

Low-energy radioactive beam experiments for nuclear astrophysics

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Main subject:

Recent experimental studies using low-energy radioactive beams at CNS

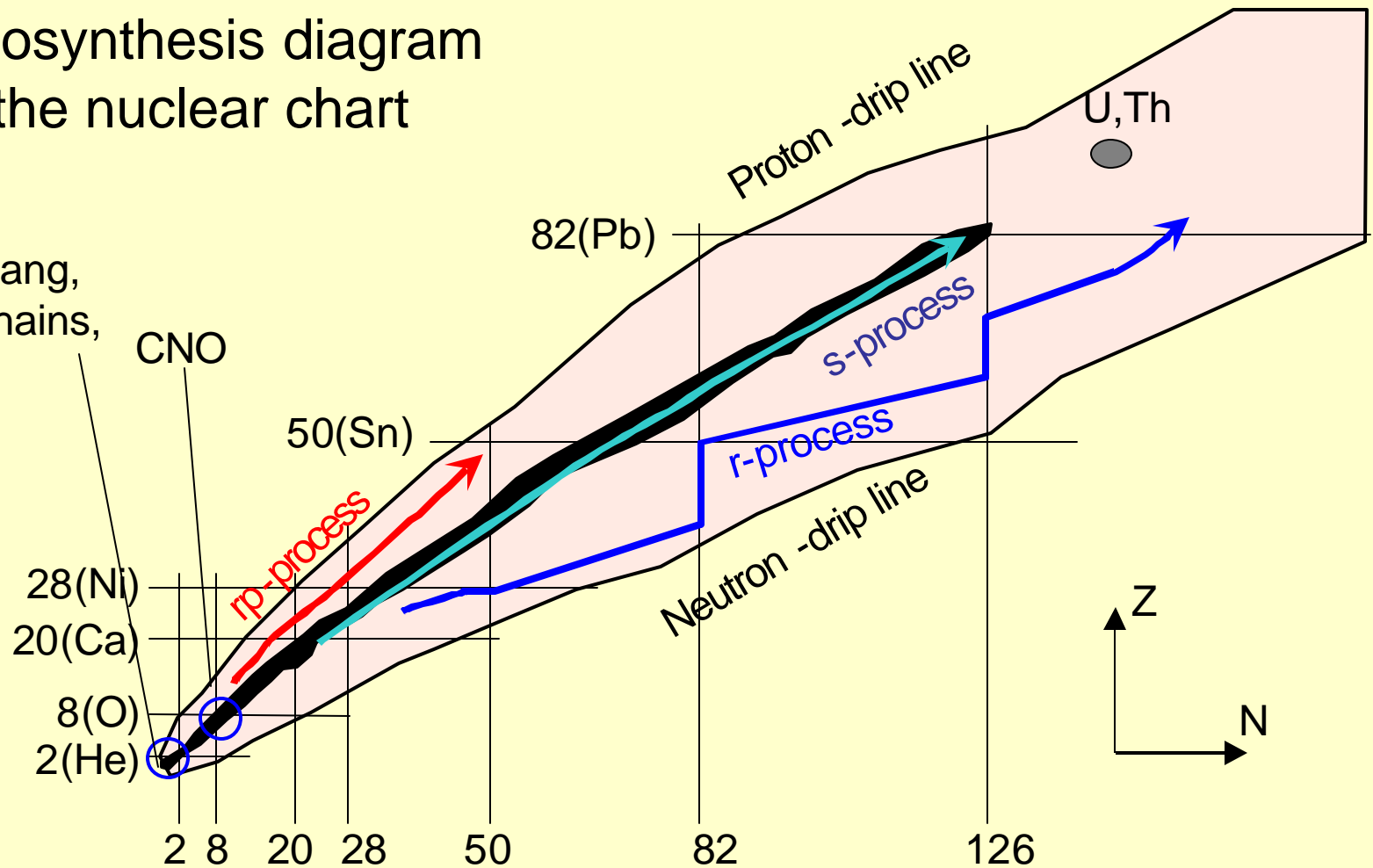
Production of low-energy radioactive nuclear beams

Basic concepts on stellar reaction cross section

Experimental techniques of measuring resonance
scattering to study explosive hydrogen burning

Nucleosynthesis diagram in the nuclear chart

Big-Bang,
p-p chains,
 3α



CNO

50(Sn)

82(Pb)

U,Th

28(Ni)

20(Ca)

8(O)

2(He)

2

8

20

28

50

82

126

Z

N

Proton -drip line

s-process

r-process

Neutron -drip line

rp-process

r-process (rapid neutron capture process) plays a crucial role to produce heavy elements like Uranium and Thorium in super nova explosion.

rp-process (rapid proton capture process) is important in energy generation and nucleosynthesis at high-temperature hydrogen-rich explosive conditions like nova and X-ray burst.

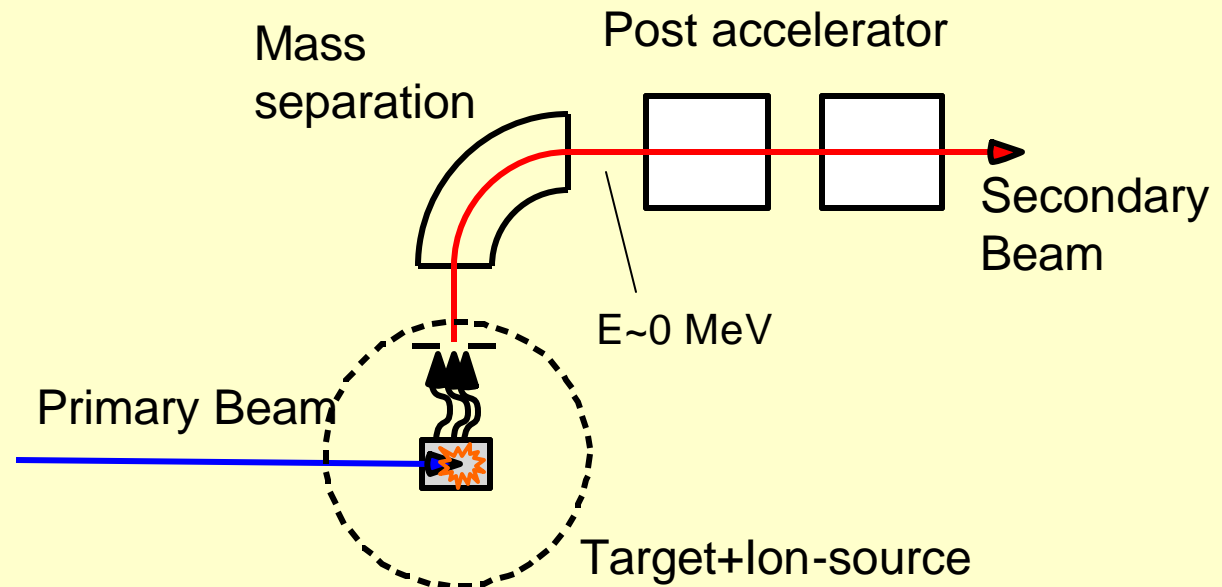
Unstable (neutron- or proton-rich) nuclei play important roles in explosive conditions!

Production of radioactive nuclear beams

Two major techniques for radioactive beam production

1. ISOL (Isotope Separator On-Line)

Reaction products are produced and stopped in a thick production target, which is part of an ion source. The reaction products are re-ionized and re-accelerated as a secondary beam



Good beam quality

Extraction efficiency depends on life time & chemical property

Post-accelerator is necessary

Good for low-energy experiments (for nuclear astrophysics)

Two techniques for radioactive beam production

2. In-Flight Method

Reaction products are emitted from the target into forward angles.
Particles are separated “in-flight” by a separator to have a secondary beam.

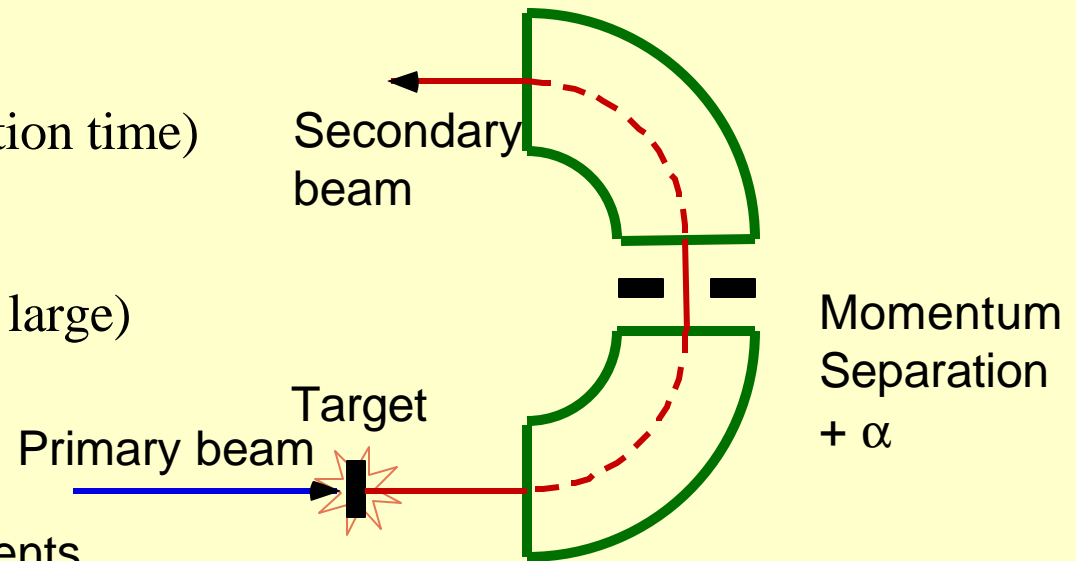
Independent of chemical properties

No problem with life time
(life time \gg beam transportation time)

Bad beam quality
(energy & angular spreads are large)

Good for high-energy experiments

- Projectile-fragmentation reaction at $E > 100$ MeV/nucleon is efficient for production of unstable nuclei far from the stability line
- Target can be thick.



Application to low-energy beams is also useful.

Radioactive Nuclear Beam Facilities

Low-energy (mostly < 5 MeV/nucleon)

ISOL

Leuven-la-Neuve, TRIUMF, ORNL, SPIRAL, REX ISOLDE, TRIAC...

In-flight

NotreDame, TexasA&M, CNS.....

Direct measurements of stellar reactions (at $E < 1$ MeV)

Indirect study of stellar reaction by various low-energy reactions

In future projects, development of high intensity beams ($> 10^9$ pps) and upgrade of beam energy (> 10 MeV/nucleon) are planned.

High-energy, In-flight ($> \sim 100$ MeV/nucleon)

GANIL, GSI, RIKEN, MSU....

Structure, decay, & excitation properties of neutron- and proton-rich nuclei

Coulomb dissociation method for stellar (p, γ) reaction rates

At future facilities (RIBF, RIA, FAIR...), mass, life-time, decay branches for extremely neutron-rich nuclei will be studied for the r-process.

Low-energy beam facility at Center for Nuclear Study (CNS), U-Tokyo

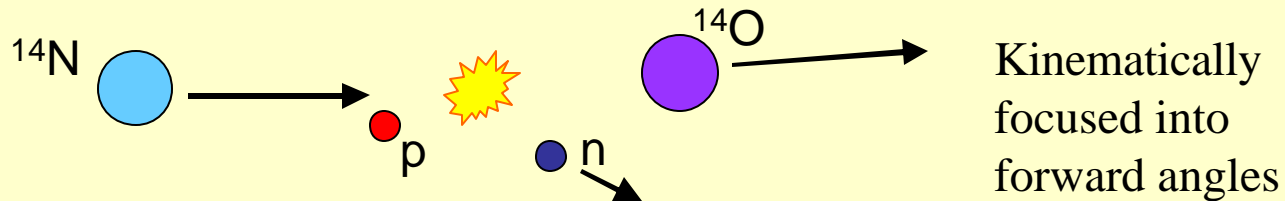
CRIB (CNS low-energy **R**adioactive-**I**on **B**eam separator) 2000~

Low-energy in-flight method

With low-energy high-intensity heavy-ion primary beams
and a large-acceptance particle separator

For example: ^{14}O beam can be produced by

- Primary beam ^{14}N (6+) Intensity 500 pA (3×10^{12} particles/s)
Energy 8.4 MeV/nucleon
- $p(^{14}\text{N}, ^{14}\text{O})n$ reaction Inverse-kinematics (heavy beam + light target)
Cross section ~ 8 mb



- Hydrogen target Methane gas CH_4 in a cell with window foils
1atm. 2 cm (0.3 mg/cm^2)

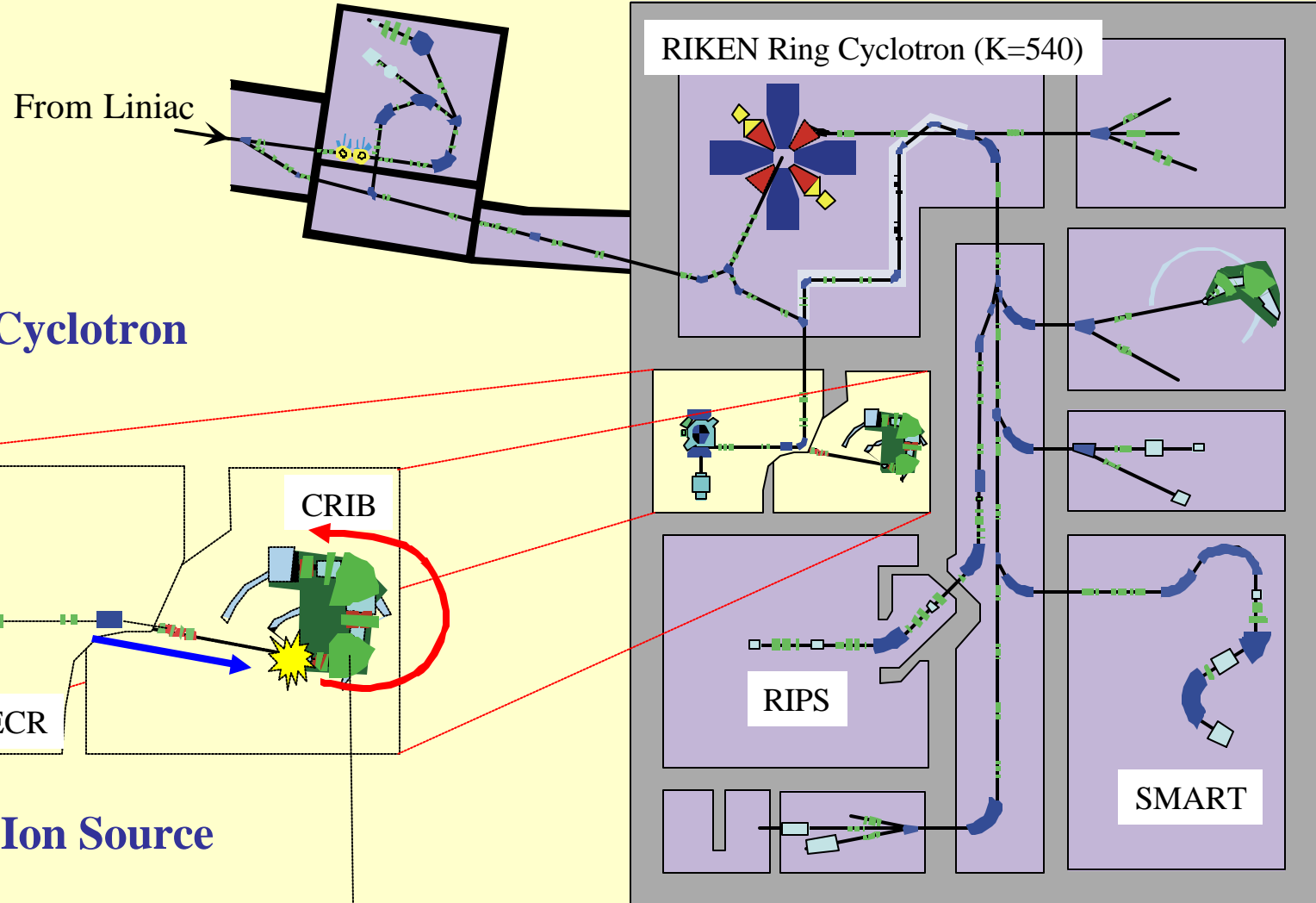
Energy < 7 MeV/nucleon



**^{14}O intensity $2 \cdot 10^6$ particles/sec
(10^7 is possible with a thicker target)**

CNS Low-Energy Radioactive-Beam Line in RIKEN Facility

RIKEN Accelerator Research Facility



CNS In-Flight Radioactive-Ion Beam Separator (CRIB)

RIKEN AVF (azimuthally varying field) cyclotron

K = 70 MeV

Extraction radius 0.714 m

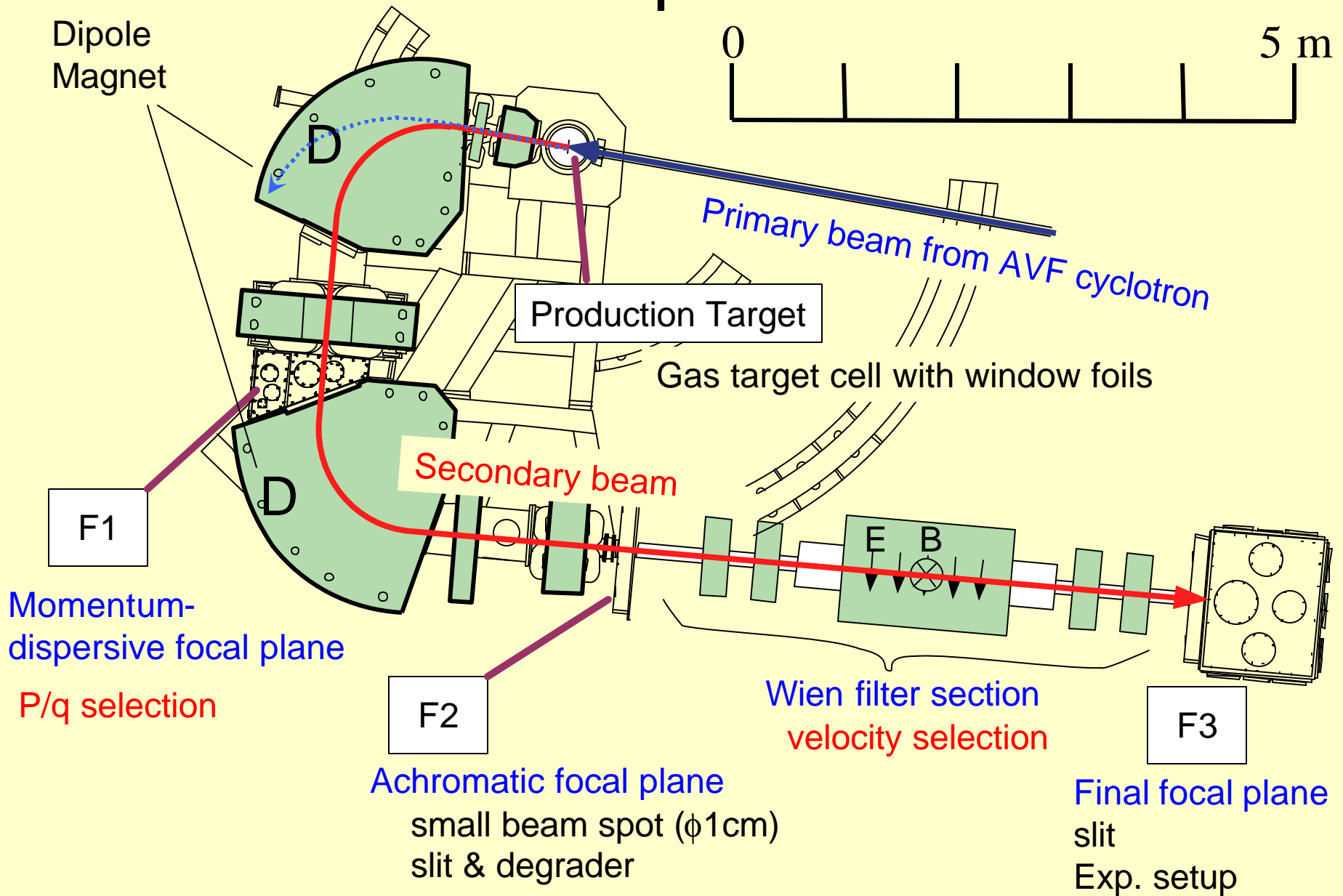
Total weight 110 ton

$$E_{\max} = K \frac{q^2}{A}$$



Modifications & improvements (flat-top cavity, maximum energy upgrade etc) are made by CNS.

CRIB separator

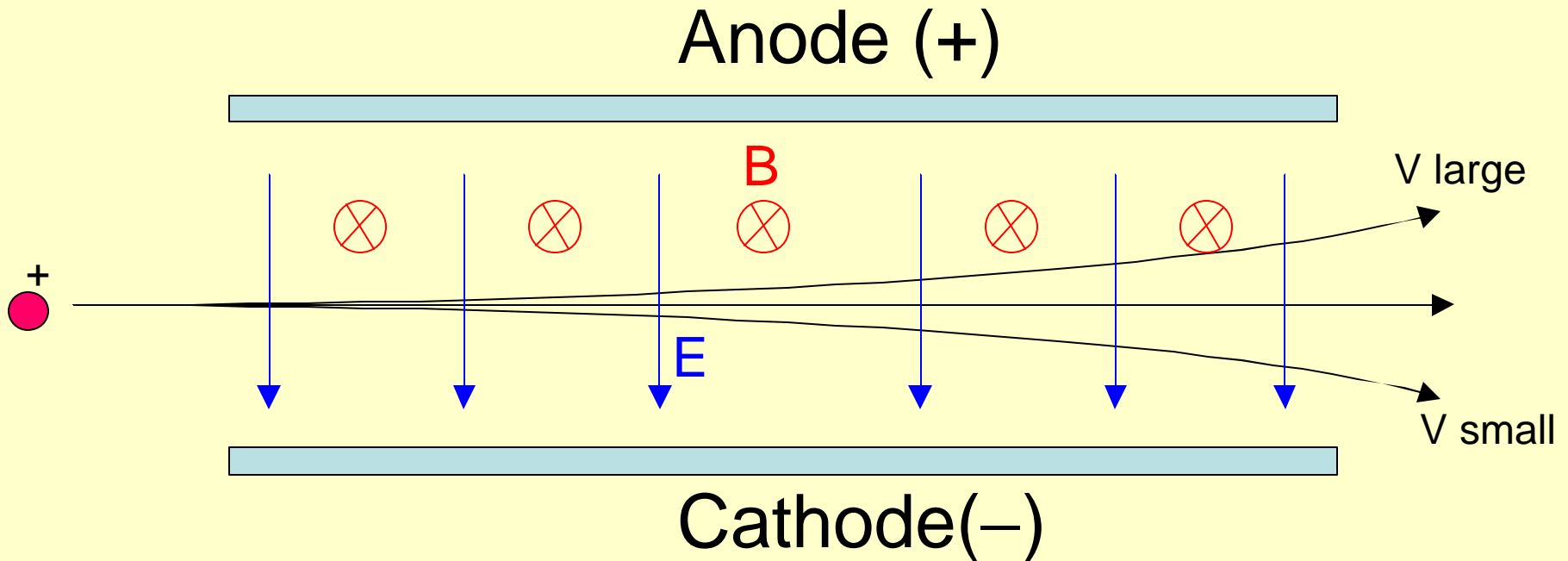


$P/q = \text{const.} \ \& \ v = \text{const.} \ \rightarrow \ m/q \ \text{selection}$

(Z can be separated by using degrader)

Wien Filter

Length of electrodes 1.5 m
Max E field ± 200 kV / 8 cm
Max B field 3 kGauss



Lorentz force

$$qE = qvB$$

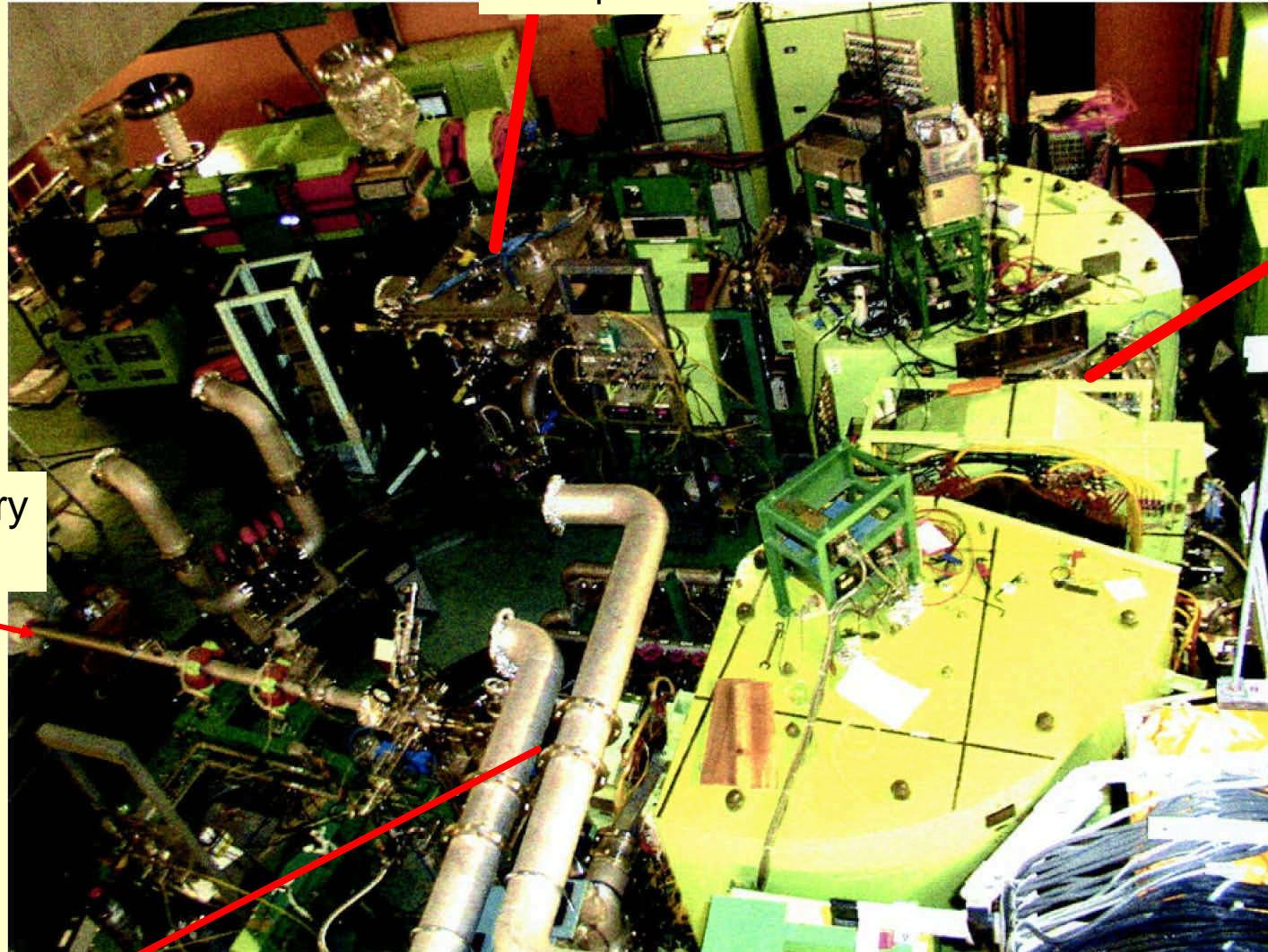
$$v = \frac{E}{B}$$

Velocity selection
Independent of charge and mass

CRIB

F2:
Achromatic
focal plane

In the RIKEN Accelerator Facility



F1:
Dispersive
focal plane

Primary
beam

Target

Production reactions for CRIB (low-energy in-flight method)

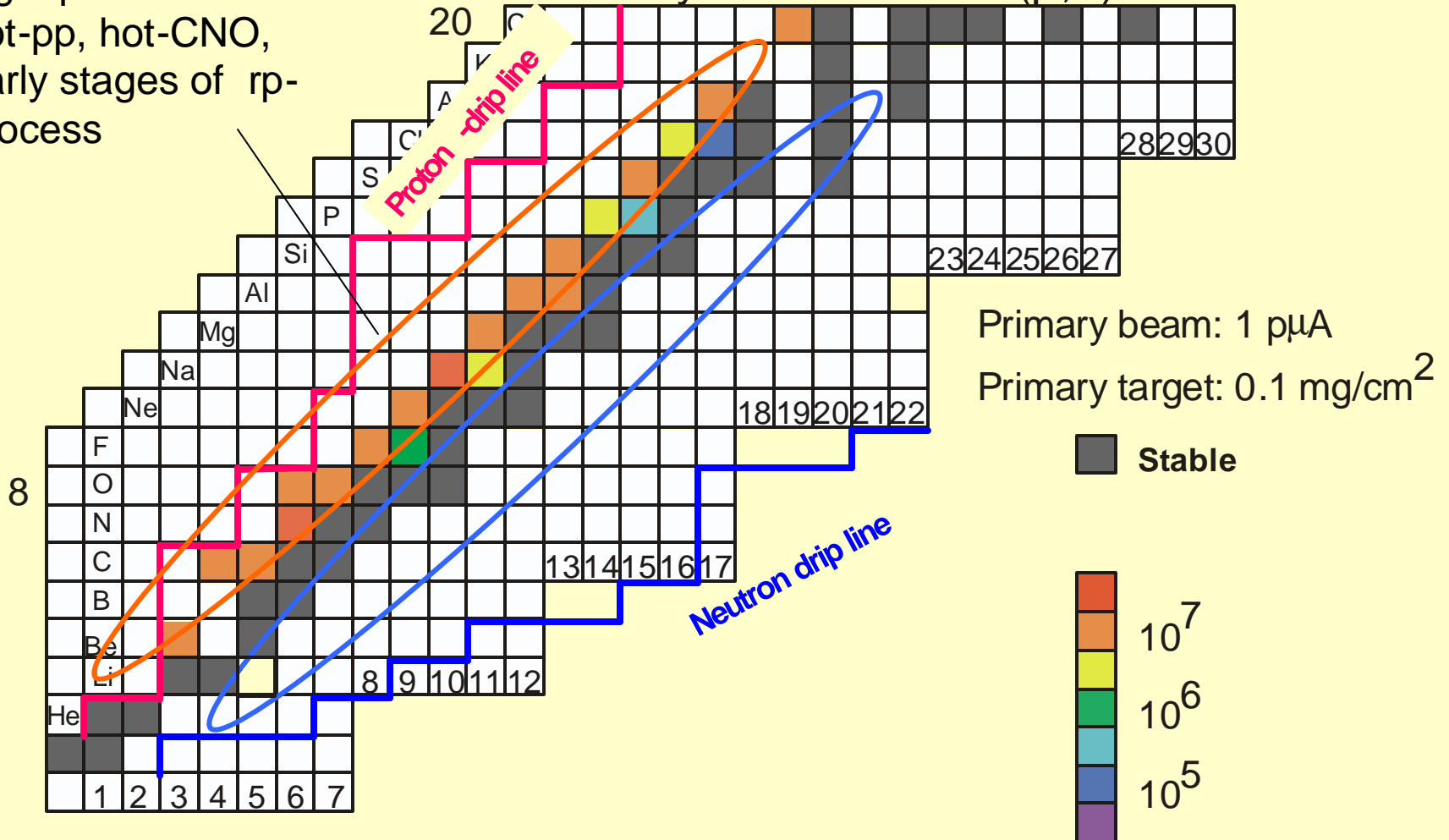
Heavy-Ion beam + light-ion target

Proton-rich nuclei: (p,n), (p,d), (d,n), (d,t), (^3He ,n)....

Neutron-rich nuclei: (d,p), (d, ^3He).....

Light proton-rich nuclei:
hot-pp, hot-CNO,
early stages of rp-
process

Intensity Prediction for (p,n) reactions



Radioactive Beams Produced by CRIB (A<20)

(p,n) reactions ↙

⁷Be 10⁶ pps

¹⁰C 1.6 × 10⁵ pps

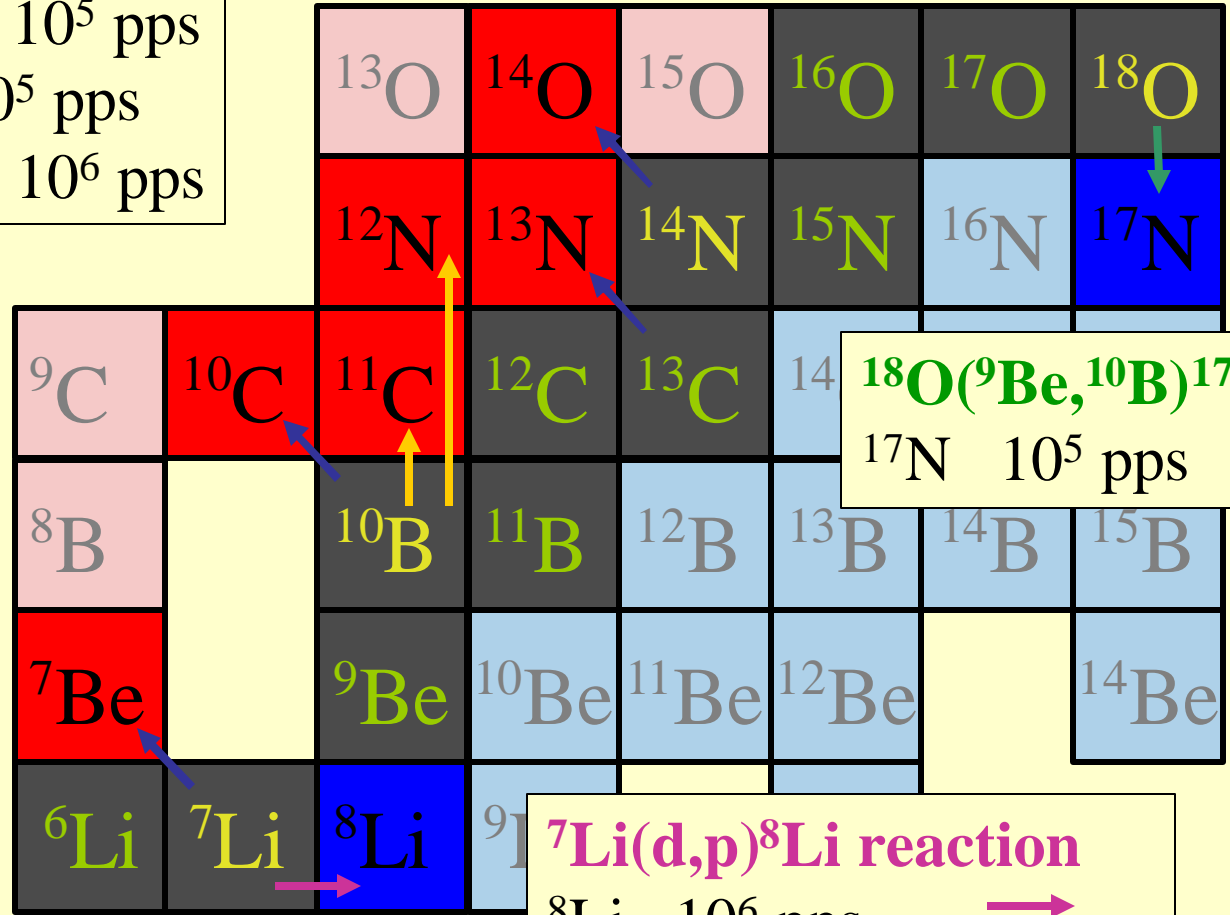
¹³N 2 × 10⁵ pps

¹⁴O 1.7 × 10⁶ pps

(³He,n) & (³He,np) reactions

¹²N 2.5 × 10³ pps ↑

¹¹C 1.7 × 10⁴ pps ↑



¹⁸O(⁹Be,¹⁰B)¹⁷N reaction

¹⁷N 10⁵ pps ↓

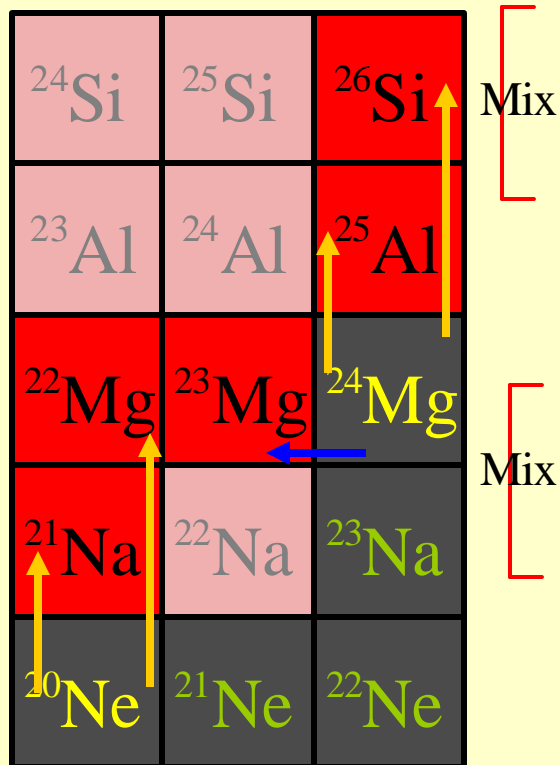
⁷Li(d,p)⁸Li reaction

⁸Li 10⁶ pps →

■ Stable nuclei

Radioactive Beams Produced by CRIB (A>20)

Secondary Beam	Primary Beam	Reaction	Target	Intensity	Purity
^{21}Na 4.2 A MeV	$^{20}\text{Ne}^{8+}$ 200 pnA	$(^3\text{He},n\text{p})$	^3He gas 0.25 mg/cm ²	$2.3 \cdot 10^4$ pps	12 %
^{22}Mg 4.6 A MeV	$^{20}\text{Ne}^{8+}$ 200 pnA	$(^3\text{He},n)$	^3He gas 0.25 mg/cm ²	$6.6 \cdot 10^3$ pps	3 %
^{25}Al 4.0 A MeV	$^{24}\text{Mg}^{8+}$ 125 pnA	$(^3\text{He},n\text{p})$	^3He gas 0.25 mg/cm ²	$1.2 \cdot 10^4$ pps	6 %
^{26}Si 4.0 A MeV	$^{24}\text{Mg}^{8+}$ 125 pnA	$(^3\text{He},n)$	^3He gas 0.25 mg/cm ²	$3 \cdot 10^3$ pps	1.5 %
^{23}Mg 4.0 A MeV	$^{24}\text{Mg}^{8+}$ 125 pnA	(d,t)	D_2 gas 0.33 mg/cm ²	$3.2 \cdot 10^4$ pps	12 %



Hydrogen burning in stars

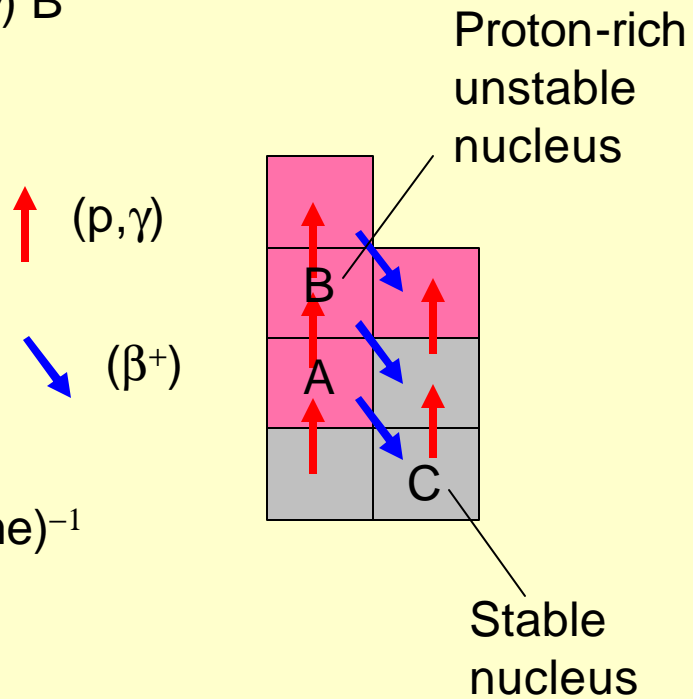
Quiet burning in stars pp-chains, CNO cycle etc.

Explosive burning
in nova or X-ray burst Hot-CNO, ..., rp-process

Radiative proton capture reaction on nucleus A $A(p, \gamma) B$

If A is a proton-rich unstable nucleus, $A(p, \gamma)B$ reaction competes with beta decay $A(\beta^+)C$

$A(p, \gamma)B$	$A(\beta^+)C$
Reaction rate	Decay rate = (life time) ⁻¹



Important to study (p, γ) reaction rates on proton-rich nuclei to understand explosive hydrogen burning

Formalism of reaction cross section

At low energies, the cross section can be approximated by

$$\sigma(E) = E^{-1} \exp(-2\eta) S(E)$$

where

$$\propto \pi \lambda^2$$

Probability for penetration through the Coulomb barrier (for the A+p system)

$$\eta = \frac{Z_1 Z_2 e^2}{\hbar v}$$

Coulomb parameter

$S(E)$:

Astrophysical S-factor

lower E → smaller $\sigma(E)$

Direct (non-resonant) capture $A+p \rightarrow B+\gamma$ $S(E)$ varying slowly with E

Resonant capture $A+p \rightarrow B^* \rightarrow B+\gamma$ $S(E)$ enhanced very much around resonance energy

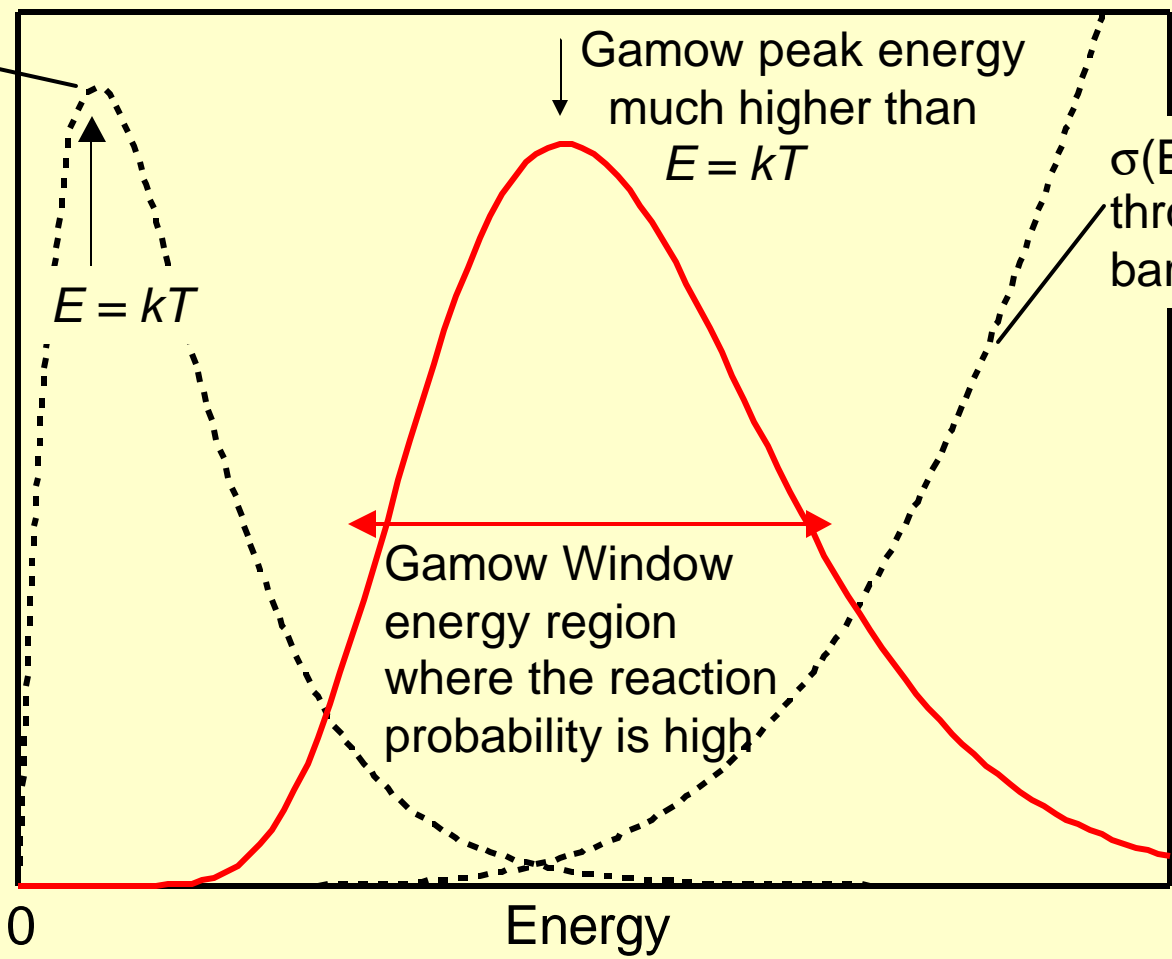
Resonance contributions are important

Non-resonant reaction rate

Reaction rate

$$\langle \mathbf{sv} \rangle \propto \int_0^\infty \mathbf{s}(E) E \exp\left(-\frac{E}{kT}\right) dE = \int_0^\infty \exp\left(-\frac{E}{kT}\right) \exp(-2\mathbf{ph}) S(E) dE$$

Maxwell-Boltzman Distribution



Gamow peak energy much higher than $E = kT$

$\sigma(E) \propto$ Penetration through Coulomb barrier

Gamow Window energy region where the reaction probability is high

0

Energy

Resonant capture cross section

Breit-Wigner formula for an isolated resonance



$$\sigma(E) = \pi \lambda^2 \omega \frac{\Gamma_p \Gamma_\gamma}{(E - E_R)^2 + (\Gamma/2)^2}$$

where

$$\omega = (2J+1)/(2J_1+1)/(2J_2+1)$$

Spin J_1, J_2, J of A, p, B^*

$$\Gamma_p, \Gamma_g$$

Proton & Gamma partial widths

$$\Gamma = \Gamma_p + \Gamma_g + \dots$$

Total width

Maximum cross section at $E = E_R$ $\mathbf{s}_{BW}(E_R) \propto \frac{\Gamma_p \Gamma_g}{\Gamma^2}$

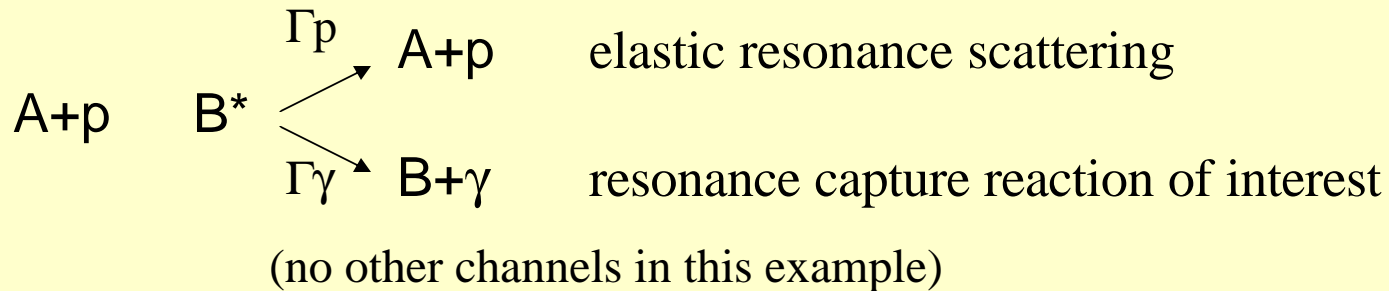
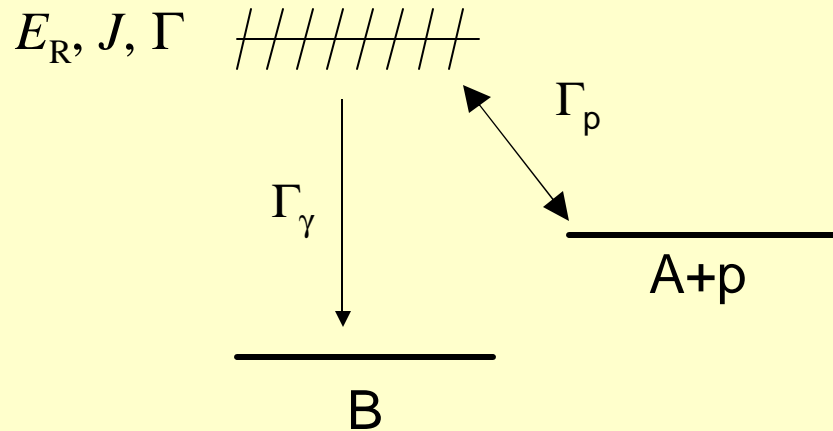
Reaction rate

$$\langle \sigma v \rangle \propto \int_0^\infty \sigma(E) E \exp\left(-\frac{E}{kT}\right) dE \propto \omega \frac{\Gamma_p \Gamma_\gamma}{\Gamma} \exp\left(-\frac{E}{kT}\right)$$

Low-lying resonances ($E \sim 0$) are important!

For stellar (p,γ) reactions of interest, often $\Gamma \sim \Gamma_p \gg \Gamma_\gamma$

Study of resonances above proton threshold



Because of $\Gamma_p \gg \Gamma_\gamma$, the resonance scattering is much easier to measure than the resonance capture reaction .

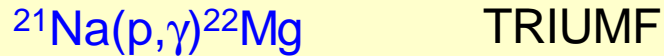
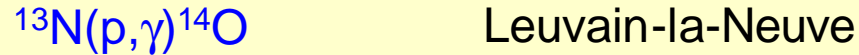
Resonance scattering experiment is useful to study the resonance

→ resonance information $E_R, J, \Gamma \sim \Gamma_p$

(However, Γ_γ can not be determined experimentally.)

Experiments with radioactive beams to study (p,γ) reactions

Direct measurement with radioactive beams at energies < ~ 1 MeV



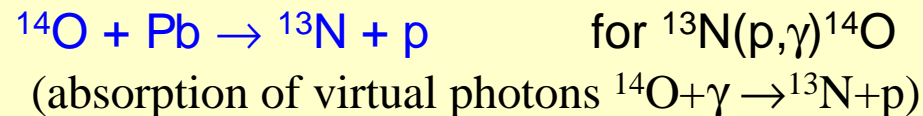
beam intensity > 10^8 pps required!

Indirect studies with larger cross sections

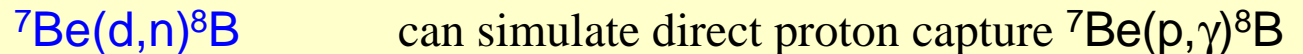
Resonance search: (at low-energy facilities)



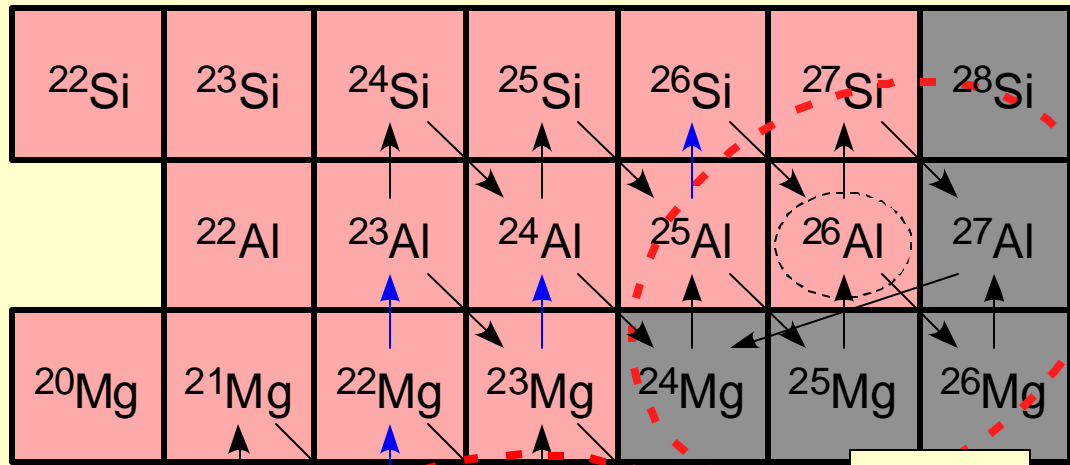
Coulomb breakup: (at high-energy facilities)



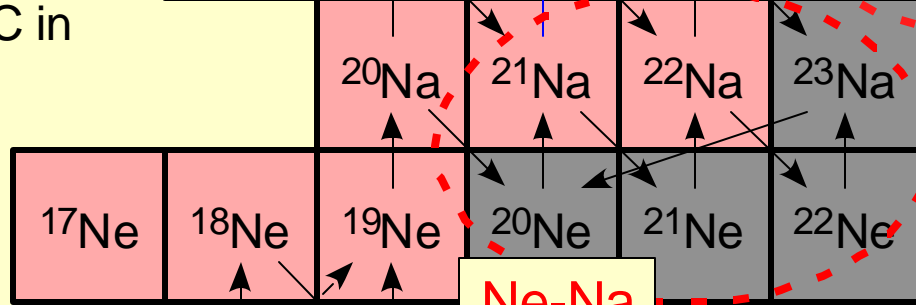
ANC (Asymptotic Normalization Coefficient) method (low-energy)



Experiments at CNS (2002—2005)



Mg-Al

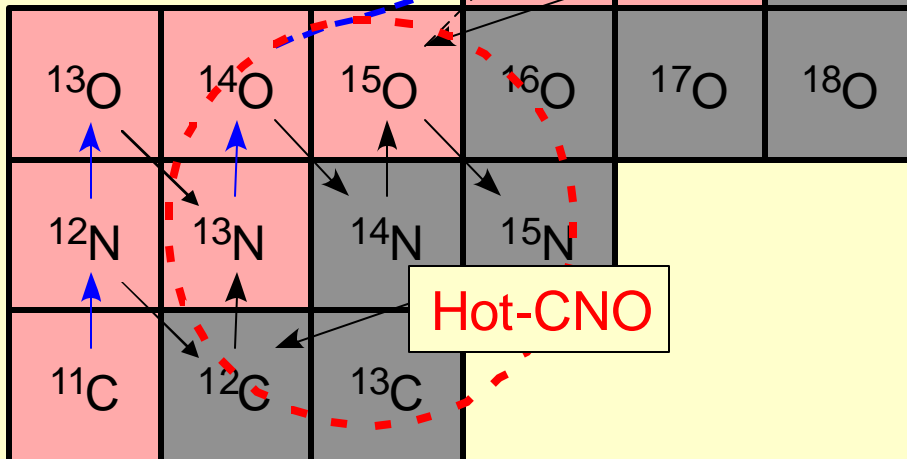


Ne-Na

Resonance search

$^{21}\text{Na}(p,p)^{21}\text{Na}$ $^{22}\text{Mg}(p,p)^{22}\text{Mg}$
 $^{23}\text{Mg}(p,p)^{23}\text{Mg}$ $^{25}\text{Al}(p,p)^{25}\text{Al}$

(p,γ) reactions break out from Ne-Na&Mg-Al into rp-process.
 Production of ^{26}Al ($t_{1/2}=7\times 10^5$ y)



Hot-CNO

Resonance search

$^{11}\text{C}(p,p)^{11}\text{C}$
 $^{12}\text{N}(p,p)^{12}\text{N}$

(p,γ) reactions in the hot-pp chain which may bypass $3\alpha \rightarrow ^{12}\text{C}$ in metal-poor massive stars.

Direct measurement

$^{14}\text{O}(\alpha,p)^{17}\text{F}$
 breaks out from Hot-CNO into rp-process

Resonance search

$^{13}\text{N}(p,p)^{13}\text{N}$

Hot-CNO.
 Resonances at higher energies

Experimental technique for the $A+p$ elastic resonance scattering

A: proton-rich unstable nucleus

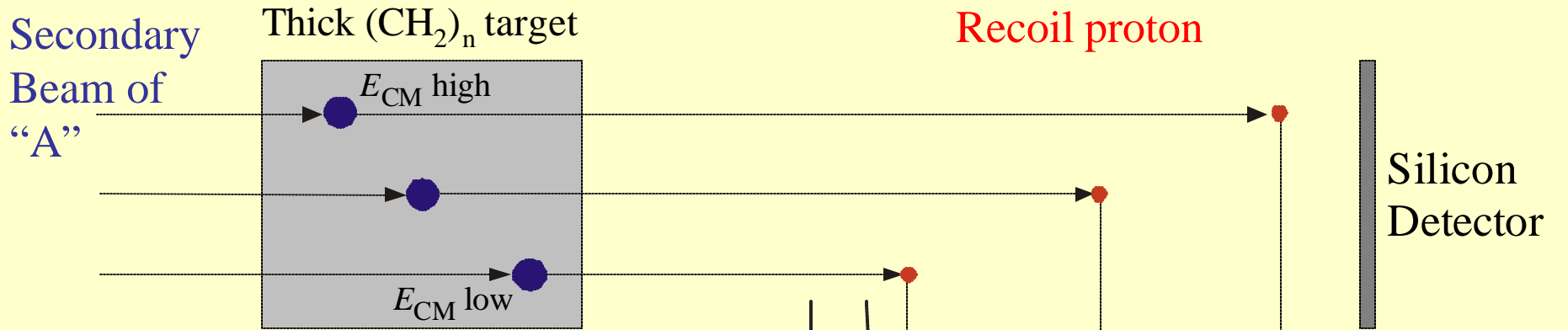
a low-energy beam of $E < \sim 4$ MeV/nucleon

p: proton

a target of polyethylene $(\text{CH}_2)_n$

In inverse kinematics

Thick-target method for A+p in inverse kinematics



- **Thick proton target**

Energy loss of the beam

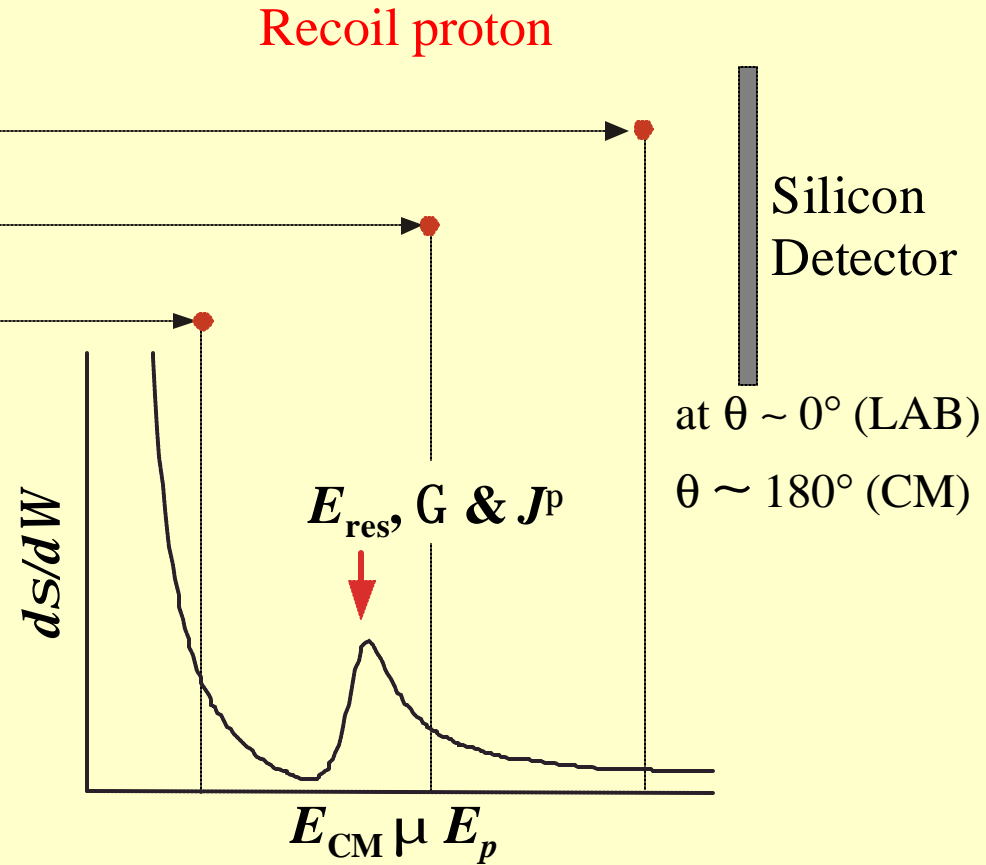
Scanning $ds/dW(E)$ automatically

Without changing the beam energy before the target

Proton yield $\propto ds/dW$

$$\frac{dN}{dE} \propto \frac{dS}{d\Omega} \cdot \frac{dx}{dE} \cdot d\Omega$$

Counts per energy-bin Target-thickness per energy-bin

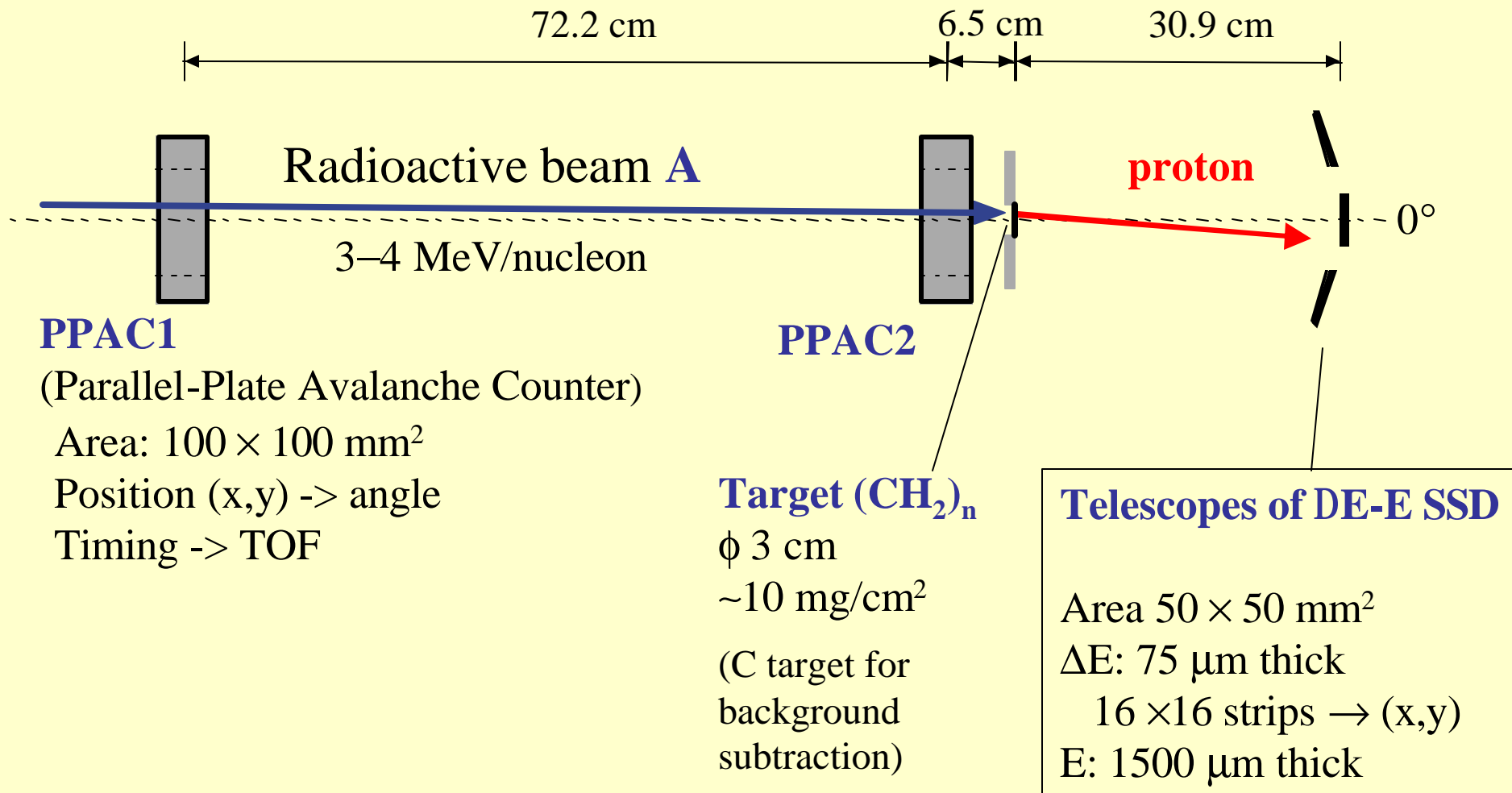


Excitation function $d\sigma/d\Omega(E)$

Interference pattern of potential & resonance scattering

Setup for A+p

at CRIB F2 or F3



The beam stops in the target.

Recoil protons come out from the target.

Reconstruction of CM Energy

$$E_{\text{CM}} = \frac{1}{4 \cos^2 \mathbf{q}_p} \frac{A+1}{A} E_p$$

A : mass number of projectile

E_p : energy of proton in LAB

By SSD

Resolution of 100 keV (FWHM)

\mathbf{q}_p : angle of proton in LAB

By PPACs & SSD (double-sided strips)

Resolution of 0.5 deg (FWHM)

E_{CM} is deduced from E_p & \mathbf{q}_p on an event-by-event basis
(energy loss in the target taken into account)

E_p resolution of 80 keV

→ E_{CM} resolution of 20 keV (FWHM) at $\mathbf{q}_p = 0$

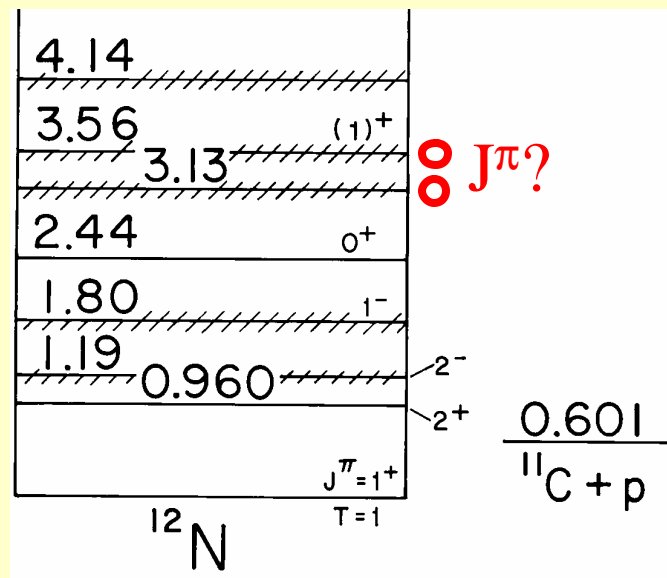
(Contribution from energy straggling of proton in the target is small.)

$^{11}\text{C} + \text{p}$ Experiment

J^π for the 3.13 & 3.56-MeV levels ?

Verifying known values of E_R , Γ ($\sim \Gamma_p$), J^π

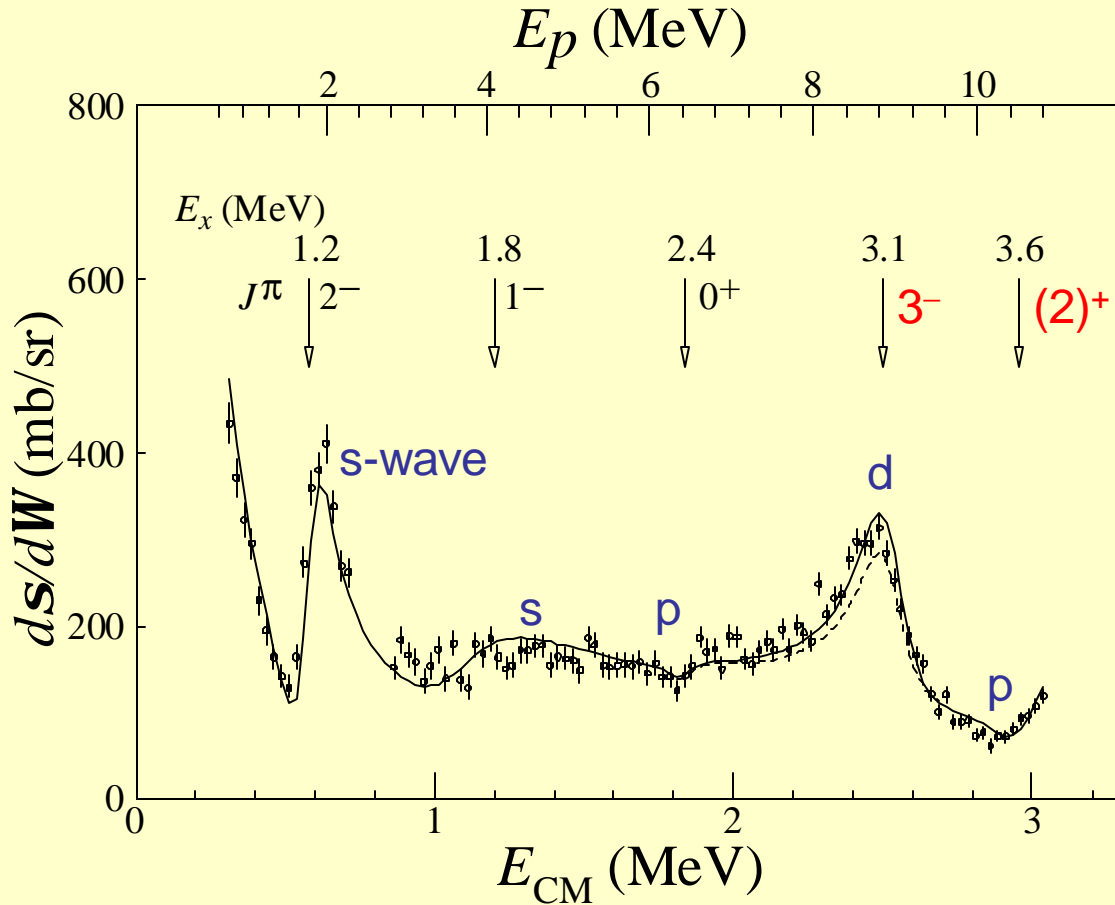
For the astrophysical $^{11}\text{C}(\text{p},\text{g})^{12}\text{N}$ reaction rates (Hot-PP)



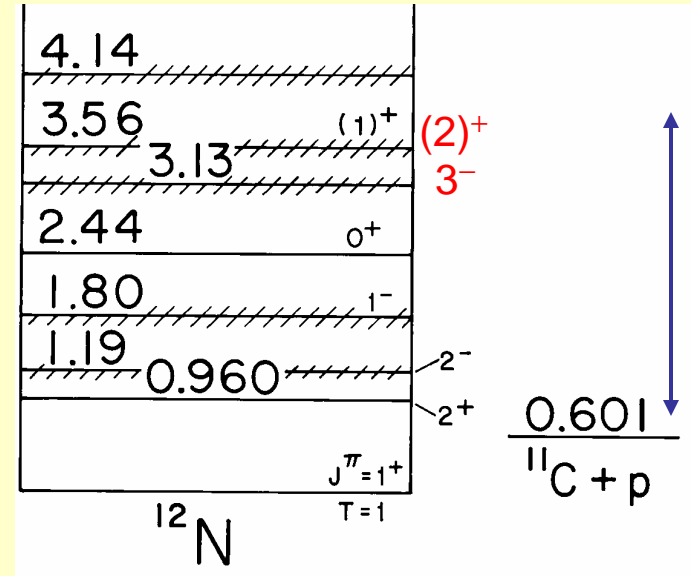
Result: $^{11}\text{C}+p$ ($^{12}\text{N}^*$) elastic resonance scattering

Resonances relevant to $^{11}\text{C}(p,\gamma)^{12}\text{N}$

T. Teranishi et al., PLB 556 (2003) 27



Solid line (R-matrix)



E & Γ are consistent width known values.

The 2⁺ level at 0.96 MeV & 2⁻ level at 1.2 MeV are important for the $^{11}\text{C}(p,\gamma)^{12}\text{N}$ reaction.

J^π = 3⁻ newly assigned to the 3.13-MeV level

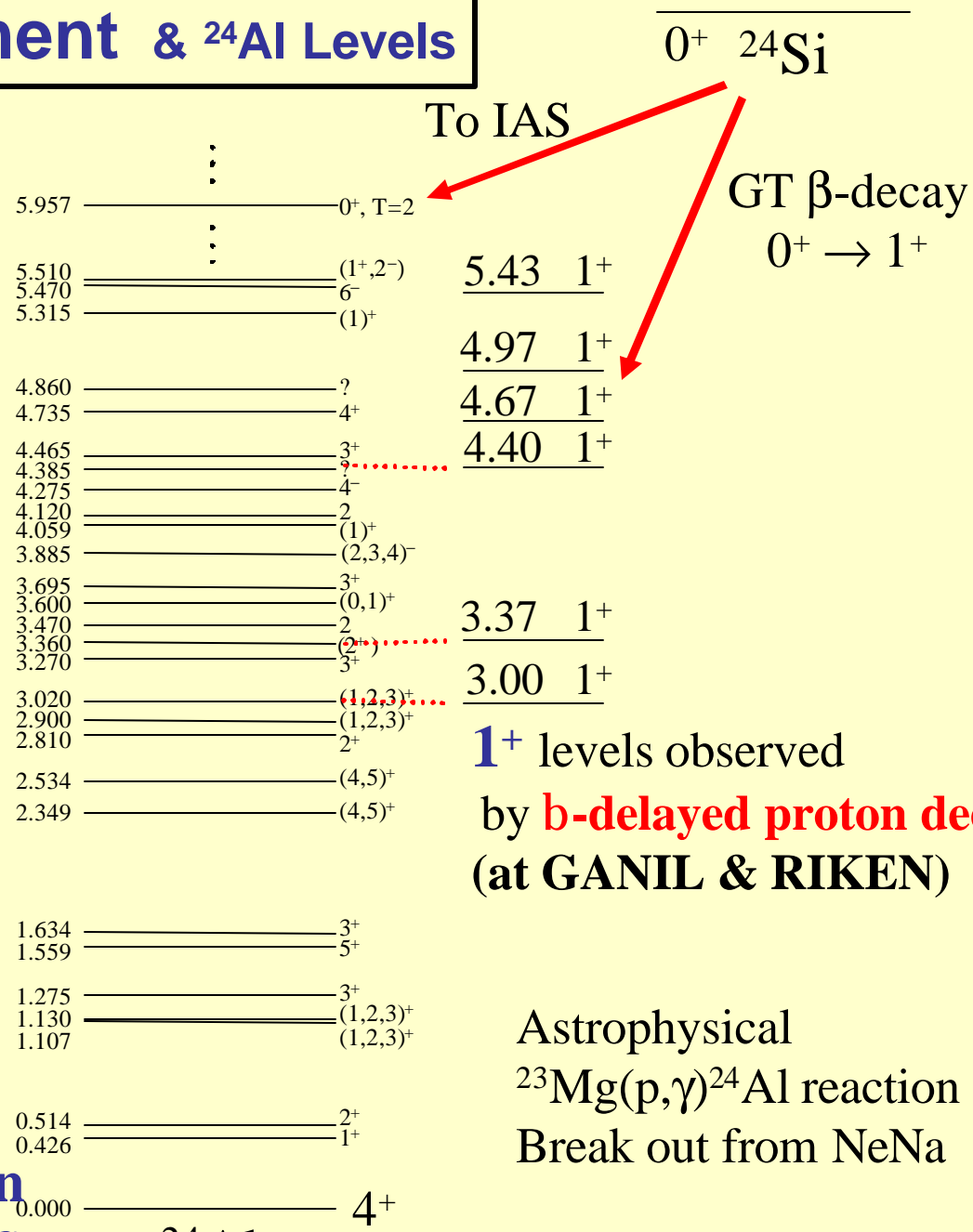
does not contribute to the (p,g) reaction so much because of the M2 transition 3⁻ → 1⁺(g.s).

$^{23}\text{Mg}+p$ experiment & ^{24}Al Levels

s-wave resonance
 $\rightarrow 1^+$ or 2^+

Elastic scattering

1.871
 $^{23}\text{Mg}+p$
 $3/2^+ \quad 1/2^+$



To IAS

GT β -decay
 $0^+ \rightarrow 1^+$

1^+ levels observed
 by **b-delayed proton decay**
 (at GANIL & RIKEN)

Astrophysical
 $^{23}\text{Mg}(p, \gamma)^{24}\text{Al}$ reaction
 Break out from NeNa

Mg beams are difficult for ISOL

Many of J^P uncertain

No exp data of G ($\sim G_p$)

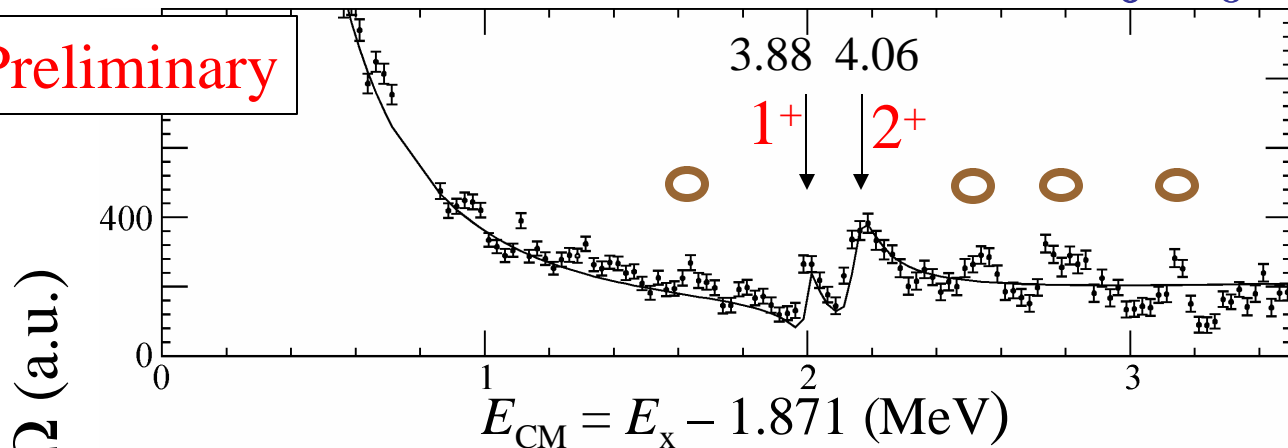
^{24}Al

Spectra of $^{23}\text{Mg}+p$ ($^{24}\text{Al}^*$)

Detector #1

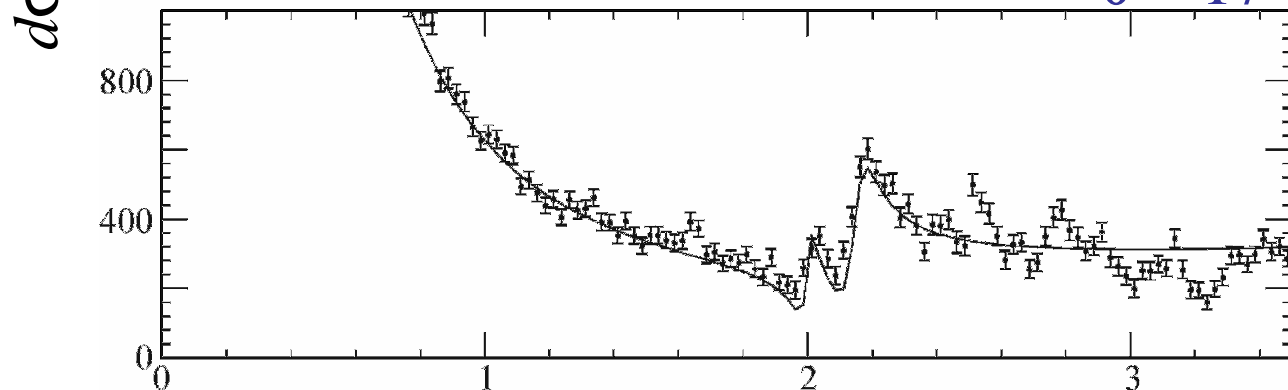
$\theta = 0^\circ$

Preliminary



Detector #2

$\theta = 17^\circ$



$E_x =$
2.4—5.3 MeV

1.871
 $^{23}\text{Mg}+p$
3/2+ 1/2+

0 4+

^{24}Al

Solid line: R-matrix fit

s-wave assumed for levels at

$E_x = 3.88 \text{ MeV} \ \& \ 4.06 \text{ MeV}$ (J^π not well known before)

Peak height depends on J value.

® 1^+ for 3.88 MeV & 2^+ for 4.06 MeV (preliminary)

^{24}Al Levels
 Above
 Proton Threshold
 of $E_x = 1.871$ MeV

Latest Compilation
 NPA633(1998)1

Ex (MeV)	J^π
2.349	(4,5) ⁺
2.534	(4,5) ⁺
2.810	2 ⁺
2.900	(1—3) ⁺
3.020	(1—3) ⁺
3.270	3 ⁺
3.360	(2) ⁺
3.470	2
3.600	(0,1) ⁺
3.695	3 ⁺
3.885	(2—4) ⁻
4.059	(1) ⁺
4.120	2
4.275	4 ⁻
4.385	
4.465	3 ⁺
4.735	4 ⁺
4.860	

○

○

○

$^{24}\text{Si}(\beta)^{24}\text{Al}^* \rightarrow ^{23}\text{Mg}+p$
 PRC63(2002)024307

Ex (MeV)	J^π
3.00	1 ⁺
3.37	1 ⁺
4.40	1 ⁺
4.67	1 ⁺
4.97	1 ⁺

○

○

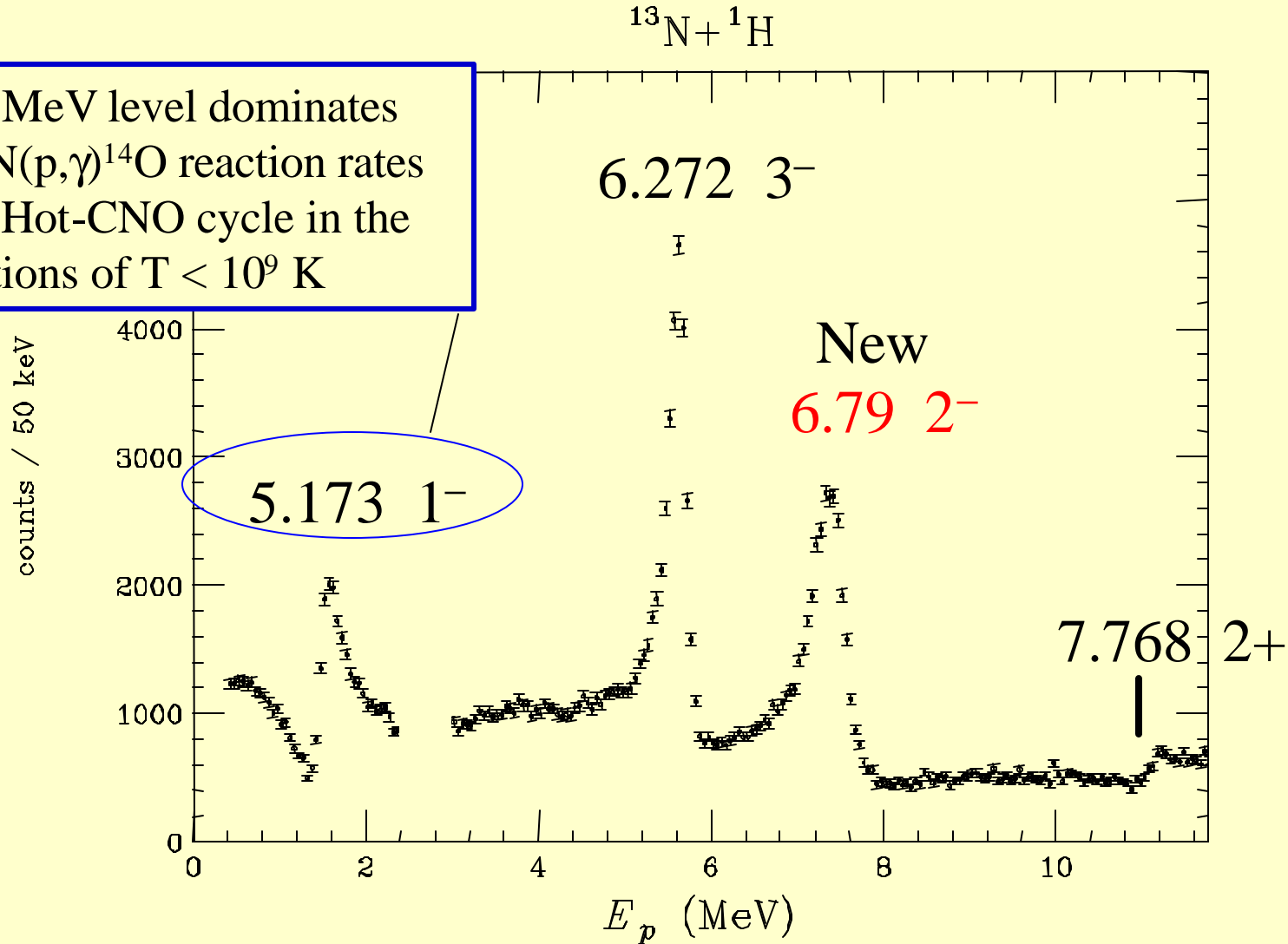
○

**Preliminary
 result of
 $^{23}\text{Mg}+p$ exp.**

1⁺ $\Gamma \sim 40$ keV
 2⁺ $\Gamma \sim 60$ keV

No exp data of G

5.173 MeV level dominates the $^{13}\text{N}(p,\gamma)^{14}\text{O}$ reaction rates in the Hot-CNO cycle in the conditions of $T < 10^9$ K



Proton-resonance scattering is a powerful tool to study nuclear structure of light unstable nuclei!

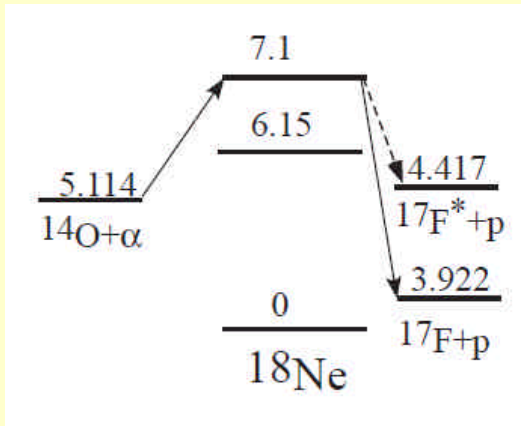
Energy resolution 20 keV (FWHM)!

Outlook

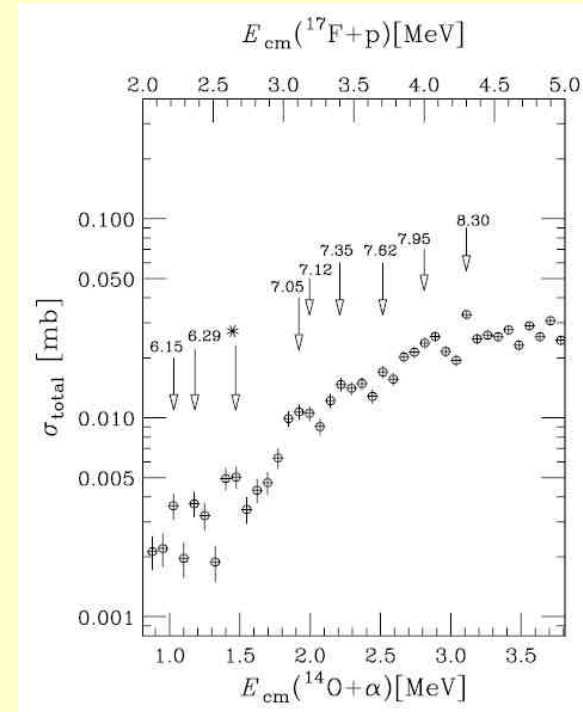
Direct measurement of stellar (α,p) or (p,α) reactions relevant to explosive hydrogen burning (rp-process) will be studied!

$^{14}\text{O}(\alpha,p)^{17}\text{F}$ break out from the hot-CNO cycle

^{14}O beam + thick He target



$$\Gamma_{\alpha} \ll \Gamma_{p}$$



Preliminary result

M. Notani et al., NPA746(2004)113c

Summary

Low-energy radioactive beams are useful to study resonance states close to the particle threshold in unstable nuclei.

Low-energy In-flight method at CNS

with intense primary beams and a large acceptance separator

Technically simpler than and complementary to ISOL

Many beams were developed in a short period

Experiments on proton-rich nuclei relevant to the explosive hydrogen burning