

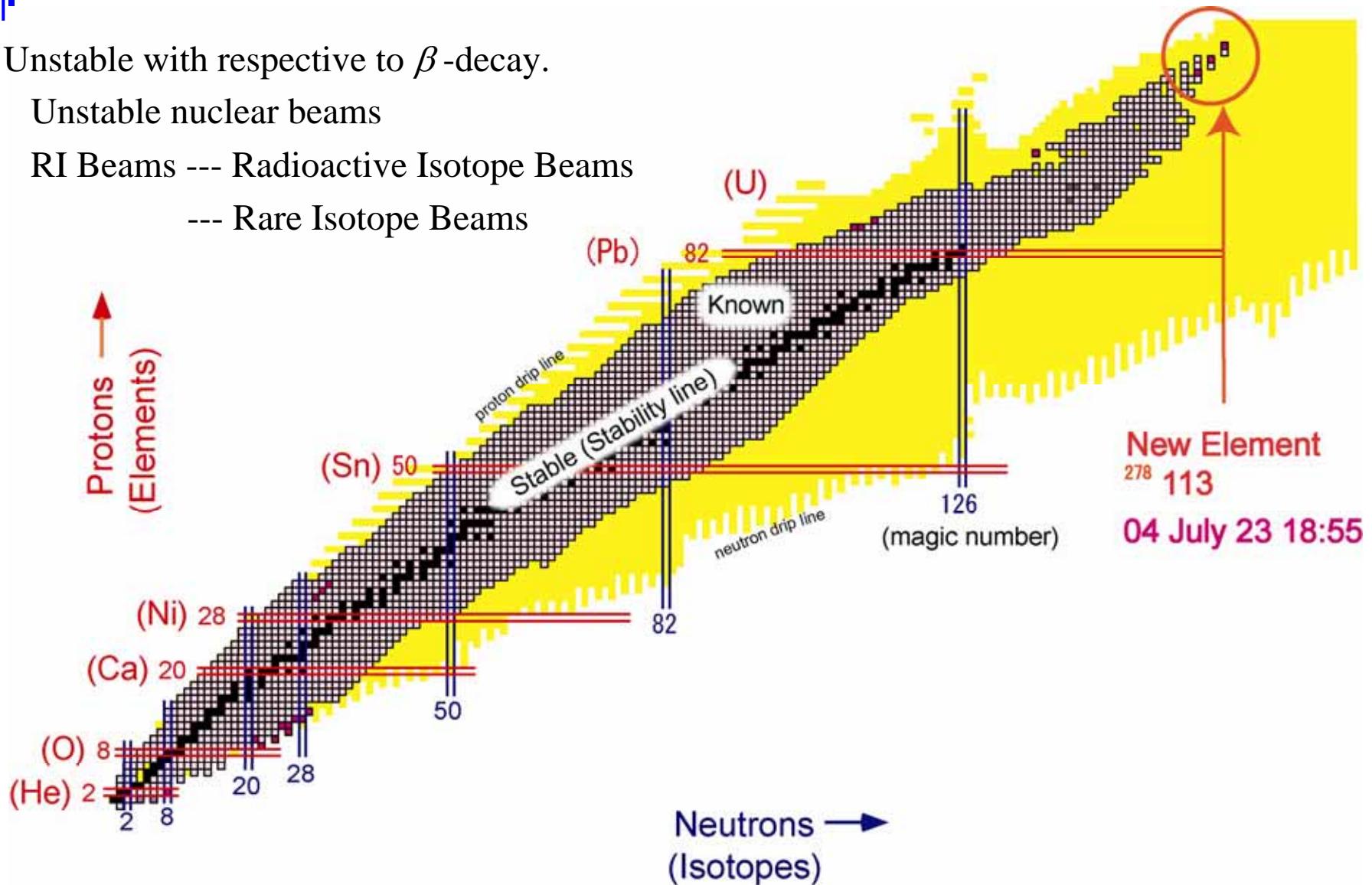


Exotic structure of unstable nuclei revealed
through a γ - ray spectroscopy technique
*--- with a emphasis on the study of
the Island of Inversion nuclei*

AOI, Nori
RIKEN

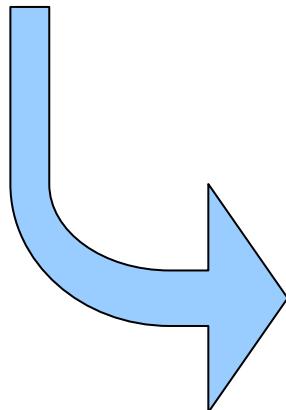
Unstable Nuclei

- Unstable with respect to β -decay.
 - Unstable nuclear beams
 - RI Beams --- Radioactive Isotope Beams
 - Rare Isotope Beams

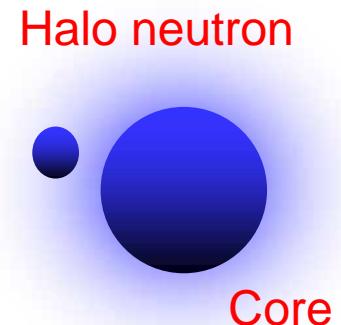


Characteristics of unstable nuclei

- Different Fermi surface of protons and neutrons
- Different single particle orbitals for valence protons and neutrons
- Different Isospin
- Weak binding
 - ⋮



- Neutron halo
- Neutron skin
- Soft E1 mode
- Modification of effective charge
- Modification of shell structure
 - Disappearances of magic number
 - New magic number
- Decoupling of Neutron and Proton distribution

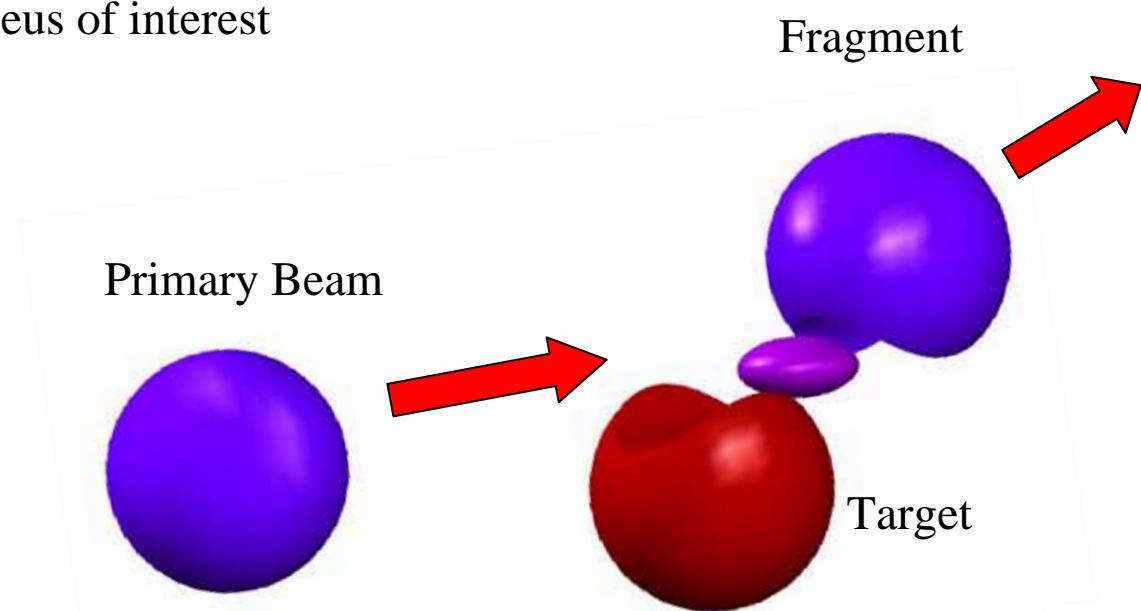


Production of Unstable Nuclear Beams

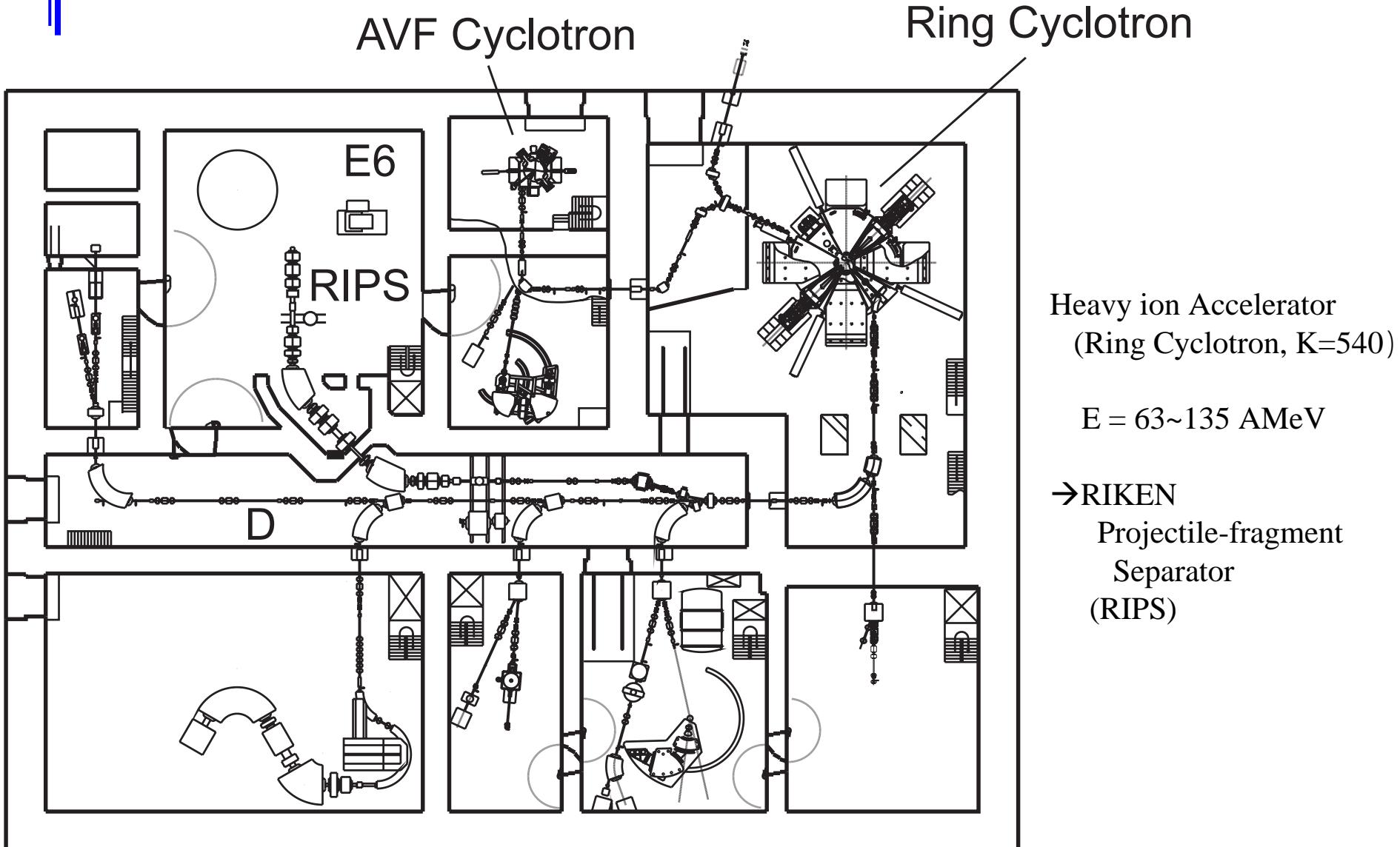
- High energy heavy ion beam
 - + Production target (eg. Be)
 $E_{\text{beam}} > \text{Fermi energy} \sim 40 \text{ MeV}$

Projectile fragmentation reaction
Various species of nuclei

- Collect and separate the nucleus of interest



RIKEN Accelerator Research Facility (RARF)



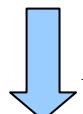
Production of Unstable Nuclear Beams

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Projectile fragmentation reaction
Various species of nuclei

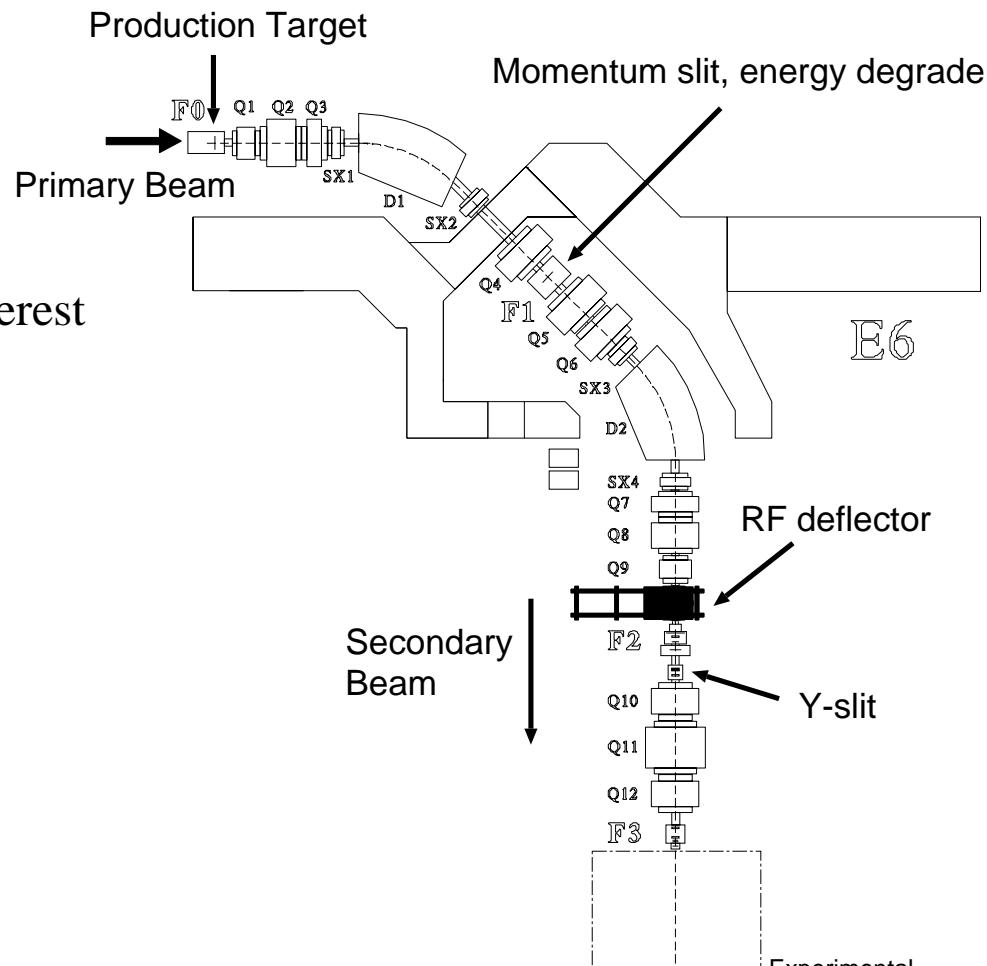
- Collect and separate the nucleus of interest

First stage : $B\rho \sim A/Z$

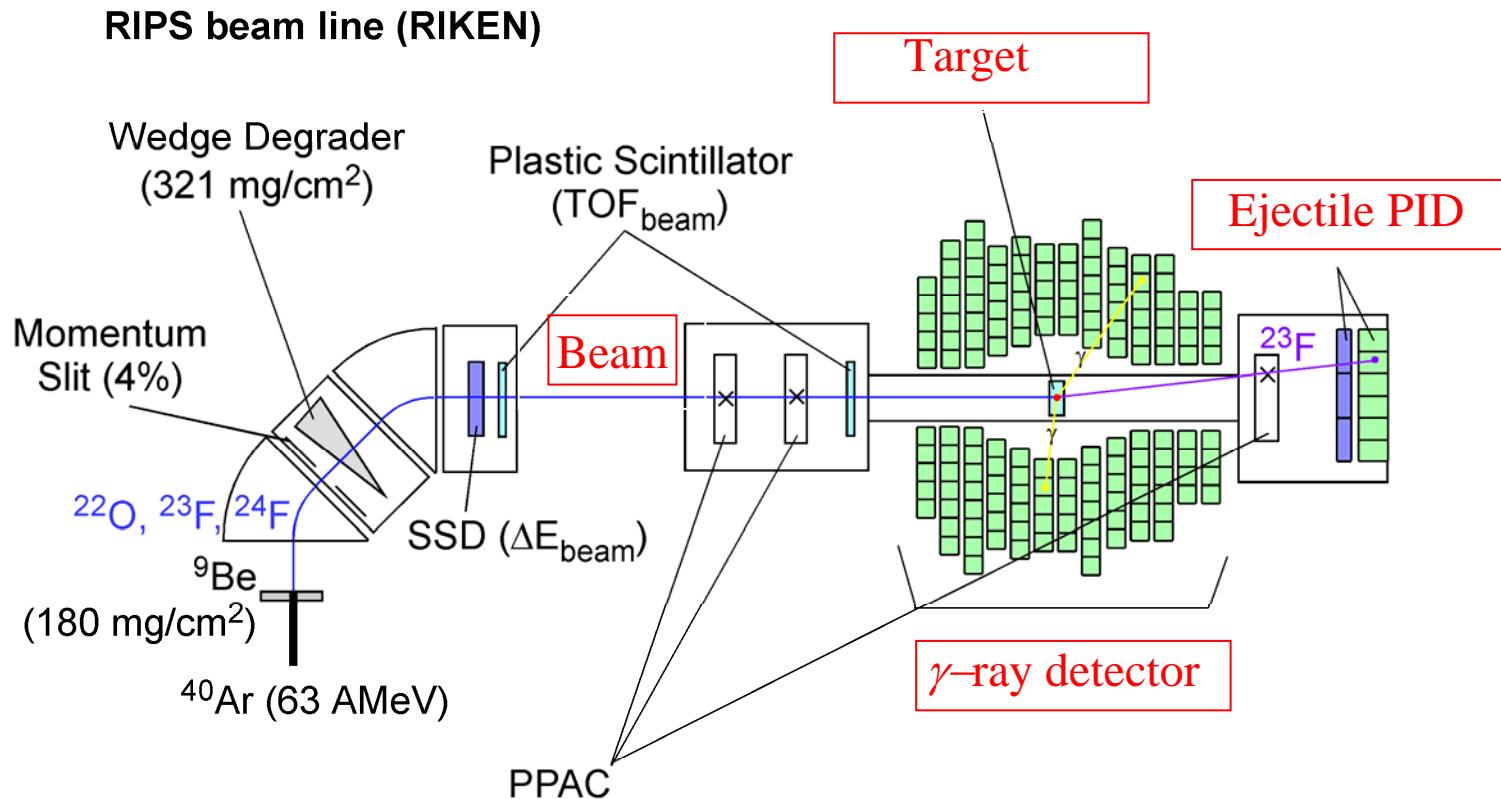
 *Energy degrador*

Second stage : $B\rho \sim A^{2.5}/Z^{1.5}$

RIPS
(RIKEN Projectile fragment
Separator)

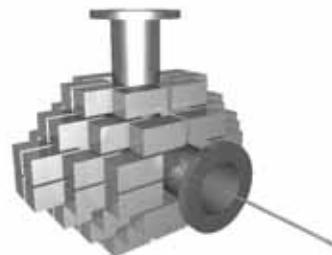


Typical Setup of γ -ray spectroscopy in inverse kinematics

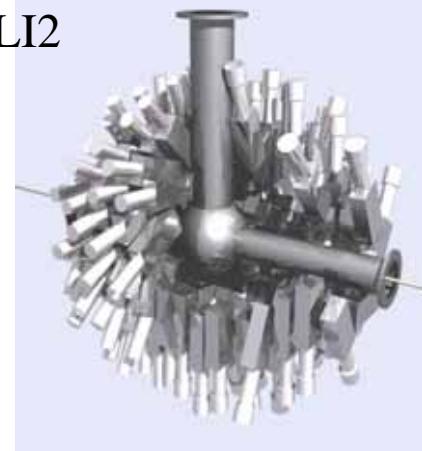


Upgraded NaI(Tl) detector array --- DALI2

DALI



DALI2



# of NaI(Tl) detectors	: 68	160
Angular resolution	: 15 deg.	8 deg.
Efficiency @ 1MeV	: 15%	21%
E resol. ($\beta=0.3$) @1MeV	: 12%	8%
Coverage (θ)	: 45~150 deg.	30~160 deg.

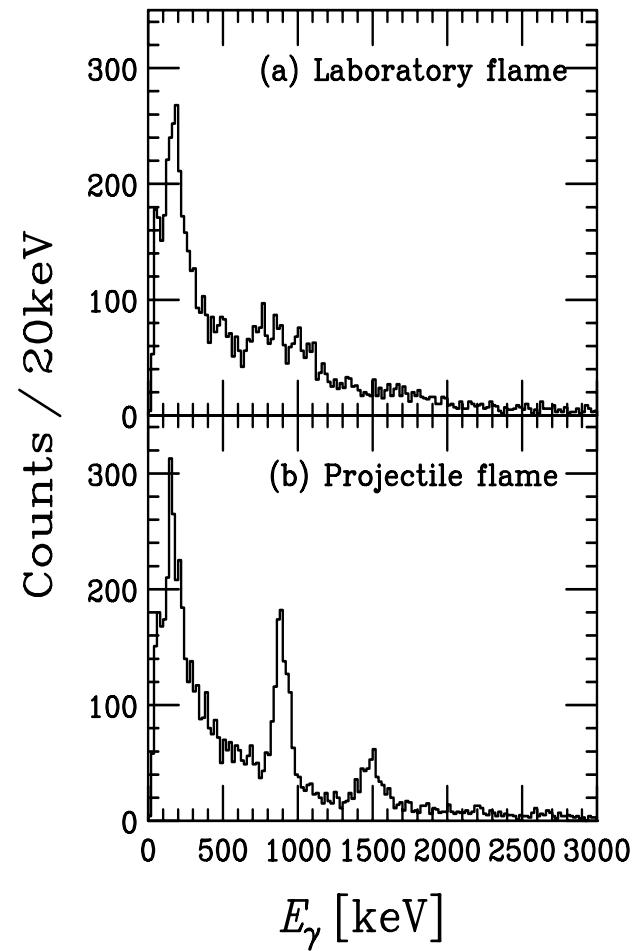
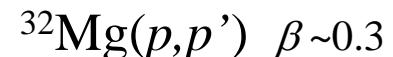
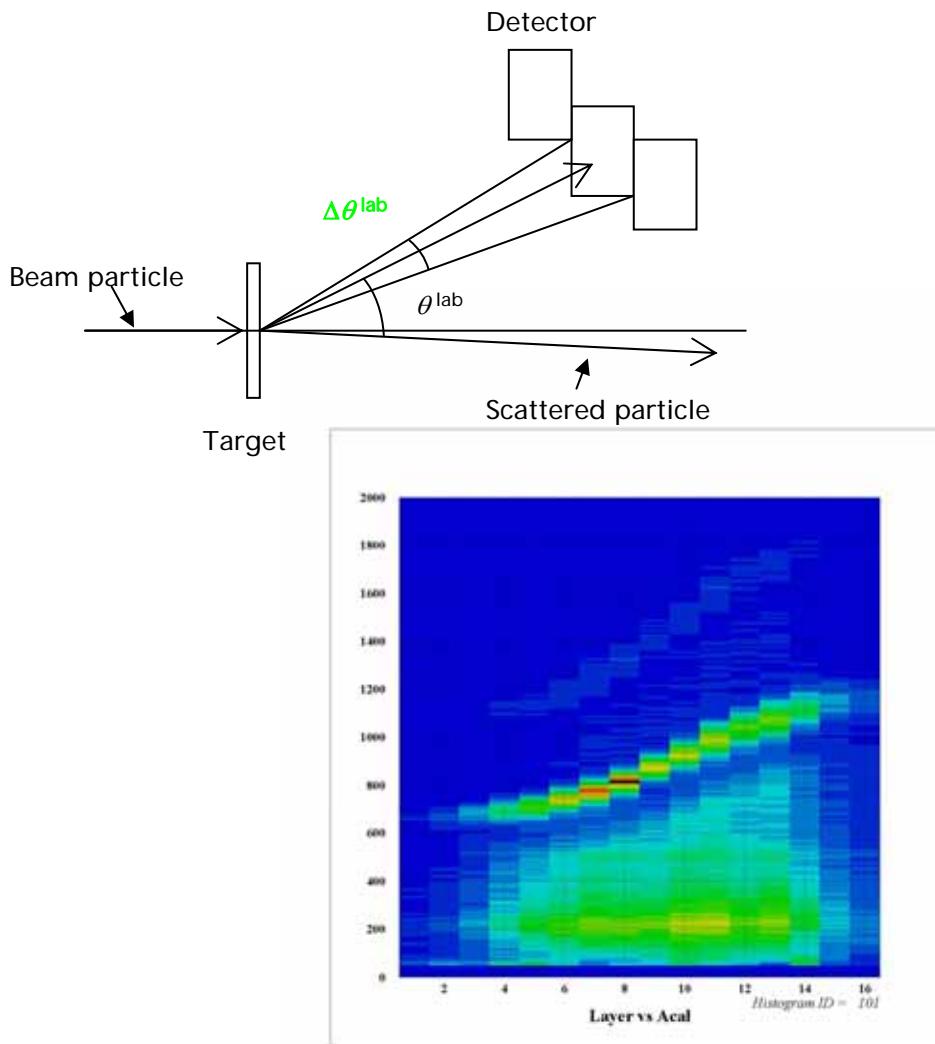
Experiments with high performance DALI2 detector.
 $\gamma-\gamma$ coincidence
Angular distribution (particle)
Angular distribution (γ -ray)
 $\gamma-\gamma$ angular correlation
Life time (Recoil Shadow Method)

Upgraded NaI(Tl) detector array - DALI2



Doppler correction of γ -rays from fast RI Beam ($\beta \sim 0.3$)

- γ -ray source is moving with $\beta \sim 0.3$
Doppler shifted \rightarrow need to be corrected for



H. Hasegawa, Master's thesis,
Rikkyo Univ., 2003

GRAPE

(Gamma-Ray detector Array with Energy and Position sensitivity)

CNS, Univ. Tokyo --- Shimoura et al.

S. Shimoura et al., CNS Annual Report 2001 (2002) 5.

Efficiency	5%	(4%; achieved)
Pos. resolution	2mm	(5mm; achieved)
E resolution	10keV	(16keV @ 2.1MeV, $\beta=0.3$; achieved)





Ejectile PID

- $\Delta E-E$
 - SSD+SSD
 - SSD+NaI
- TOF- $\Delta E-E$
 - Plastic scintillator hodoscope
 - TOF Spectrometer

γ -ray spectroscopy for unstable nuclei

- $N \sim 8$ ^{12}Be Magicity loss
- $A = 16$ ^{16}C Egg-like nucleus
- $Z = 9$ $^{23}\text{F}, ^{27}\text{F};$ Single proton state
- $N \sim 20$ ^{32}Mg , etc Island of Inversion
- $N \sim 28$ ^{42}Si , etc. New doubly magic nuclei?
- $N \sim 32, 34$ $^{52}\text{Ca}, ^{56}\text{Ti}$ New magic number?
- $N \sim 40$ ^{64}Cr New region of strong deformation?
- $\sim 78\text{Ni}$ $^{68,74}\text{Ni}, \text{Ge}, \text{Se}$ etc. $N=50, Z=28$ magicity ?

Island of Inversion

- Irregularity in Mass

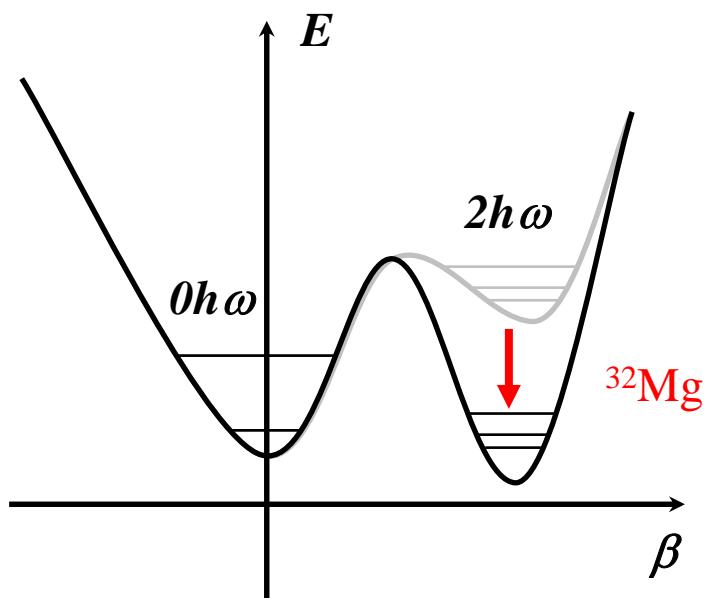
$^{31,32}\text{Na}$, $^{31,32}\text{Mg}$

Irregularity in $E_x(2^+)$

^{32}Mg

C. Thibault et al., PRC12(75)644

C. Detraz et al., NPA394(83)378,
E.K. Warburton et al., PRC41(90)1147.



$Z=20$									
^{36}Ca	^{37}Ca	^{38}Ca	^{39}Ca	^{40}Ca	^{41}Ca	^{42}Ca	^{43}Ca	^{44}Ca	
^{35}K	^{36}K	^{37}K	^{38}K	^{39}K	^{40}K	^{41}K	^{42}K	^{43}K	
^{34}Ar	^{35}Ar	^{36}Ar	^{37}Ar	^{38}Ar	^{39}Ar	^{40}Ar	^{41}Ar	^{42}Ar	
^{33}Cl	^{34}Cl	^{35}Cl	^{36}Cl	^{37}Cl	^{38}Cl	^{39}Cl	^{40}Cl	^{41}Cl	
^{32}S	^{33}S	^{34}S	^{35}S	^{36}S	^{37}S	^{38}S	^{39}S	^{40}S	
^{31}P	^{32}P	^{33}P	^{34}P	^{35}P	^{36}P	^{37}P	^{38}P	^{39}P	
^{30}Si	^{31}Si	^{32}Si	^{33}Si	^{34}Si	^{35}Si	^{36}Si	^{37}Si	^{38}Si	
^{29}Al	^{30}Al	^{31}Al	^{32}Al	^{33}Al	^{34}Al	^{35}Al	^{36}Al	^{37}Al	
^{28}Mg	^{29}Mg	^{30}Mg	^{31}Mg	^{32}Mg	^{33}Mg	^{34}Mg	^{35}Mg	^{36}Mg	
^{27}Na	^{28}Na	^{29}Na	^{30}Na	^{31}Na	^{32}Na	^{33}Na	^{34}Na	^{35}Na	
^{26}Ne	^{27}Ne	^{28}Ne	^{29}Ne	^{30}Ne	^{31}Ne	^{32}Ne		^{34}Ne	

$N=20$

Island of Inversion

- Irregularity in Mass

$^{31,32}\text{Na}$, $^{31,32}\text{Mg}$

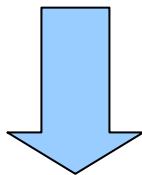
C. Thibault et al., PRC12(75)644

- Irregularity in $E_x(2^+)$

^{32}Mg

C. Detraz et al., NPA394(83)378,

E.K. Warburton et al., PRC41(90)1147.



Advent of In-flight RI beam facility

- Detailed γ -ray spectroscopy through properties of excited states via secondary reactions such as **Coulomb excitation**.

Coulex \rightarrow $B(\text{E}2) \propto Q_0^{-2} \propto \beta_2^{-2}$

Collectivity large : $B(\text{E}2)$ Large

$E_x(2^+)$ small

Coulomb Excitation

Office of Naval Research, European Scientific Notes, No. 7-9, May 1, 1953

*Proposed Coulomb Excitation of Nuclei**

At a recent colloquium in the Institute for Theoretical Physics, Copenhagen, Dr. B. R. Mottelson discussed a novel proposal for producing excitation of nuclear states. Mottelson's proposal was to bombard atomic nuclei with charged particles whose energy is well below the barrier. The probability of penetrating the barrier would consequently not be appreciable, and the nucleus would experience only the Coulomb field. Thus the excitation resulting from the pulse of electromagnetic energy would reflect the properties of the target nucleus free from complication by the nuclear force between target and projectile.

- Energy of in-flight RI beam is much higher than

$$\text{Coulom barrier} = 4.0 \text{AMeV } (^{32}\text{Mg} + ^{208}\text{Pb})$$

RIKEN, GANIL $\sim 50A$ MeV

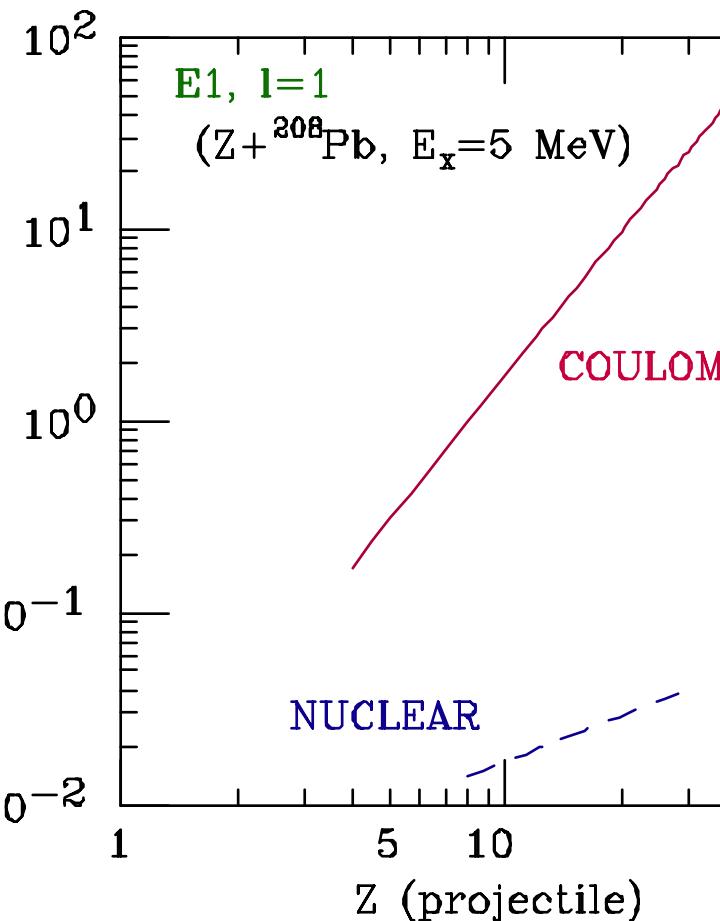
MSU, GSI $100 \sim 200A$ MeV

RIBF $\sim 250A$ MeV

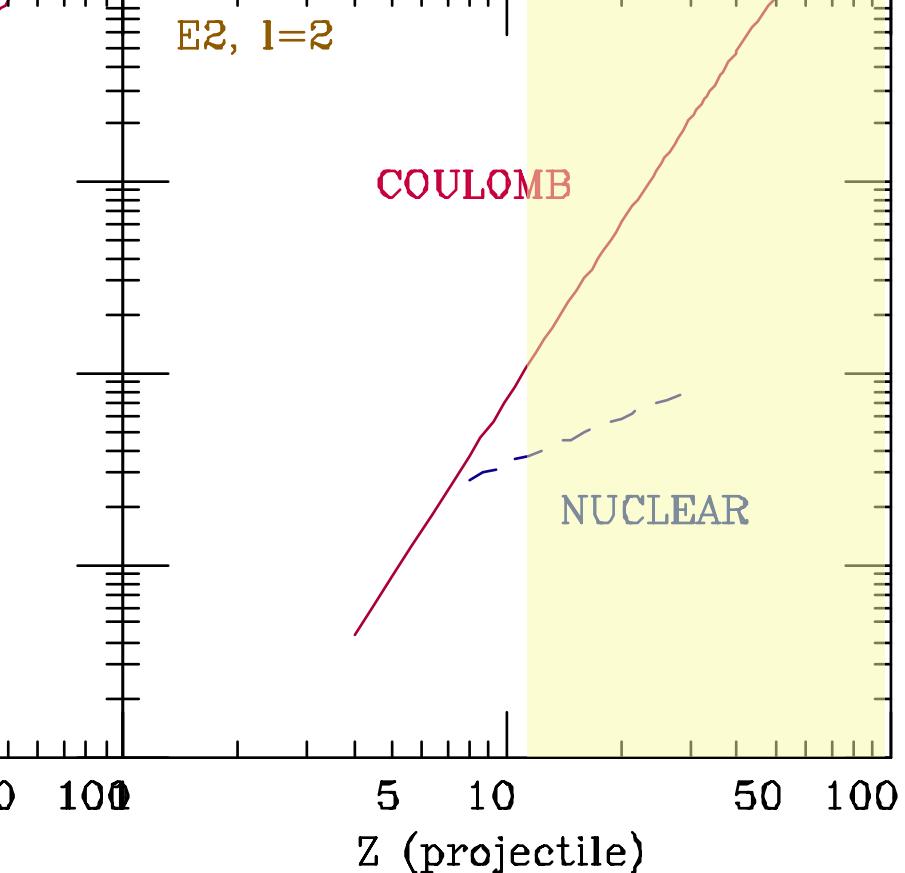
- For nuclei with $Z > 10$, $\sigma(\text{Coulomb}) > \sigma(\text{nuclear})$

Huge Cross section \sim a few 100 mb

relative cross section



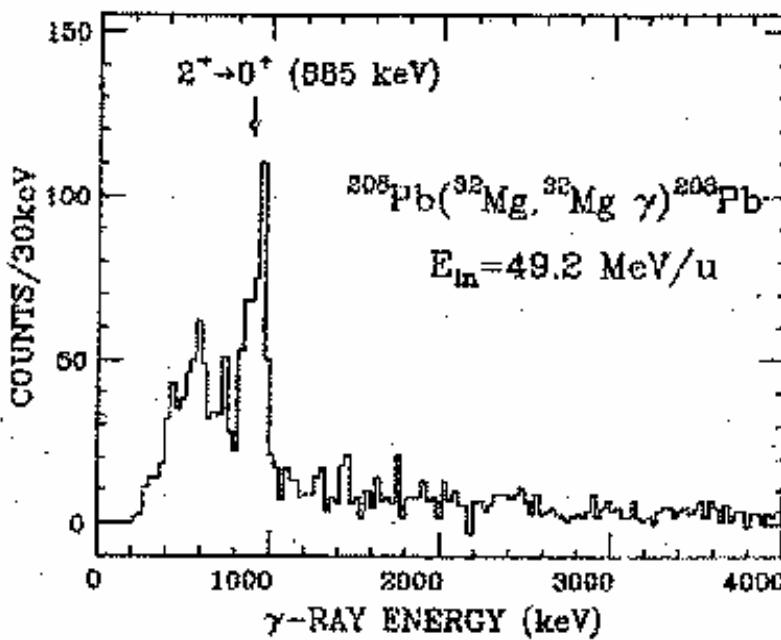
$C > N$



$C \sim N$

$E_{\text{in}} = 50 \text{ MeV/nucleon}$, a fixed deformation

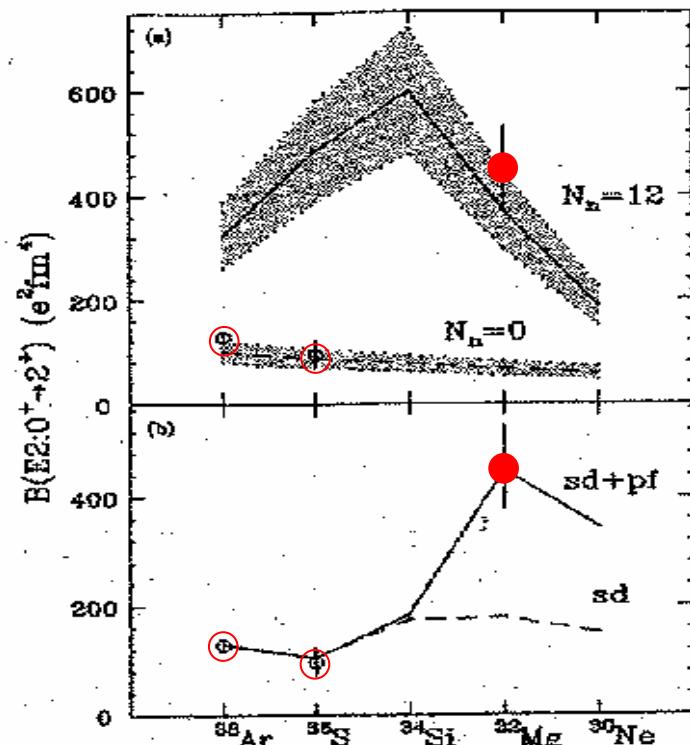
^{32}Mg Coulex --- dawn of γ -ray spectroscopy of unstable nuclei



T. Motobayashi et al., Phys. Lett. B346,

^{32}Mg beam: 300 cps

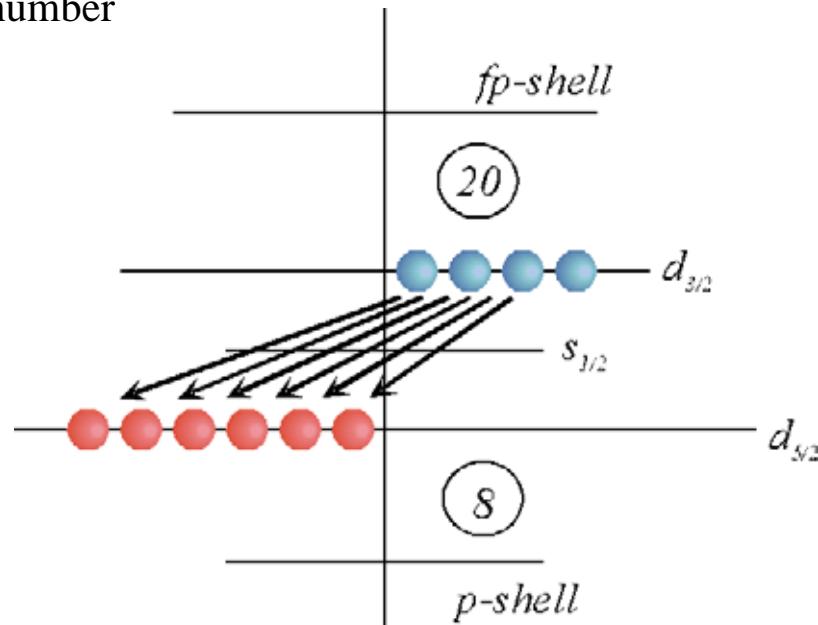
Exhibit: Strong deformation of ^{32}Mg
Usefulness of Int. Energy Coulex



Fukunishi et al., PLB 296, 279(92)

Strong deformation of ^{32}Mg

- Strong $\sigma\tau N-N$ Interaction ($(d_{5/2})_p$ - $(d_{3/2})_n$)
 - T. Otsuka et al., PRL **87**, 082502 (2001).
 - Y. Utsuno et al., PRC 60, 054315(1999)
 - Change of the effective single particle energies
 - Disappearance of $N=20$ magicity
 - $N=16$ new magic number

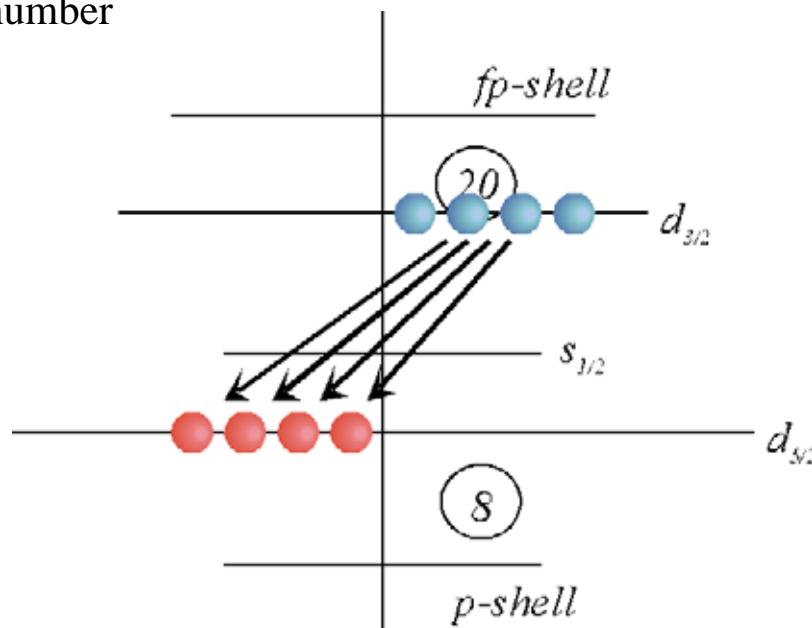


^{34}Si

Strong deformation of ^{32}Mg

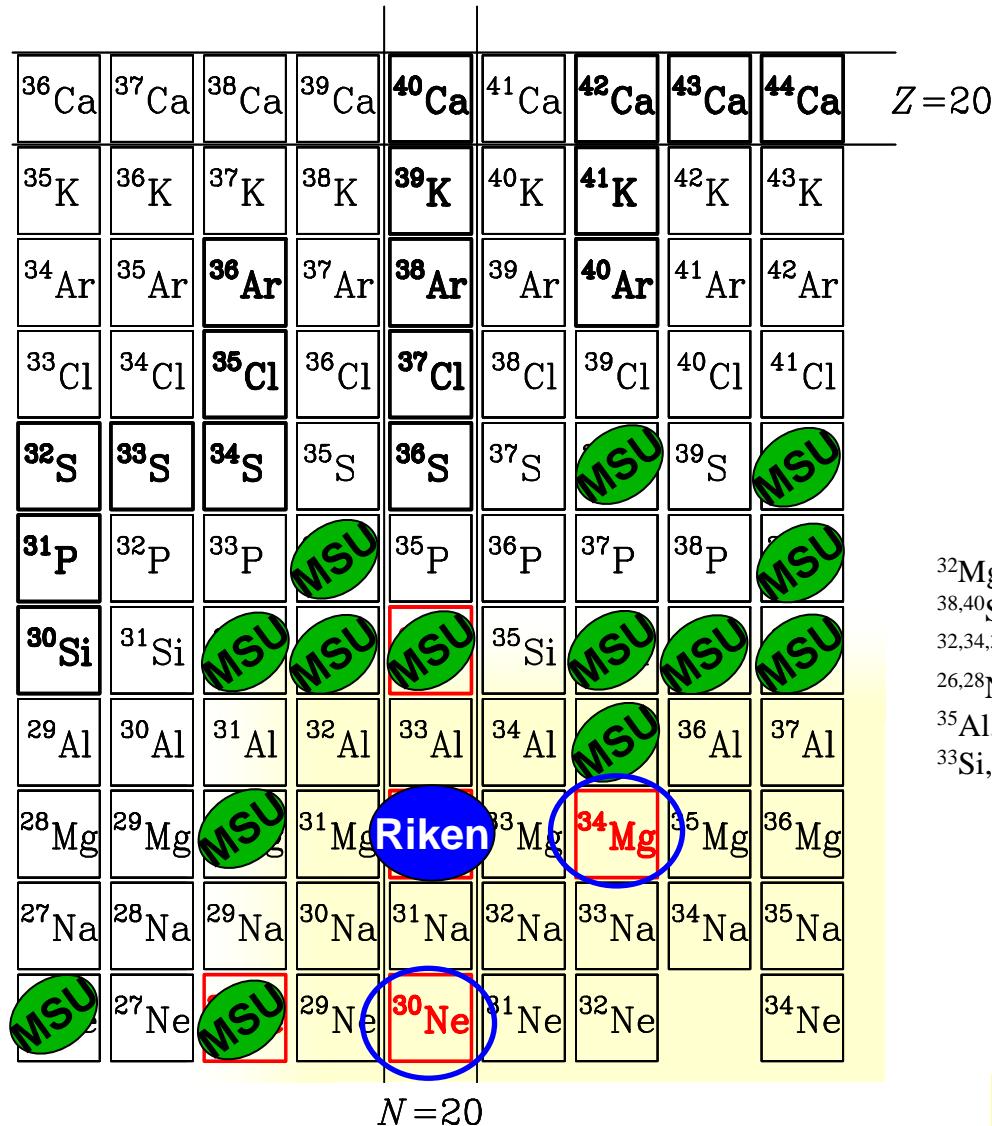
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T. Motobayashi et al., PLB 346, 9(1995)



^{32}Mg

Experiments in “Island of Inversion” region



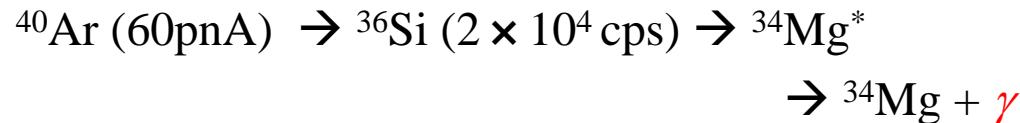
- ^{32}Mg :PLB346(95)9
- $^{38,40}\text{S}$:PRL77(96)3967.
- $^{32,34,36,38}\text{Si}$:PRL80(98)2081.
- $^{26,28}\text{Ne}, ^{30}\text{Mg}$:PLB461(99)322.
- $^{35}\text{Al}, ^{37}\text{Si}, ^{39}\text{P}$:PRC59(99)642.
- $^{33}\text{Si}, ^{34}\text{P}$:PRC62(00)051601(R).

Island of inversion

$E_x(2^+)$ measurement for ^{34}Mg by two-step projectile fragmentation method

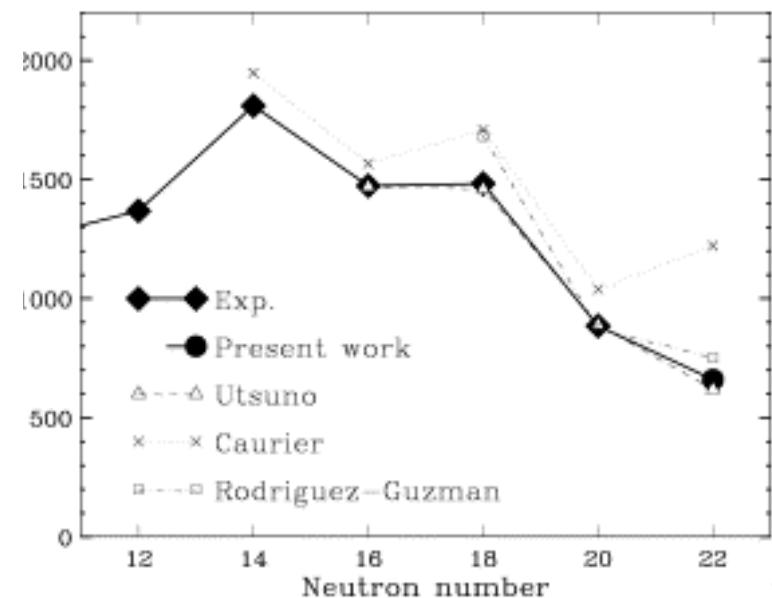
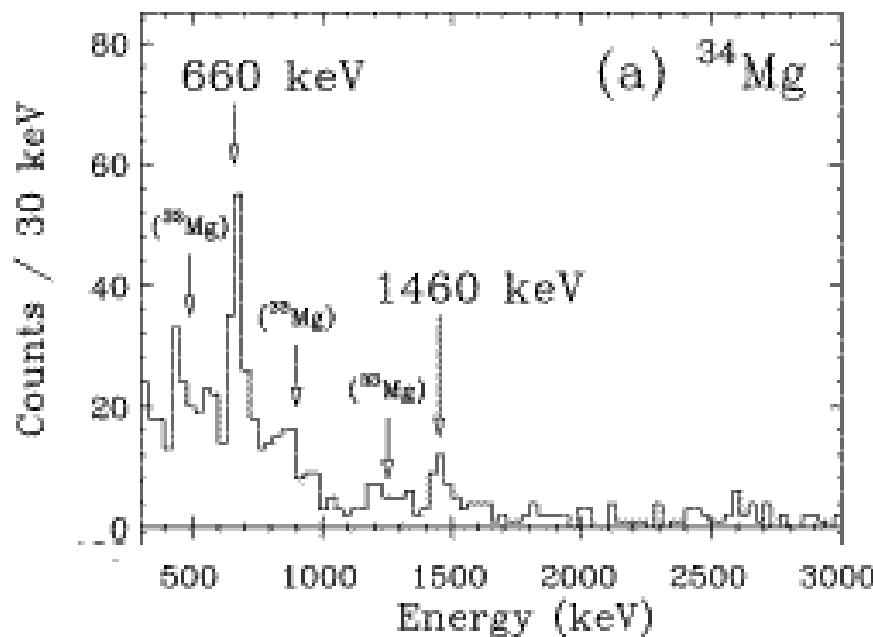
- $E_x(2^+)$ and $E_x(4^+?)$

Two-step projectile fragmentation method



$$E_x(2^+) = 660 \text{ keV} \quad \text{Lower than } {}^{32}\text{Mg} \quad E_x(2^+) = 885 \text{ keV}$$

K. Yoneda et al., PLB499(2001) 233.



^{34}Mg $B(\text{E}2)$ by Coulex

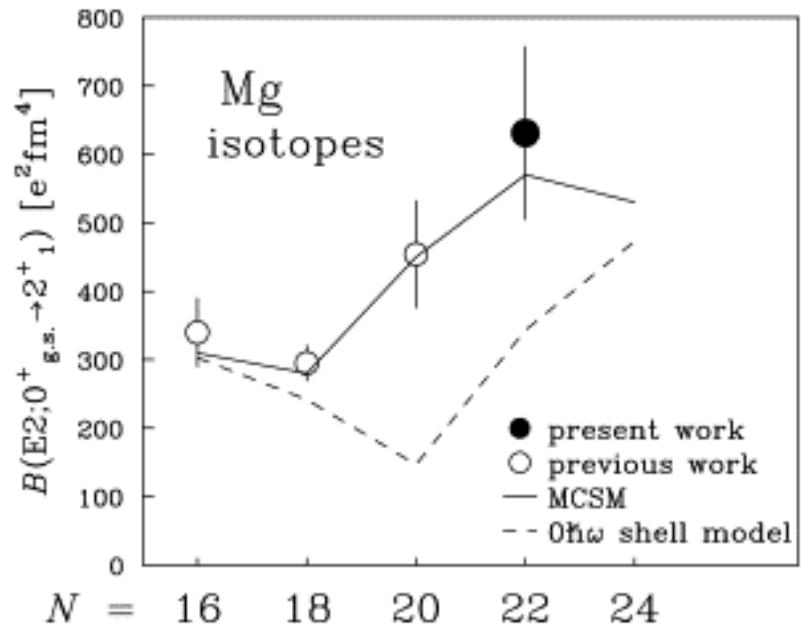
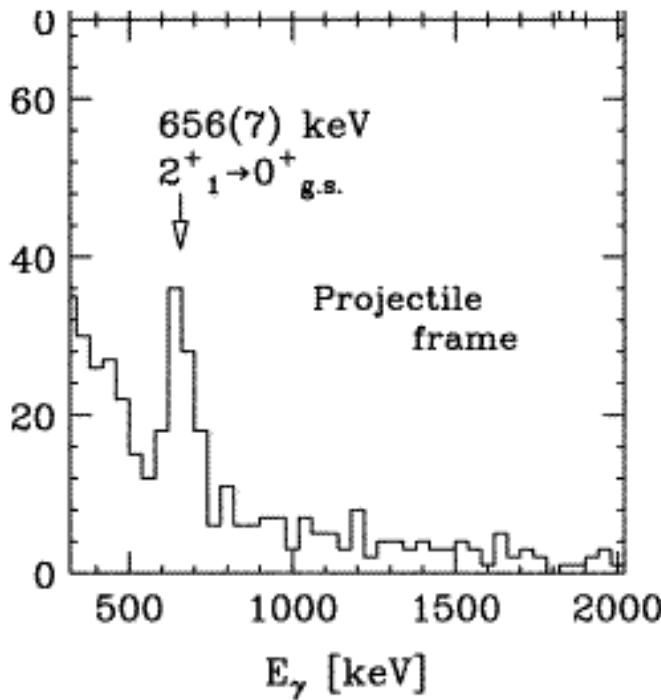
- $B(\text{E}2)$ measurement by Coulomb excitation
with 4 cps ^{34}Mg beam.

$$B(\text{E}2) = 631(126)\text{e}^2\text{fm}^4$$

Even larger than ^{32}Mg ($454(78)\text{e}^2\text{fm}^4$)

H. Iwasaki et al., PLB522(2001)227.

^{34}Mg is located inside the Island of Inversion



^{34}Mg : 4 cps --- Succeeded
Already difficult

^{30}Ne : 0.2cps --- How do we do ?

(p, p') using Liq. H_2 target

(p,p') with in-beam γ -ray spectroscopy tech. using Liq. H₂ target

- Reaction mechanism

- Simple reaction mechanism:

- \leftrightarrow Heavy Ion induced reaction.

- Complex reaction mechanism: --- Optical potential problem

- \leftrightarrow Coulex

- Sensitive both to protons and to neutrons

- \leftrightarrow Coulex, $\rightarrow M_n/M_p$

- “Loose” selectivity

- \circ Chance to study levels with various J^P ; 2^+ , 1^- , 3^- , 0^+ , 4^+ , 1^+ ,...

- \times Need of correction for cascade decays $\rightarrow \gamma\text{-}\gamma$ analysis, ...

- J^π assignment \rightarrow angular distribution, angular correlation,...

- Experimental advantages

- Efficient-1:

- Largest number of nuclei in the target with energy loss equivalent thickness.

- \rightarrow Highest luminosity

- Efficient-2:

- Large acceptance for ejectiles due to kinematical focusing.

- Clean spectra-1: (γ -ray spectroscopy)

- Absence of background γ -rays (or X-rays) originating from the target.

- Clean spectra-2:

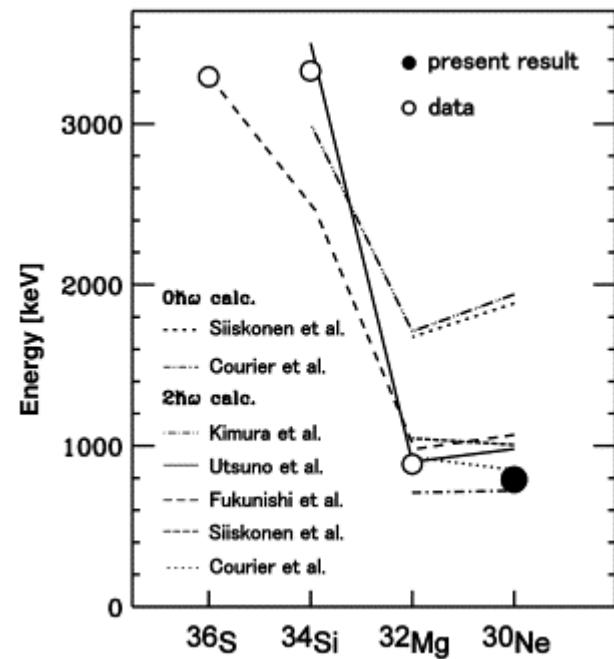
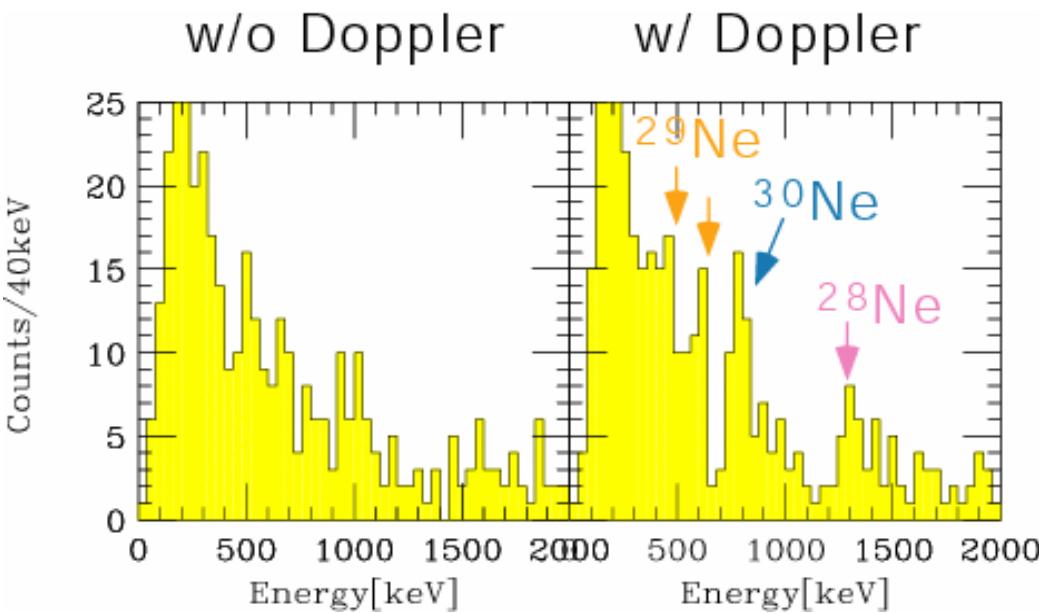
- Pure proton target \leftrightarrow CH₂ target – C target

$^{30}\text{Ne } E_x(2^+)$

- $\text{H}(\text{H}^{30}\text{Ne}, \text{H}^{30}\text{Ne} \gamma) = ^{30}\text{Ne}(p, p')$
 $\text{Ex}(2+) = 791(26) \text{ keV}$

Y.Yanagisawa et al., PLB566(02)84

^{30}Ne is located inside the Island of Inversion



Experiments in “Island of Inversion” region

Island of inversion

^{34}Si --- Boundary of Island of Inversion ?

- Coulomb excitation @ MSU

R.W.Ibbotson et al., PRL 80(98)2081

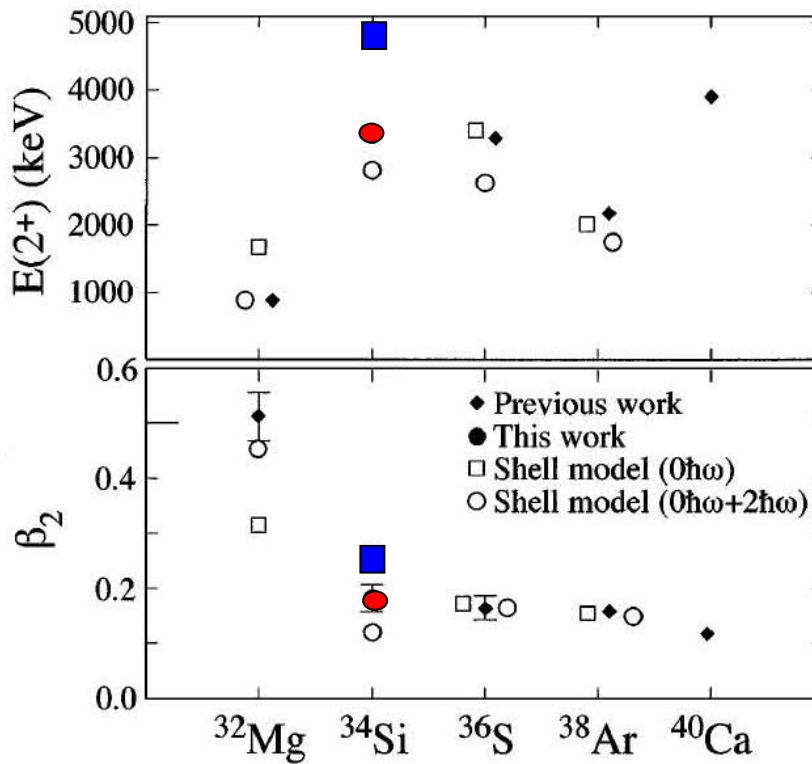
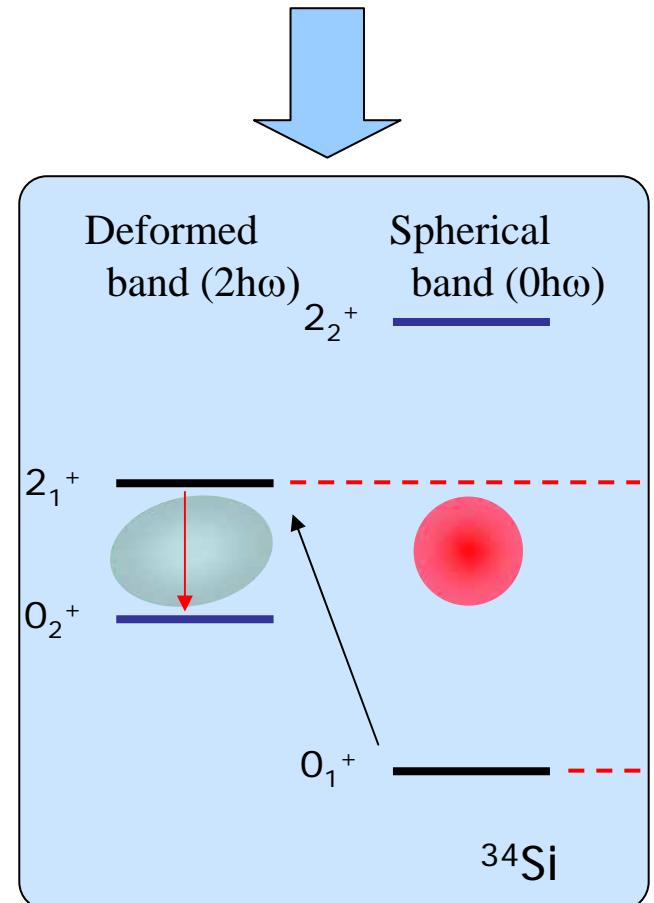
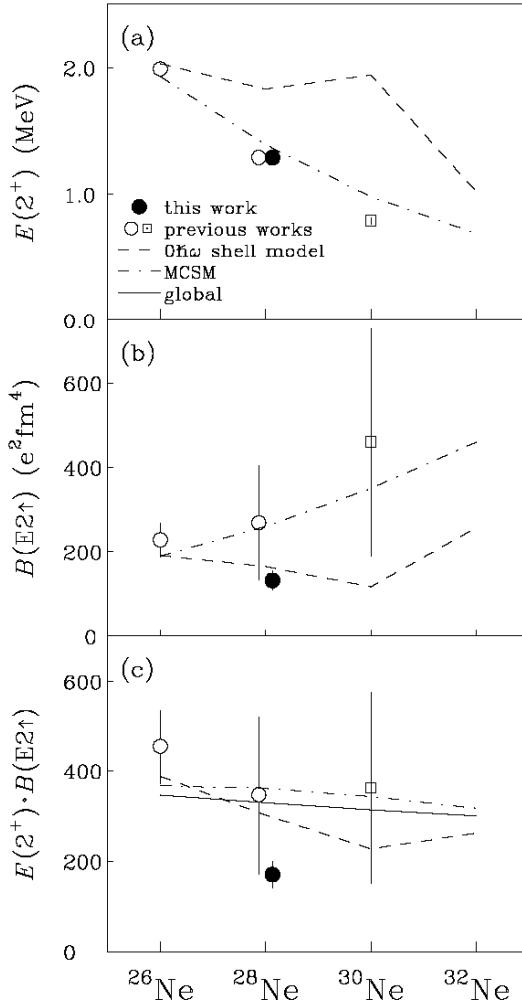


FIG. 3. The deformation parameter β_2 extracted from the known $B(E2 \uparrow)$ values in the $N = 20$ nuclei. The ^{34}Si measurement is from the present work.

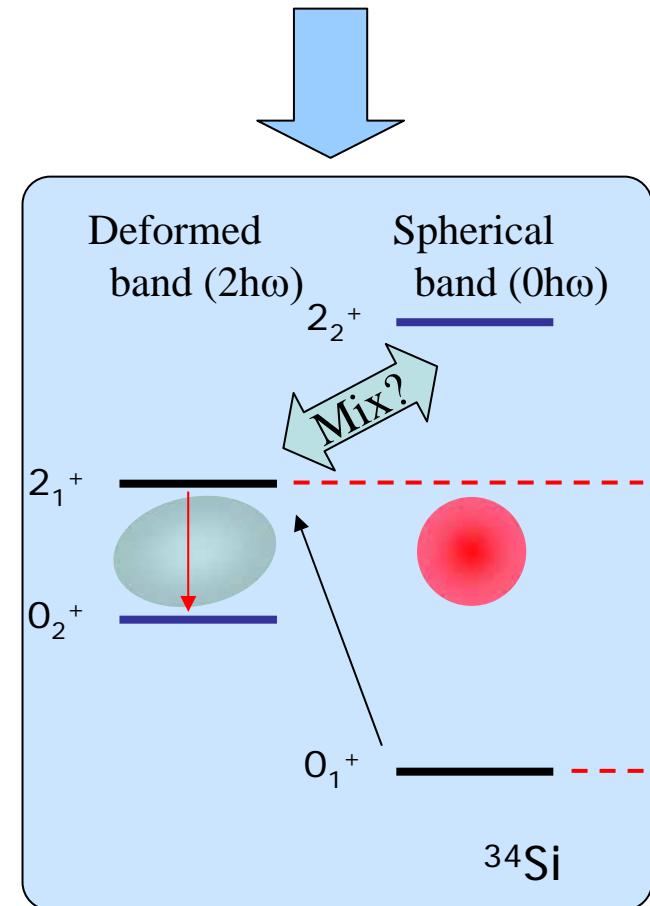
$B(E2)$ (β_2) is smaller than the value predicted from $E_x(2^+)$



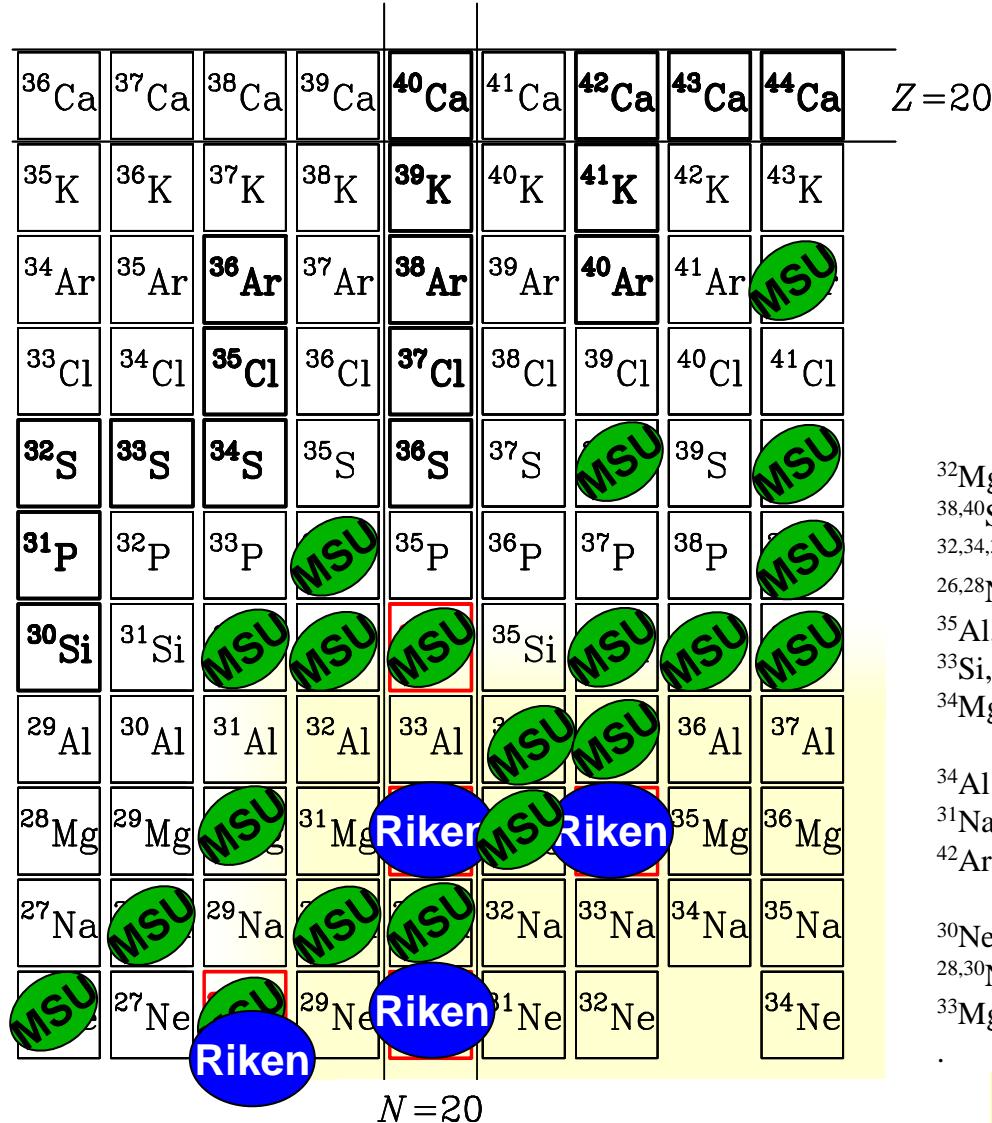
^{28}Ne --- Boundary of Island of Inversion ?



Ex(2^+): agree with $2\hbar\omega$ calculation
 B(E2): agree with $0\hbar\omega$ calculation

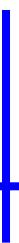


Experiments in “Island of Inversion” region



^{32}Mg	:PLB346(95)9
$^{38,40}\text{S}$:PRL77(96)3967.
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$^{33}\text{Si}, ^{34}\text{P}$:PRC62(00)051601(R).
^{34}Mg	:PLB499(01) 233. PLB522(01)227
^{34}Al	:PRC63(01)047308.
^{31}Na	:PRC63(01)011305(R).
^{42}Ar	:PRC63(01)014604.
^{30}Ne	:PLB566(02)84
$^{28,30}\text{Na}$:PRC66(02)024325.
^{33}Mg	:PRC65(02)061304(R).

Island of inversion



More elaborate study for the nuclei

in and around the Island of Inversion

Possibility of shape coexistence in ^{32}Mg and ^{34}Si

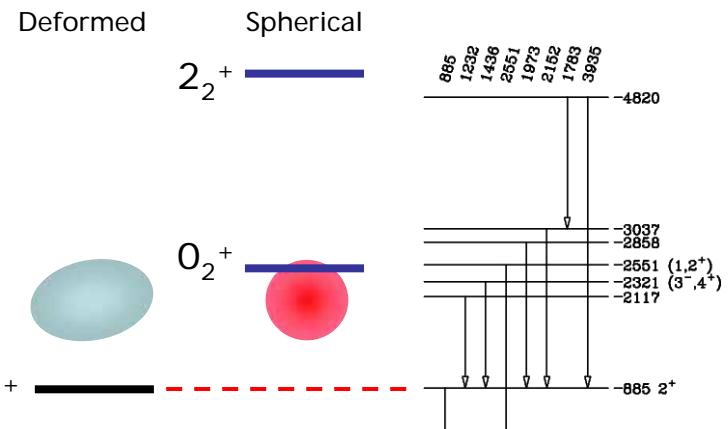
S. Takeuchi et al.

^{32}Mg , ^{34}Si

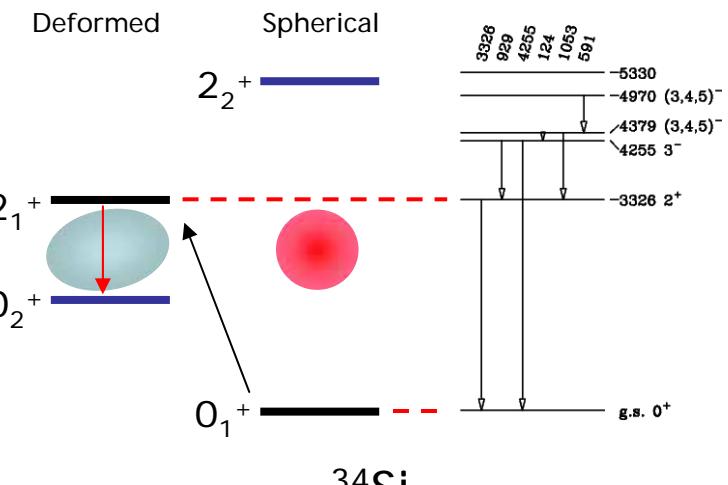
Shape co-existence has not yet been established experimentally nor directly.

→ detailed spectroscopy with (p,p')

- J^π determination
- $d\sigma/d\Omega(\theta)$
- γ -ray angular distribution
- $\gamma-\gamma$ angular correlation
- M_n/M_p (p,p')+Coulex

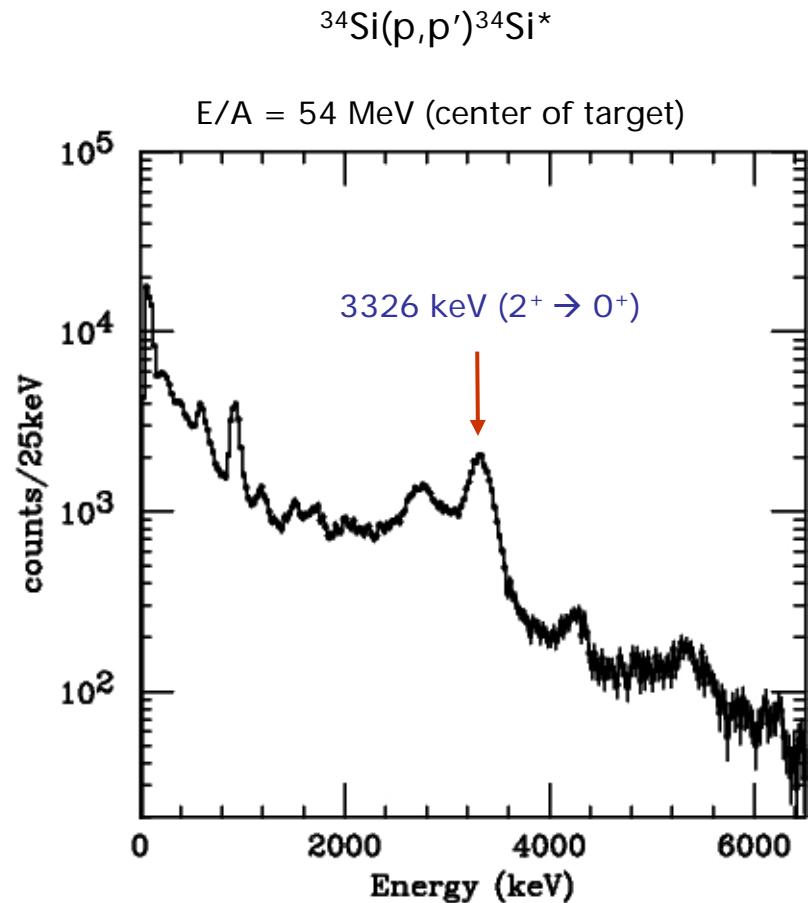
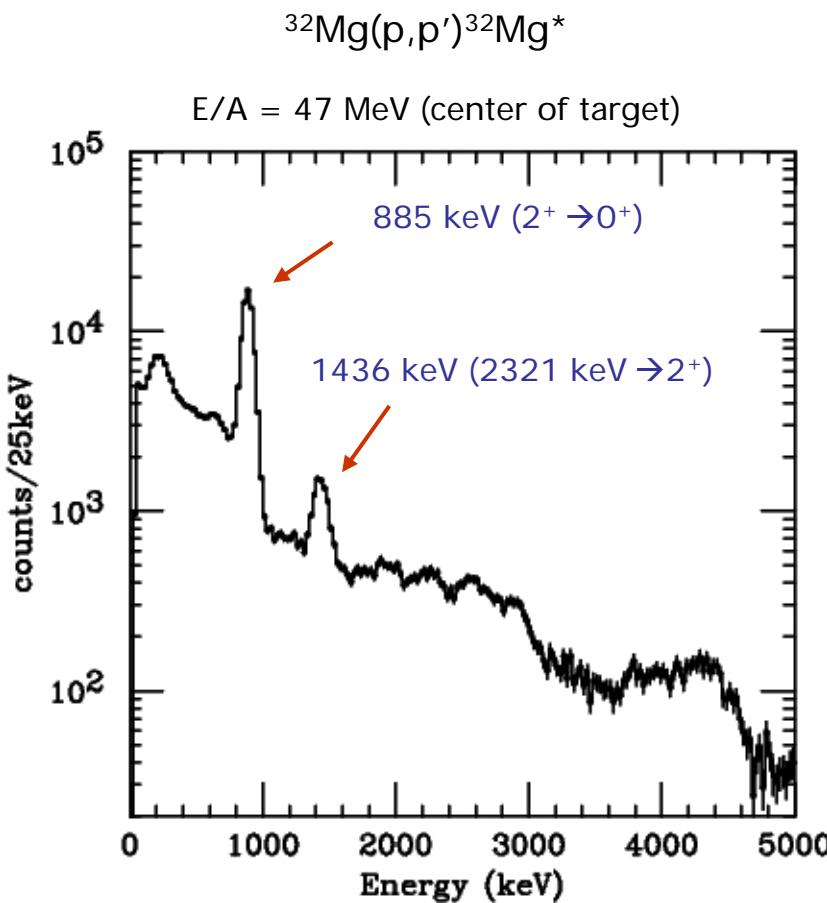


^{32}Mg



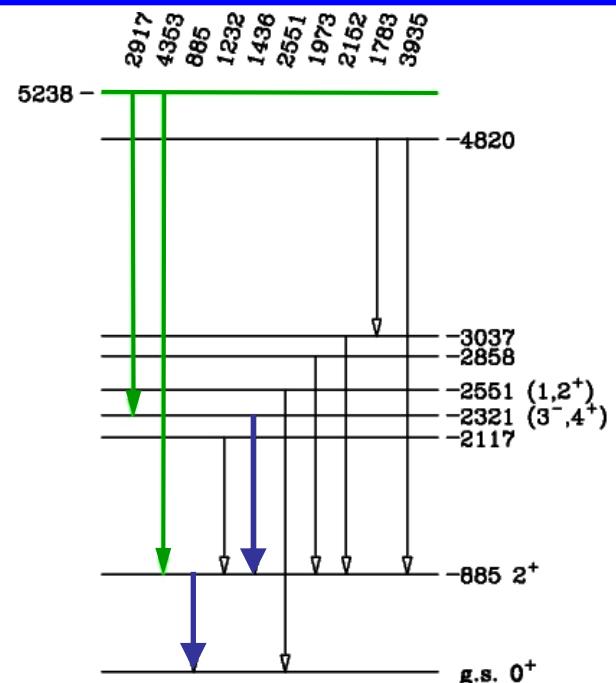
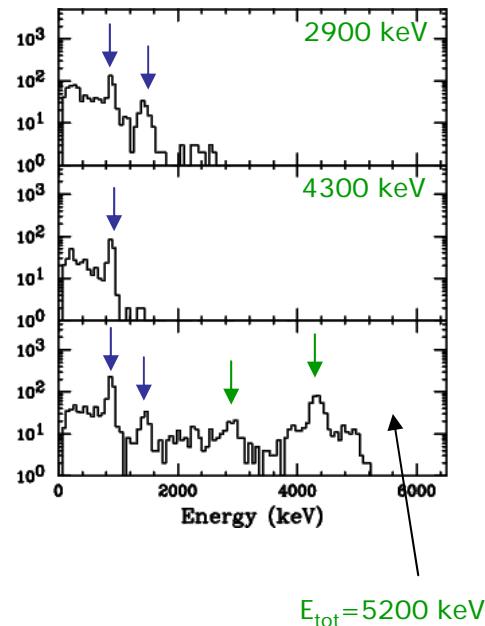
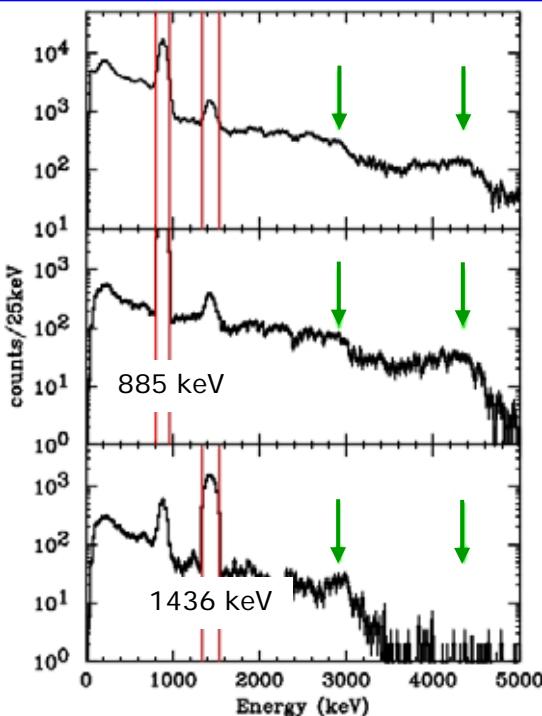
^{34}Si

γ -ray spectra of $^{32}\text{Mg}(p,p')$ $^{32}\text{Mg}^*$ and $^{34}\text{Si}(p,p')$ $^{34}\text{Si}^*$



- γ -ray spectra were obtained after Doppler corrected by DALI2 for each reactions.
- In order to obtain cross sections, γ - γ analysis was performed to estimate cascading contributions.

γ -ray spectra -³²Mg-



2900 keV γ ray is coincident with both 885 and 1436 keV γ rays.

$$2900 \text{ keV} + 1436 \text{ keV} + 885 \text{ keV} = 5221 \text{ keV}$$

4300 keV γ ray is coincident with 885 keV γ ray while it disappear in 1436 keV gate spectrum.

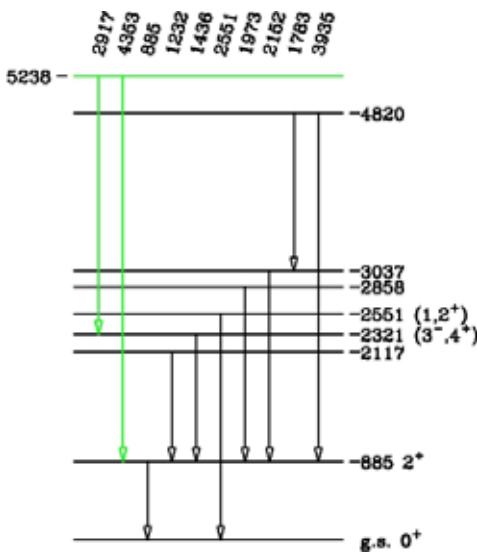
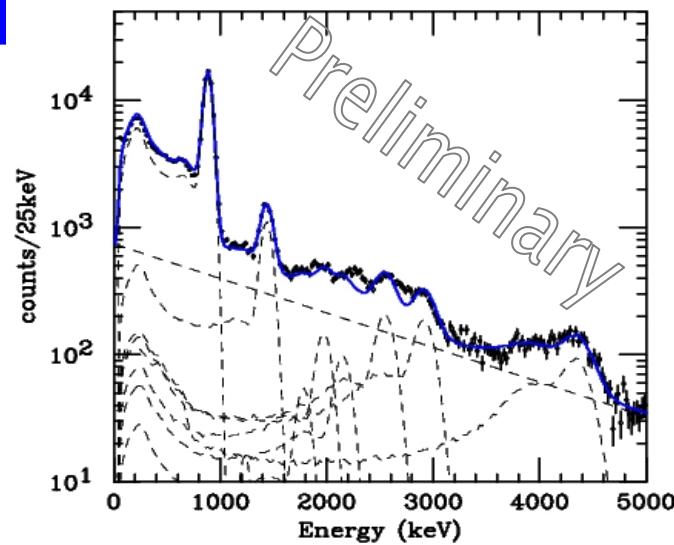
$$4300 \text{ keV} + 885 \text{ keV} = 5185 \text{ keV}$$

Peak energies are obtained γ - γ spectrum with 5200 keV gate on total energy spectrum as follows:

$$4353 \text{ keV}, 2917 \text{ keV}.$$

Assuming those γ rays are transitions from same level, level energy is assigned to be 5238 keV preliminary.

Cross sections ${}^{32}\text{Mg}$ -



$$\sigma(0^+ \rightarrow 2^+) = 43.8(56) \text{ mb}$$

$$\sigma(0^+ \rightarrow 3^-/4^+) = 3.8(9) \text{ mb}$$

Deformation parameter and deformation length are deduced from DWBA calculation(ECIS97) with CH89 optical parameters.

$$\beta_2^{pp'} = 0.472(30), \delta_2^{pp'} = 1.768(112) \text{ fm for } 2^+ \text{ state.}$$

Adopted value*

$$\beta_2 = 0.473(43), \delta_2 = 1.802(164) \text{ fm } (r_0 = 1.2 \text{ fm})$$

* S. RAMAN et al., Atomic Data and Nuclear Data Tables **78**(2001)1

$$(\text{Mn/Mp})/(\text{N/Z}) = 0.955$$

Discussion about $E_x = 2321 \text{ keV}$ state

$J^\pi = 3^-$ case : Deformation parameter β_3 is deduced from DWBA calculation and experimental cross section assuming one-phonon state as follows.

$$\beta_3^{pp'} = 0.162(14)$$

$J^\pi = 4^+$ case : Cross section is estimated to be 1.2 mb by DWBA calculation with $\beta_2^{pp'} = 0.472$ assuming two-step transition.

E_x (keV)	J^π	C.S. (mb)
5238		5.4(12)
4820		0.4(2)
3037		0.6(4)
2858		1.4(4)
2551	(1,2 ⁺)	2.6(6)
2321	(3 ⁻ ,4 ⁺)	3.8(9)
2117		0.1(1)
885	2 ⁺	43.8(56)

“Safe Coulomb excitation”

Coulomb excitation
 $^{30}\text{Mg} + \text{Ni}$
at around Coulomb barrier, 2.25AMeV
@ REX-ISOLDE

Smaller $B(E2)$...

PRL 94, 172501 (2005)

PHYSICAL REV

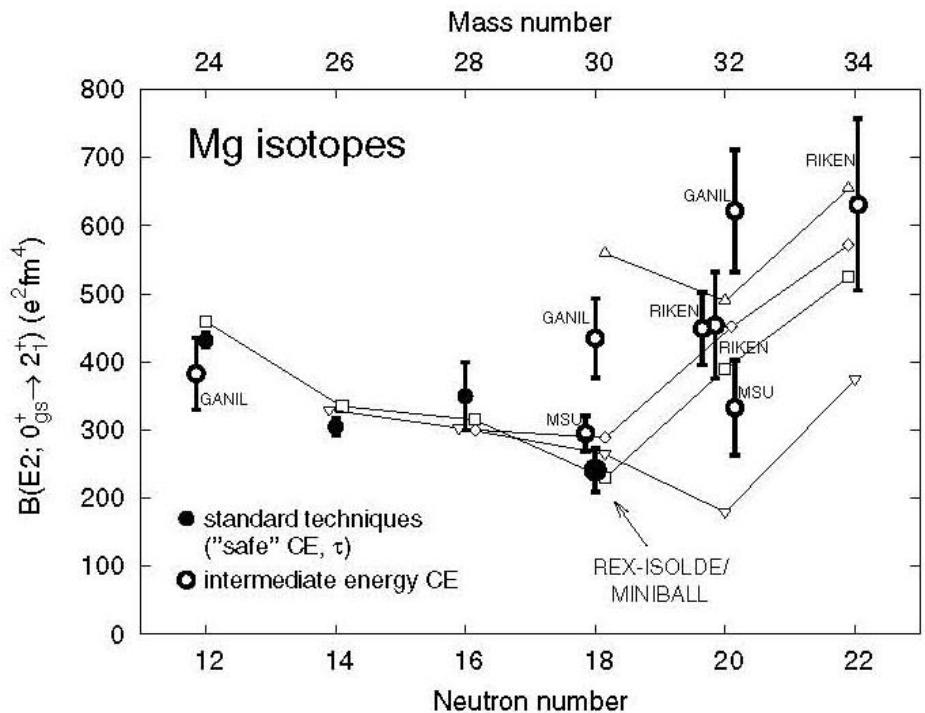


FIG. 2. Experimental (open and filled circles) and theoretical $B(E2)$ values (connected by thin lines to guide the eye) for the even Mg isotopes. The experimental data are from Refs. [5–8,23] and the present experiment; the theoretical values are from □ [11], ◇ [9], ▽ [10,26] (normal), △ [10] (intruder).

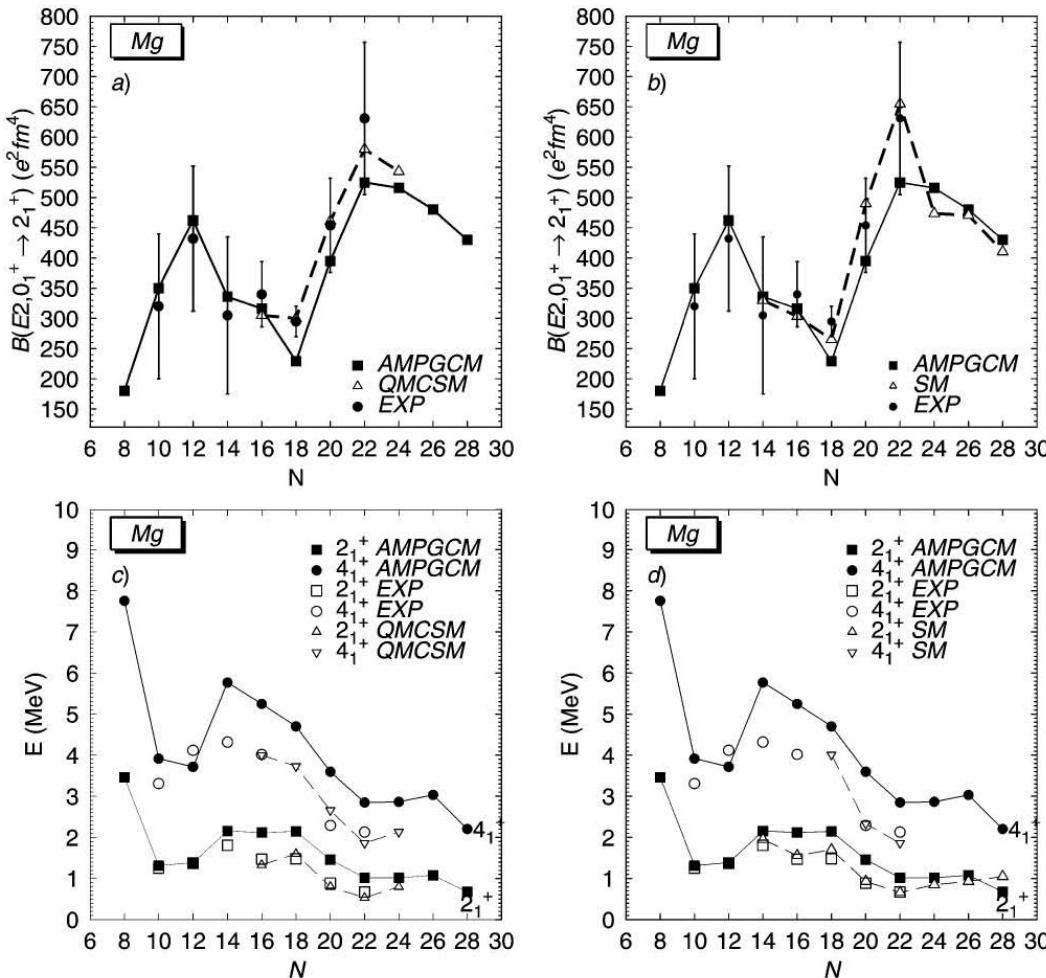
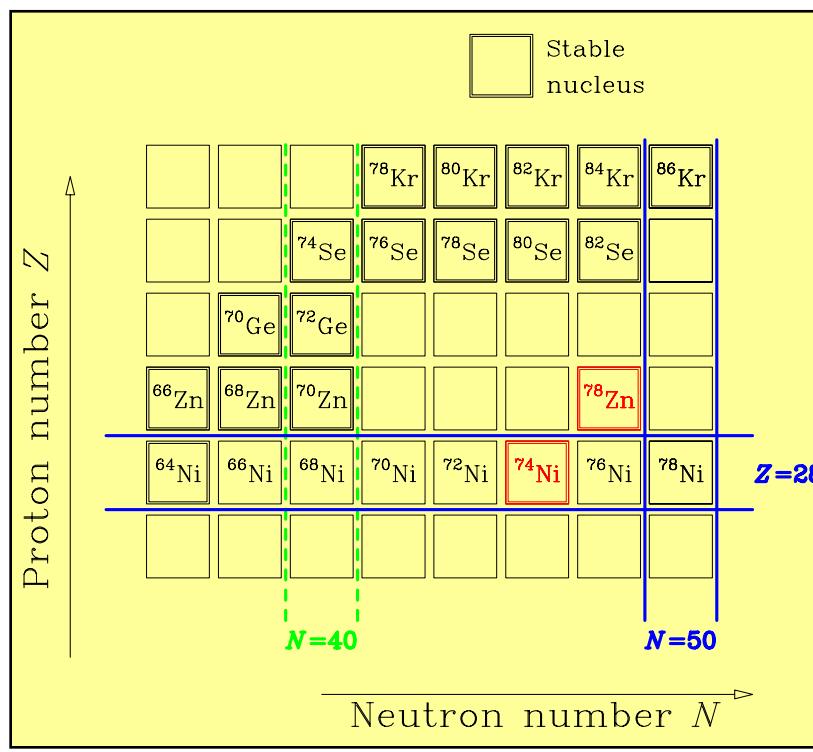


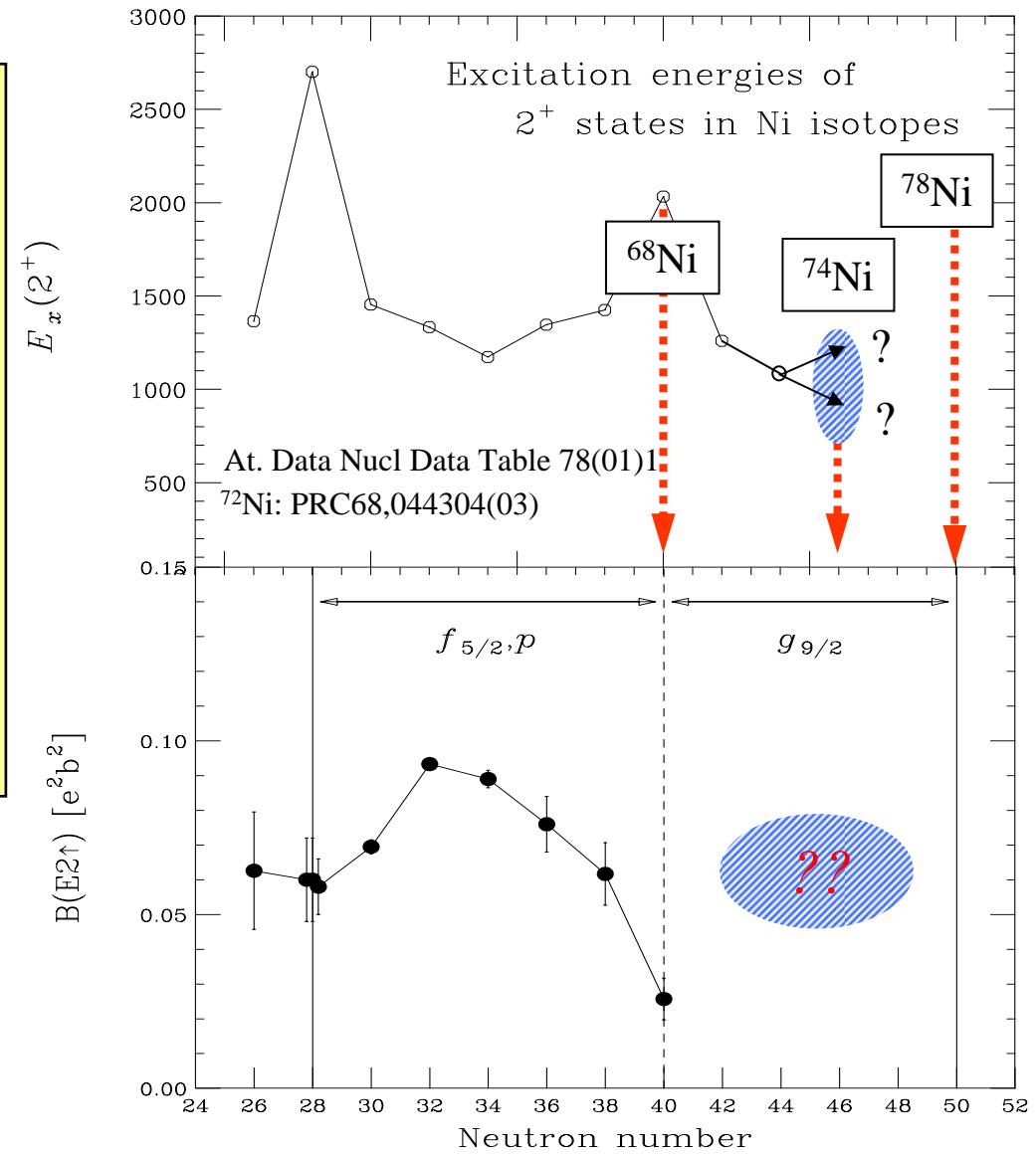
Fig. 13. The excitation energies of the states 2_1^+ and 4_1^+ provided by the AMPGCM and the $B(E2, 0_1^+ \rightarrow 2_1^+)$ transition probabilities in $^{20-40}\text{Mg}$ are compared with the available experimental data [15,16,19,20,22,23,25] and with the theoretical predictions of the Quantum Monte Carlo Shell Model [45] and the Shell Model [44,46].

^{74}Ni ($p,p'\gamma$) experiment

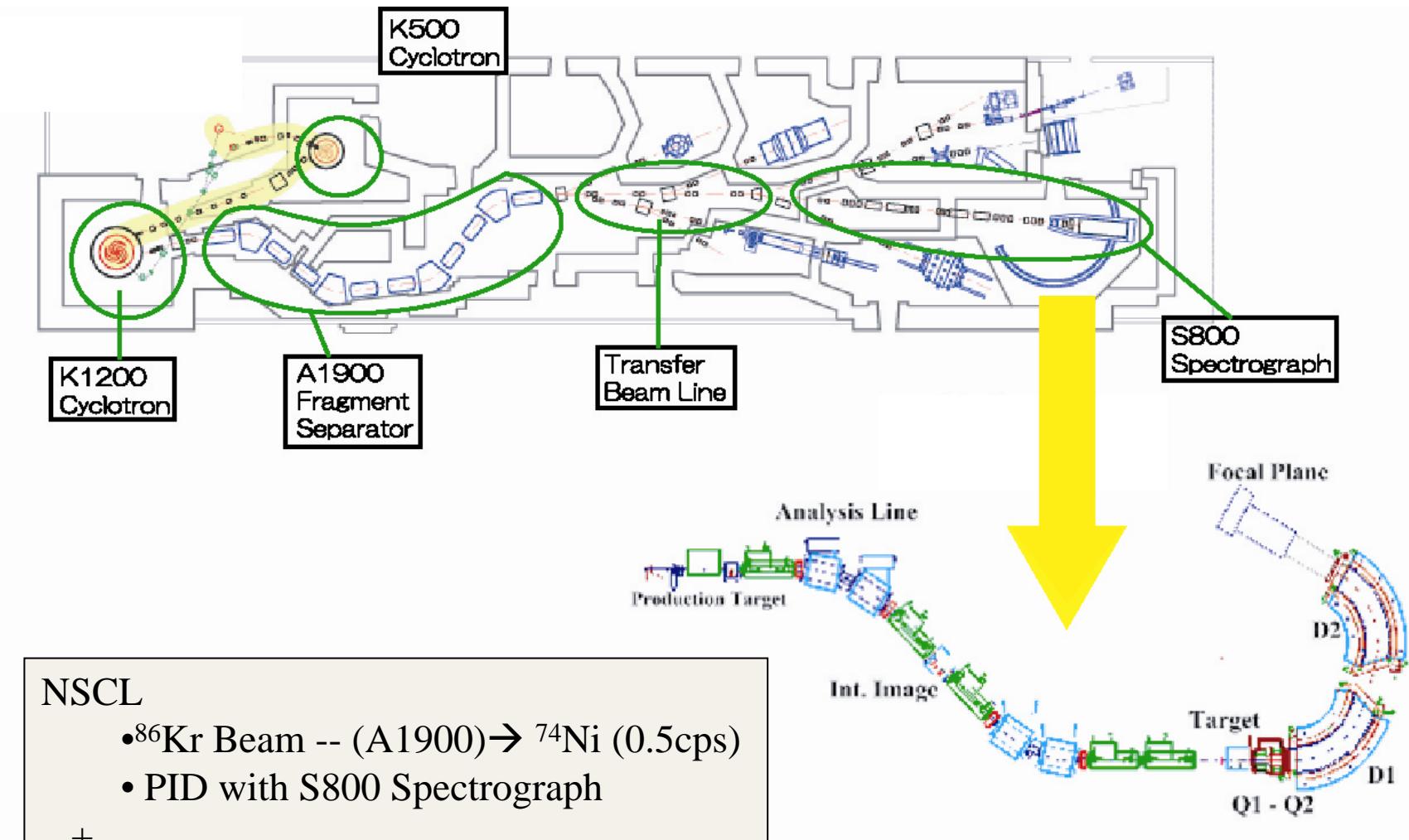
S. Kanno et al.



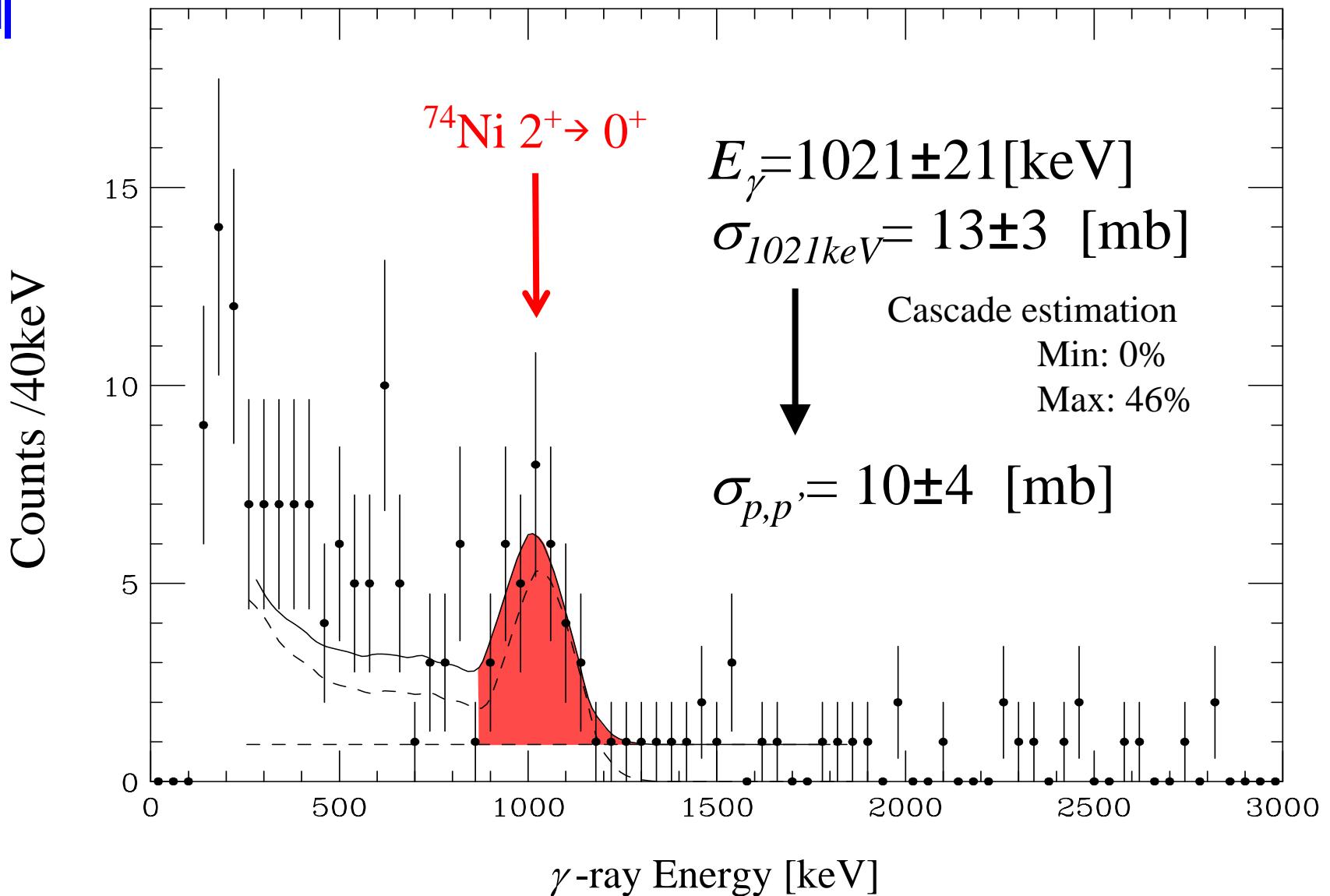
^{74}Ni : $E_x(2^+)$ unknown
 (cf. GANIL gr. @ ENAM04)
 $B(E2)$ unknown
 ^{78}Zn : $E_x(2^+)$ known
 $B(E2)$ unknown



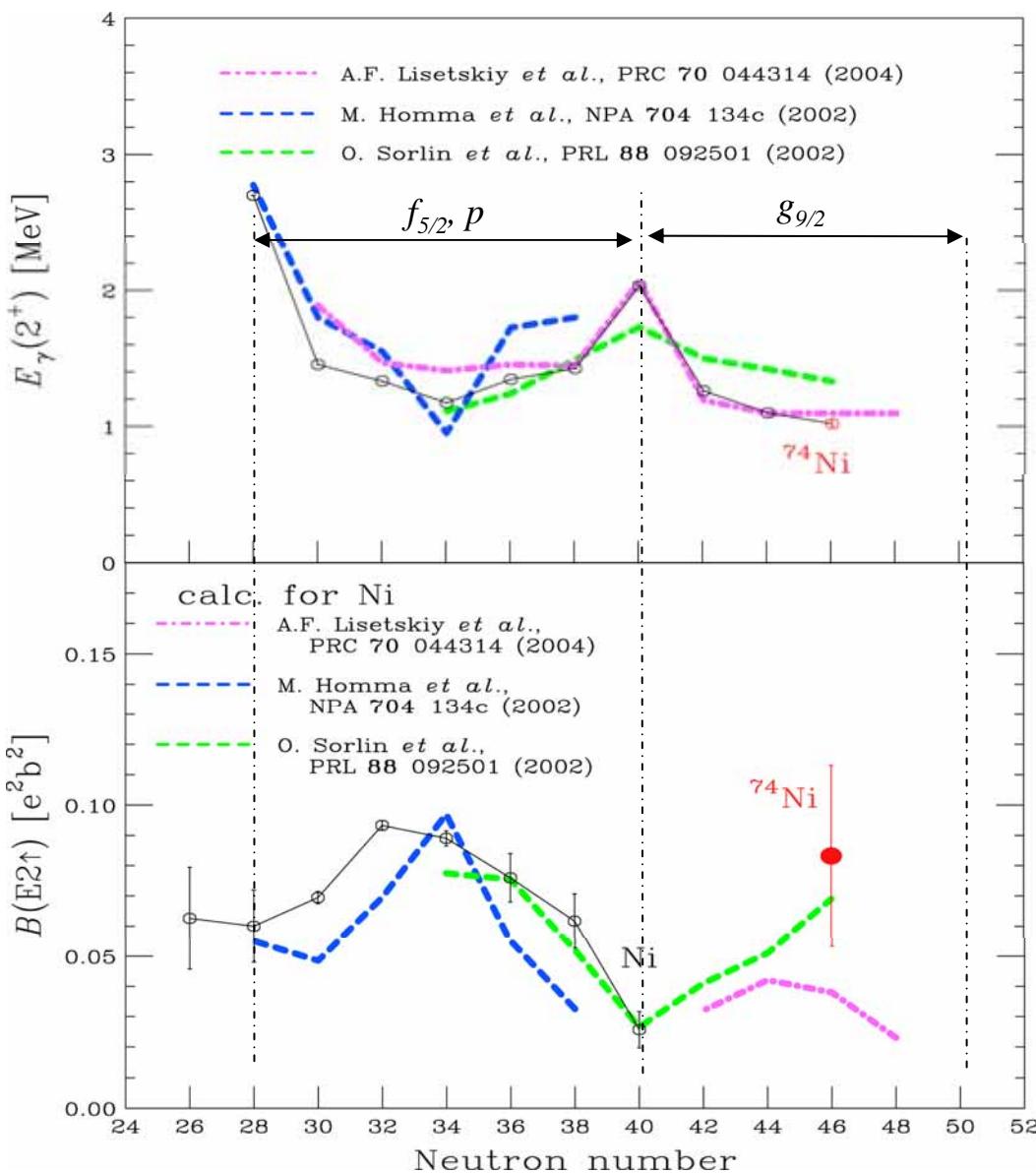
MSU National Superconducting Cyclotron Lab.



$^{74}\text{Ni}(p,p'\gamma)$ γ -ray spectrum



Systematics of $Ex(2^+)$ and $B(E2 \rightarrow 0^+)$ for Ni isotopes



$$\sigma_{p,p} = 10 \pm 4 \text{ [mb]}$$

$$\beta_{p,p} = 0.17 \pm 0.04$$

$$B(E2 \rightarrow 0^+) = 0.08 \pm 0.03 \text{ [e}^2\text{b}^2\text{]}$$

Core; ^{56}Ni

$\nu p_{3/2}p_{1/2}f_{5/2}g_{9/2}$

$$e_n = 1.0e$$

Core; ^{40}Ca (Full pf -shell)

MCSM+FDA+GF40A

$$e_p = 1.23e, e_n = 0.54e$$

Core; ^{48}Ca

$\pi f_{7/2}p_{3/2}p_{1/2}f_{5/2}$

$\nu p_{3/2}p_{1/2}f_{5/2}g_{9/2}$

$$e_p = 1.5e, e_n = 0.5e$$

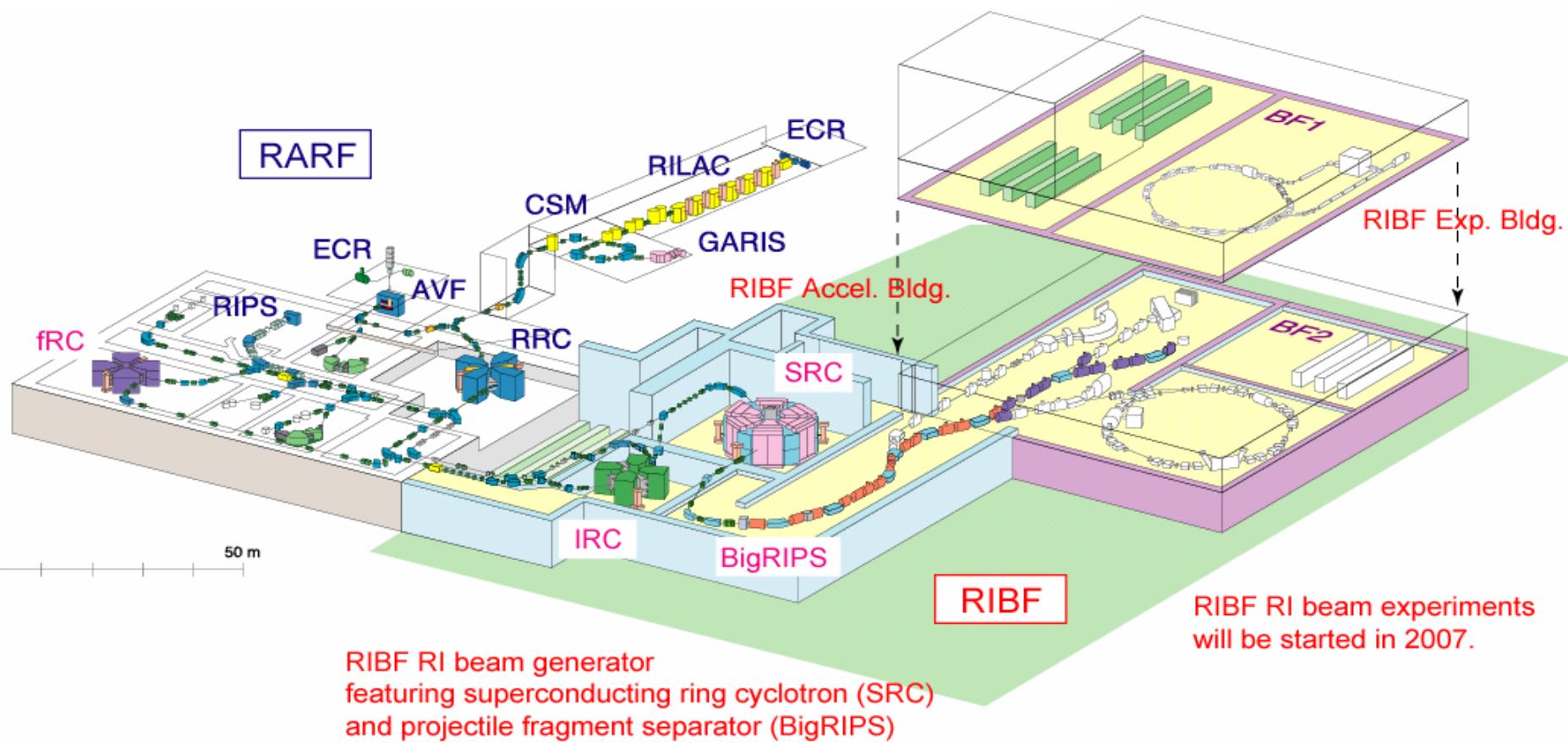
$$(e_{pol} = 0.5)$$

TBME A.Poves et al., NPA 694
157 (2001)



Toward heavier region
at RIBF

Schematic view of RI Beam Factory

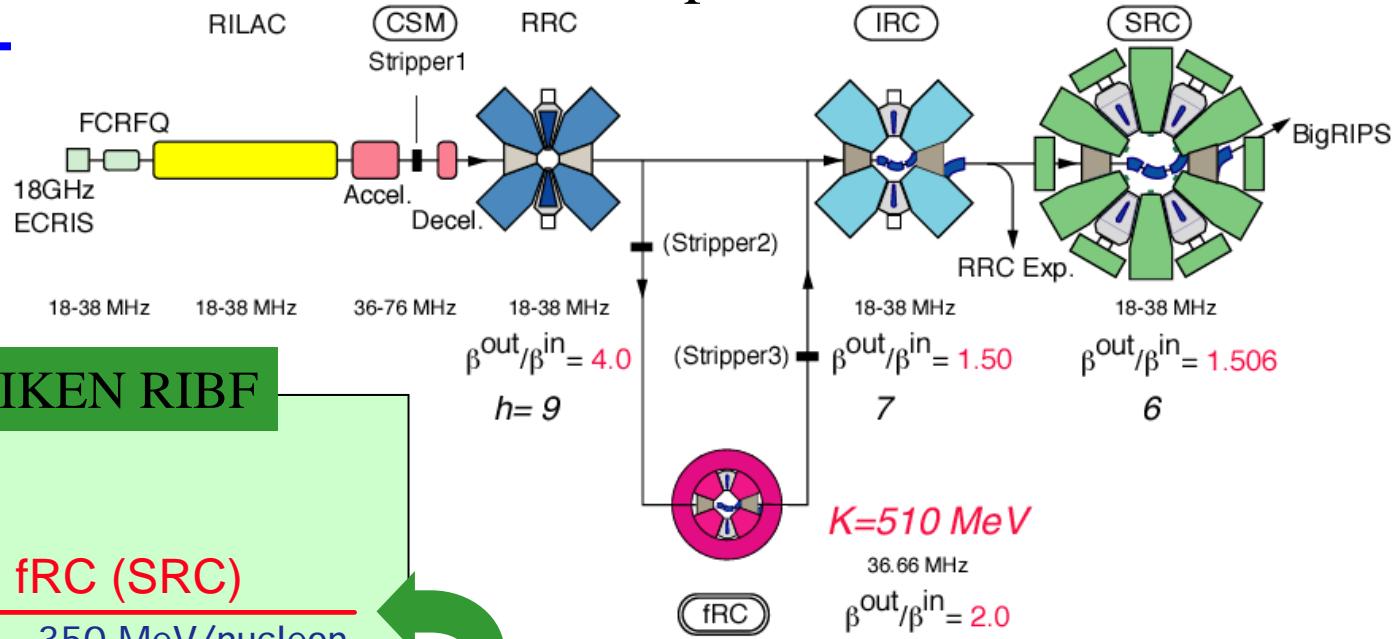


RIBF Accelerator Complex

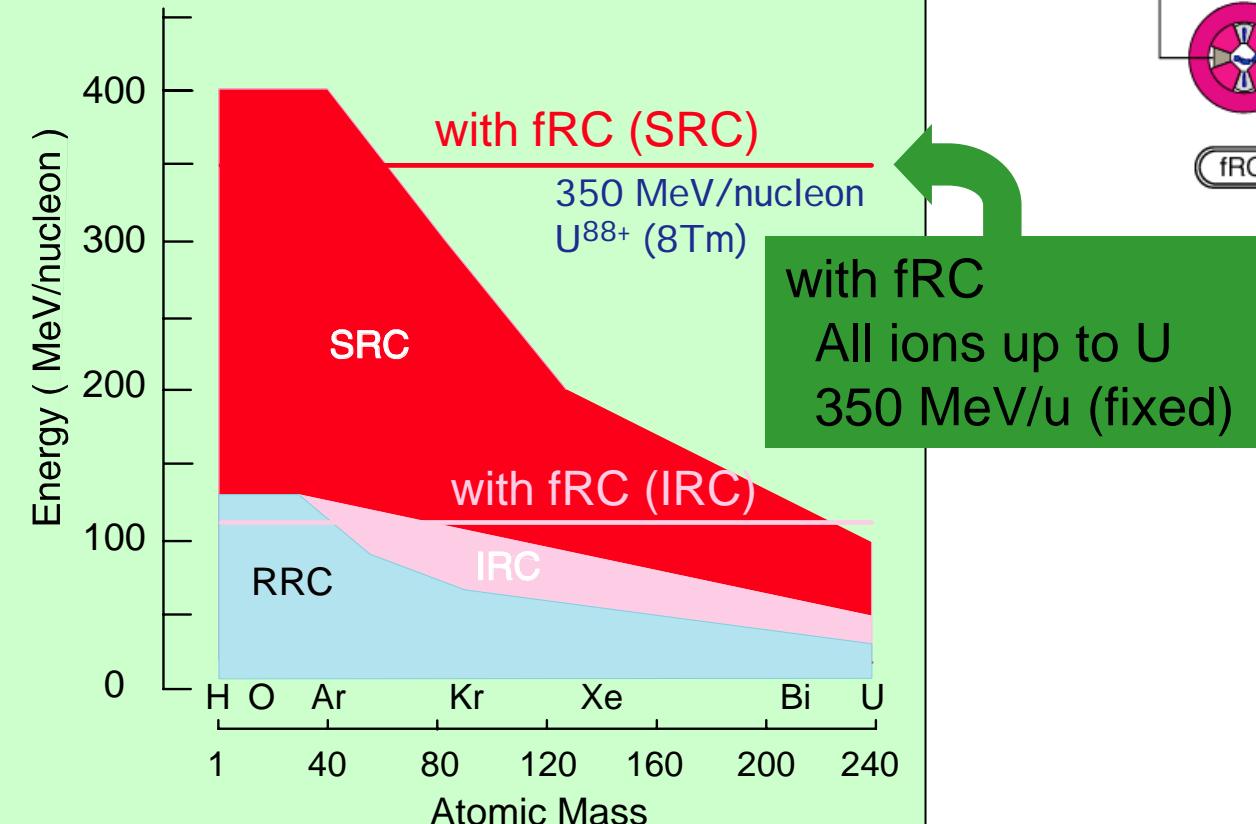
$K=510 \text{ MeV}$

980 MeV

2500 MeV



Max. beam energy at RIKEN RIBF



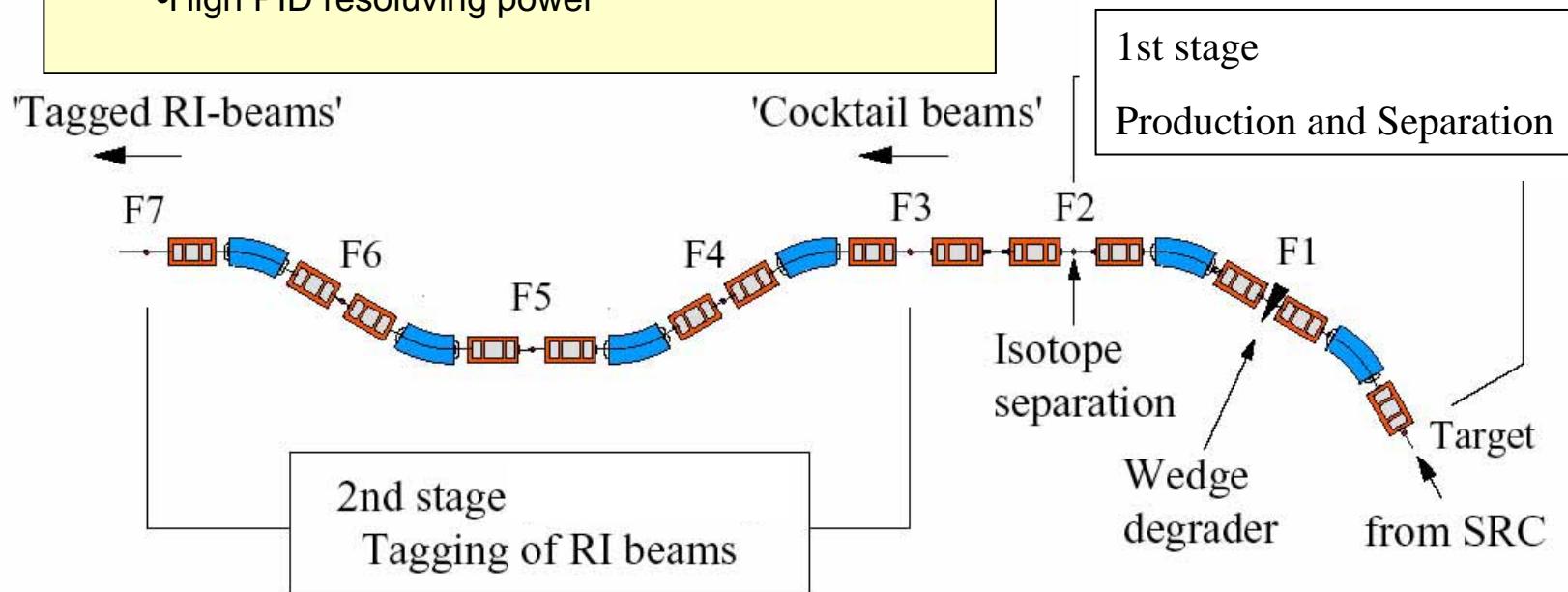
Beam Intensity

goal: $1 p\mu\text{A}$ for all ions
 2007: 10 pnA ^{238}U
 $0.3 p\mu\text{A}$ ^{136}Xe
 $1 p\mu\text{A}$ ^{86}Kr

Fragment Separator BigRIPS

- Production Method
 - Projectile fragmentation
 - In-flight fission of U
- Tandem Separator for TAGGING
 - High PID resolving power

Nucl. Instr. and Meth. B 204 (2003) 97.



TOF, $B\beta$, $\Delta E \rightarrow Z, A/Q (A, Q), P$

Momentum Acceptance	$\pm 3\%$
Angular Acceptance	± 50 mrad
Maximum Rigidity	9 Tm
1 st order resolving power	1290 (Separation section) 3300 (Tagging section)

RIBF

RI Beam Factory : the 3rd generation facility

