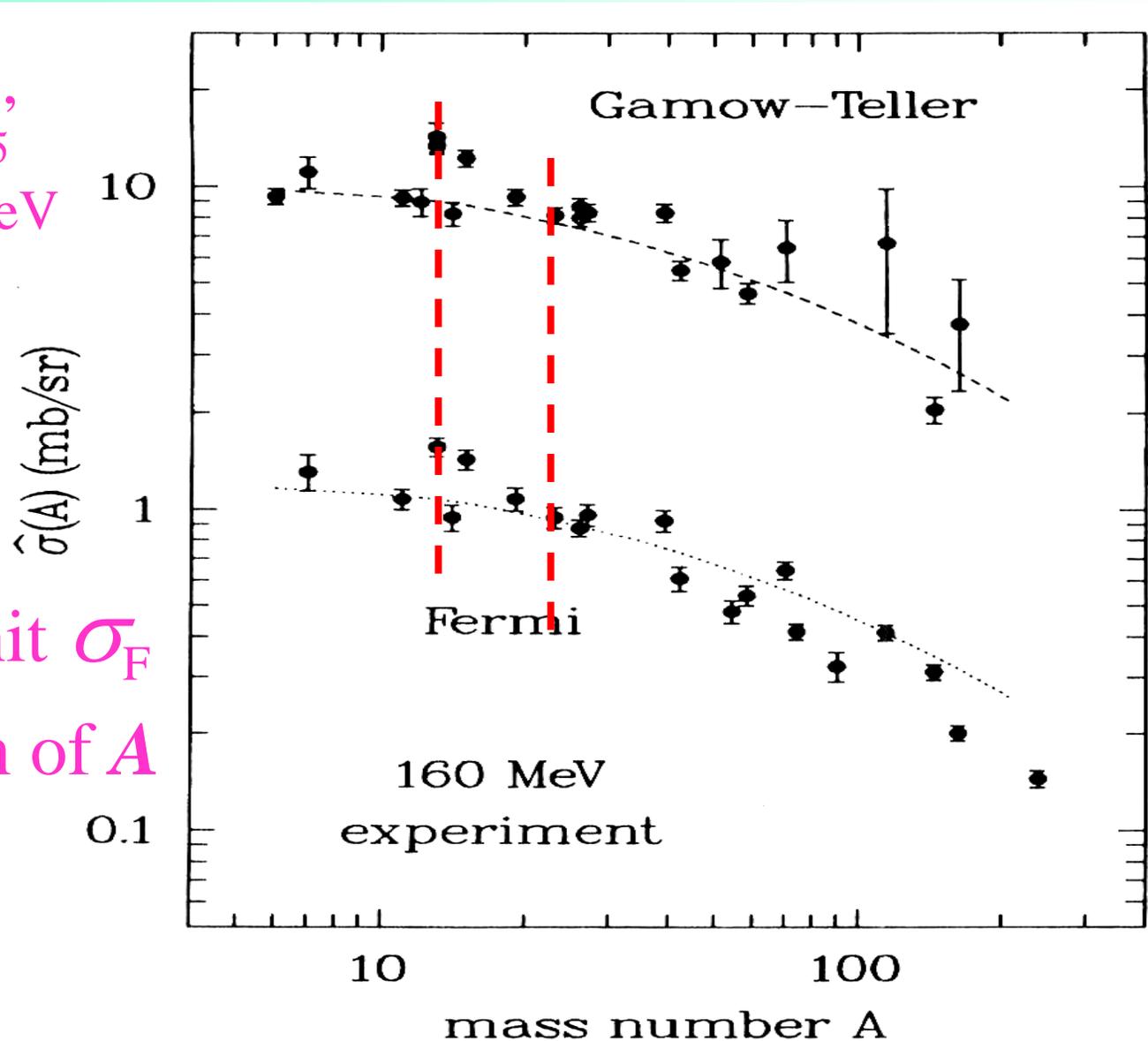
Target nuclei under study :

$T_0=1$	$^{46}\text{Ti}, ^{50}\text{Cr}, ^{54}\text{Fe}, ^{58}\text{Ni}$
$T_0=2$	$^{48}\text{Ti}, ^{52}\text{Cr}, ^{56}\text{Fe}, ^{60}\text{Ni}$
$T_0=3$	$^{50}\text{Ti}, ^{62}\text{Ni}$

GT & Fermi : unit cross sections in (p,n)

Taddeucci *et al.*,
N.P. A469 (1987) 125
survey at $E_p=160$ MeV

$R^2 = \text{unit } \sigma_{GT} / \text{unit } \sigma_F$
smooth function of A



Unit σ and R^2

$$\sigma_{GT}(0^\circ) = KN_{\sigma\tau} |J_{\sigma\tau}(0^\circ)|^2 B(GT)$$

$$\sigma_F(0^\circ) = KN_\tau |J_\tau(0^\circ)|^2 B(F)$$

define

$$R^2 = \text{unit } \sigma_{GT}(0^\circ) / \text{unit } \sigma_F(0^\circ),$$

where

$$\text{unit } \sigma_{GT}(0^\circ) = \sigma_{GT}(0^\circ) / B(GT)$$

$$\text{unit } \sigma_F(0^\circ) = \sigma_F(0^\circ) / B(F) = N - Z$$

trick

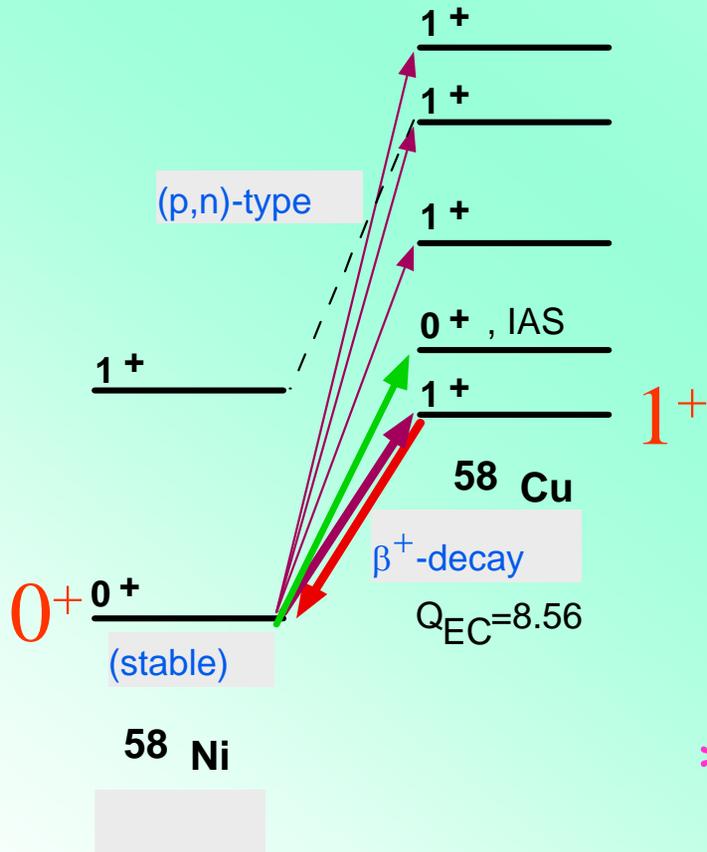
Fermi strength concentrates in the IAS

$$B(F) = N - Z$$

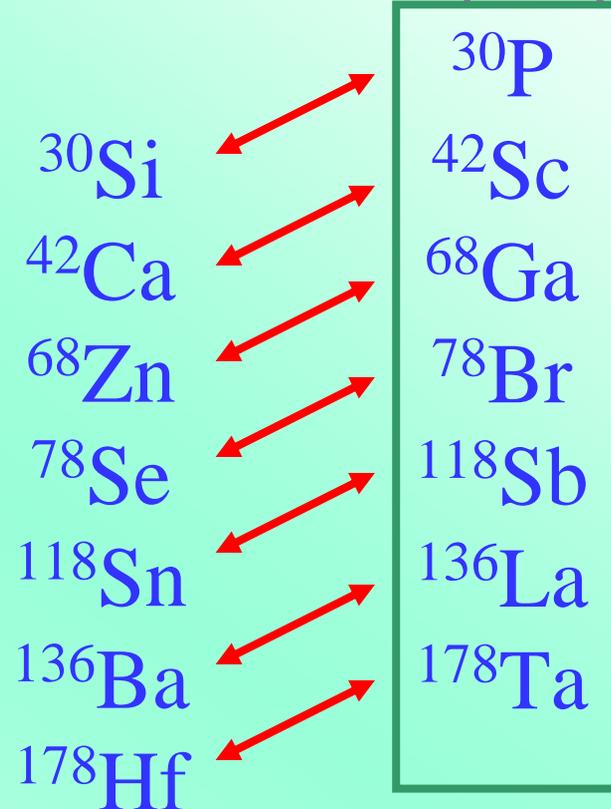
Systematics of R^2 value ?

Connection between Charge Exchange & β decay

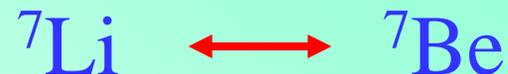
0^+ & 1^+ relationship
in $A=58$ Nuclei
(in real energy space)



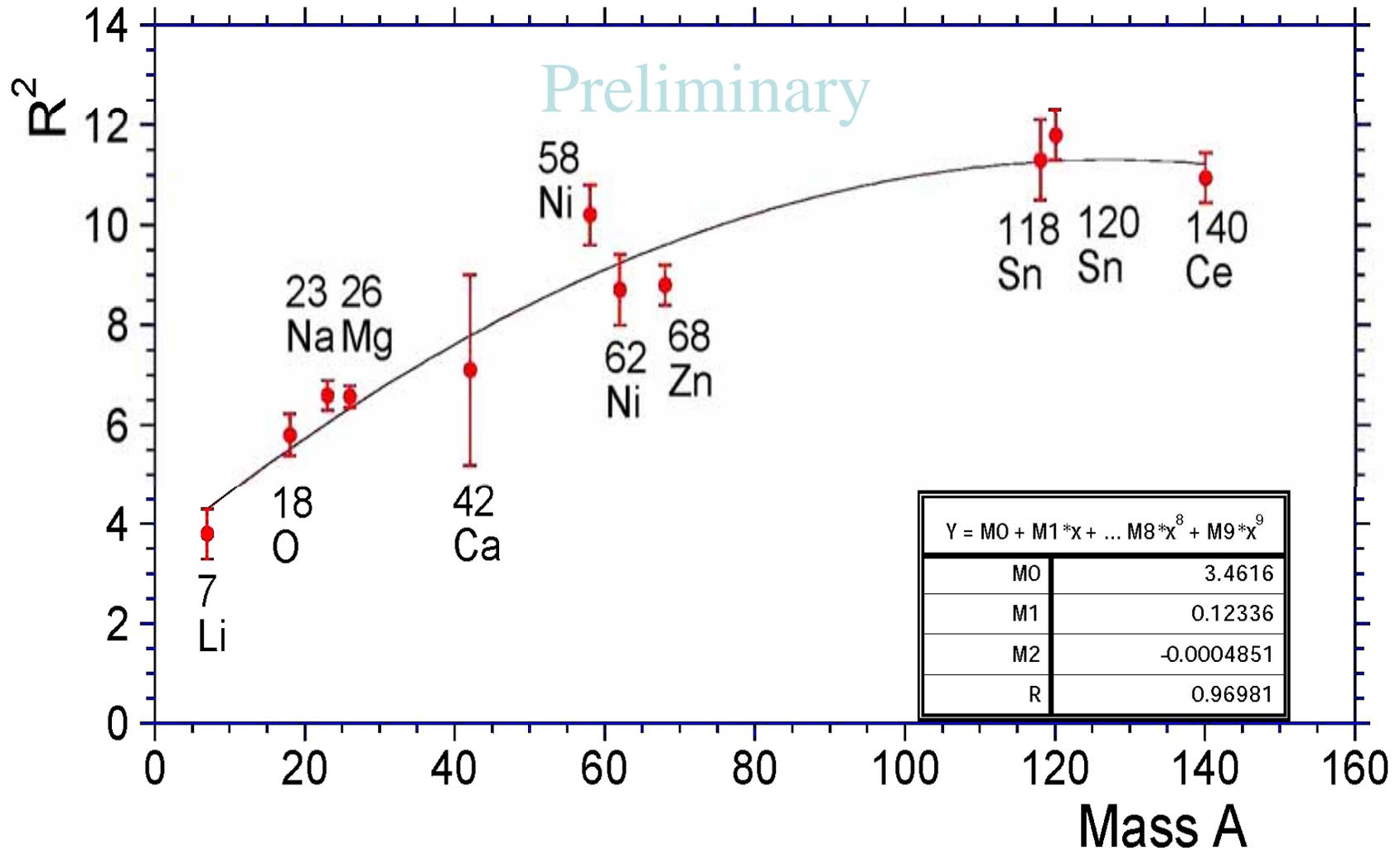
* 0^+ & 1^+ relationship of g.s.



* $T_z=1/2$ nucleus : ^7Li 1^+ g.s.



$$R^2 (= \text{unit } \sigma_{GT} / \text{unit } \sigma_F)$$



Perspective

Accelerator : underway for improvement

smaller beam emittance,
better beam energy resolution

As a Result:

smaller beam size

- smaller background
- good chance for (p, p') at 0°
 - $M1$ and $E1$ response

better energy resolution

- even better spectrum resolution
- smaller beam spot size
 - angular distribution measurement

High-Resolution Collaborations

TU Darmstadt (Germany) : (e, e'), (^3He , t), (p, p')

Gent (Belgium) : (^3He , t), (d, ^2He), (γ , γ')

GSI, Darmstadt (Germany) : inverse kinematics

ISOLDE, CERN (Switzerland) : β decay

iThemba LABS. (South Africa) : (p, p'), (^3He , t)

Jyvaskyla (Finland) : β decay

Koeln (Germany) : γ decay, (^3He , t)

KVI, Groningen (The Netherlands) : (d, ^2He)

LTH, Lund (Sweden)

Valencia (Spain) : β decay

Michigan State University (USA) : (t, ^3He)

Muenster (Germany) : (d, ^2He)

Rosendorf (Germany) : (γ , γ')

Summary Words

High Resolution

In **Charge Exchange** and **Inelastic Reactions**

--at Intermediate Incident Energies--

(³He,t) reaction : one order better resolution than in a (p,n) reaction

(p, p') reaction : spectrum as low as $E_x=5$ MeV

Active Operators, Isospin Symmetry

Similarity of Active Operators for Analog Transitions

Gamow-Teller operator in **β decay** (weak interaction)

Spin-isospin interaction in **reactions** (strong interaction)

Spin-Isospin Responses

In Various Nuclei with High Resolution