

A 3D CAD model of a detector assembly, likely for the SHARAQ experiment. The model shows a complex arrangement of components, including a central cylindrical detector, various support structures, and a large green rectangular component. The entire assembly is mounted on a diamond-shaped base.

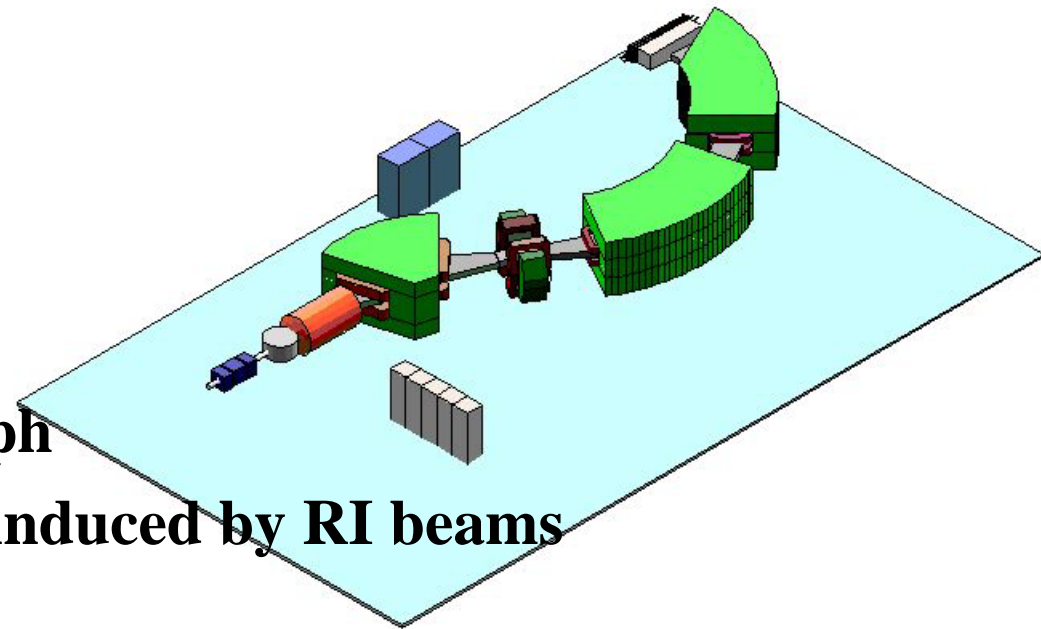
**Studies of New Excitation Modes in Nuclei
via Exothermic Nuclear Reactions
~ Physics of SHARAQ ~**

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Outline



New **SHARAQ** Spectrograph
EXOTHERMIC reactions induced by RI beams

LECTURE:

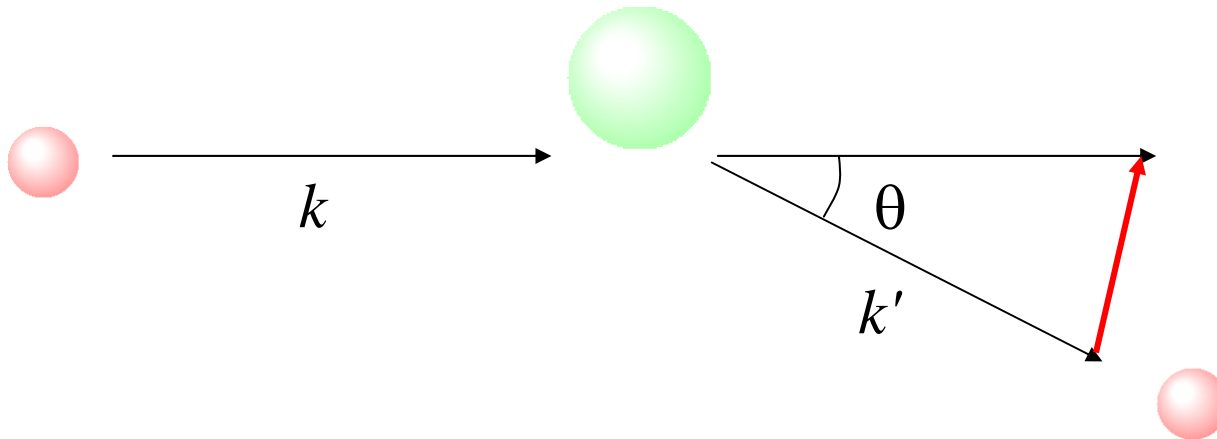
- Introduction to momentum transfer (q) in nuclear reactions
- q -dependences of nuclear transitions
- Idea of exothermic reactions
- New excitation modes in nuclei reachable by the reactions
- Overview of SHARAQ spectrograph



What is Momentum Transfer

momentum given to the target nucleus through nuclear reaction

= difference of momenta of projectile and ejectile.



$$q = k - k'$$
$$\sim 2k \sin(\theta/2) \text{ if } |k| \sim |k'|$$

angular distribution q -dependence

q takes its minimum value at 0°



Nuclear Reaction in Momentum Space

Transition amplitude by (DW) Born Approximation

$$\begin{aligned} T(k_f, k_i) &= \langle \Psi_f \chi^-(k_f) | V_{\text{residual}} | \chi^+(k_i) \Psi_i \rangle \\ &= \int \mathcal{D}(Q; k_f, k_i) \mathcal{V}(Q) \rho_{fi}(Q) dQ \end{aligned}$$

$\mathcal{D}(Q; k_f, k_i)$ Fourier transform of DW

$\mathcal{V}(Q)$ Fourier transform of interaction

$\rho_{fi}(Q)$ Fourier transform of transition density

In the plane wave limit

$$\mathcal{D}(Q; k_f, k_i) = \int e^{i(k_f - k_i)r} dr = \delta(Q - q)$$

$$T(k_f, k_i) \xrightarrow{\text{PW}} \mathcal{V}(q) \rho_{fi}(q)$$

$$q = k_i - k_f \quad \text{momentum transfer}$$



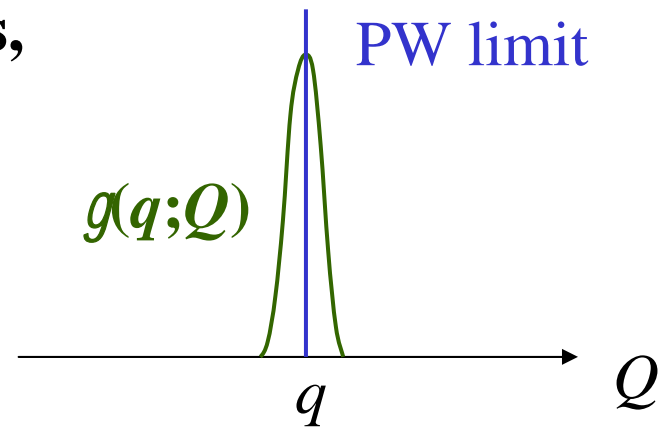
Nuclear Reaction in Momentum Space (*cont.*)

even in the presence of distortion effects,

T depends mostly on q

distortion depends only weakly on Q

interaction also, if it is short-range



$$T(k_f, k_i) \sim \mathcal{D}(q; k_f, k_i) \mathcal{V}(q) \int \underline{g(q; Q)} \rho_{fi}(Q) dQ$$

smearing function

Nuclear structure dependences of transition amplitude

can be clearly seen through momentum transfer $q = k_i - k_f$



Angular Momentum and q

Relation between orbital angular momentum and q

transition density in momentum space

$$\rho_{fi}(q) = \int \tilde{\rho}_{fi}(\mathbf{r}) e^{-i\mathbf{q}\cdot\mathbf{r}} d\mathbf{r}$$

$$\tilde{\rho}_{fi}(\mathbf{r}) \sim \mathcal{R}_\ell(r) Y_{\ell m}(\hat{\mathbf{r}})$$

Rayleigh expansion

$$e^{-i\mathbf{q}\cdot\mathbf{r}} = \sum_{\ell=0}^{\infty} \sum_m (2\ell + 1) i^\ell j_\ell(qr) Y_{\ell m}(\hat{\mathbf{k}}) Y_{\ell m}^*(\hat{\mathbf{r}})$$

Using orthogonality of spherical harmonic

$$\rho_{fi}(q) \sim \int \mathcal{R}_\ell(r) j_\ell(qr) dr$$

If the reaction is sensitive to nuclear surface,

$$\frac{d\sigma}{d\Omega} \sim |j_\ell(qR)|^2$$

$$\frac{d\sigma}{d\Omega} \propto T^2 \sim \rho_{fi}^2(q)$$



Spherical Bessel Function

for $R=4$ fm

$L=0$ $j_0(qr)$

peak at $qr = 0$

1st minimum at $qr = \pi$

$q \sim 0.8 \text{ fm}^{-1} = 160 \text{ MeV}/c$

$L=1$ $j_1(qr)$

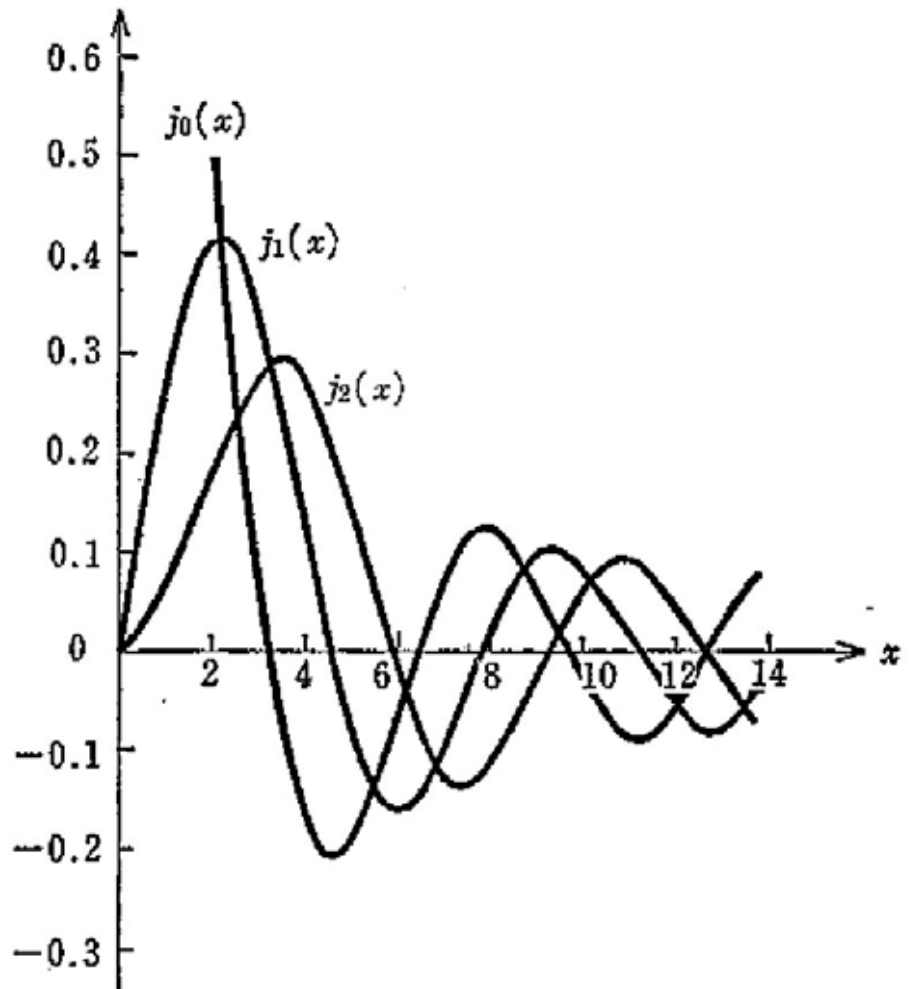
1st peak at $qr \sim 2$

$q \sim 0.5 \text{ fm}^{-1} = 100 \text{ MeV}/c$

$L=2$ $j_2(qr)$

1st peak at $qr \sim 4$

$q \sim 1.0 \text{ fm}^{-1} = 200 \text{ MeV}/c$





q-region and related physics

Large momentum transfer

high momentum states
short-range phenomena

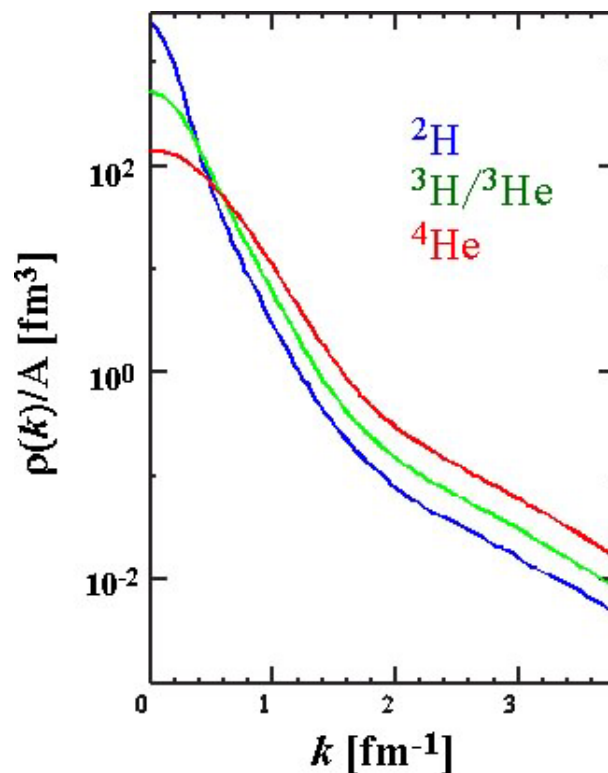
Ideguchi-san's talk

Small momentum transfer

$\Delta L = 0$ transitions
Gamow-Teller transition
weakly bound states

$$k \sim \sqrt{2\mu B}$$

neutron rich nuclei
pionic atom





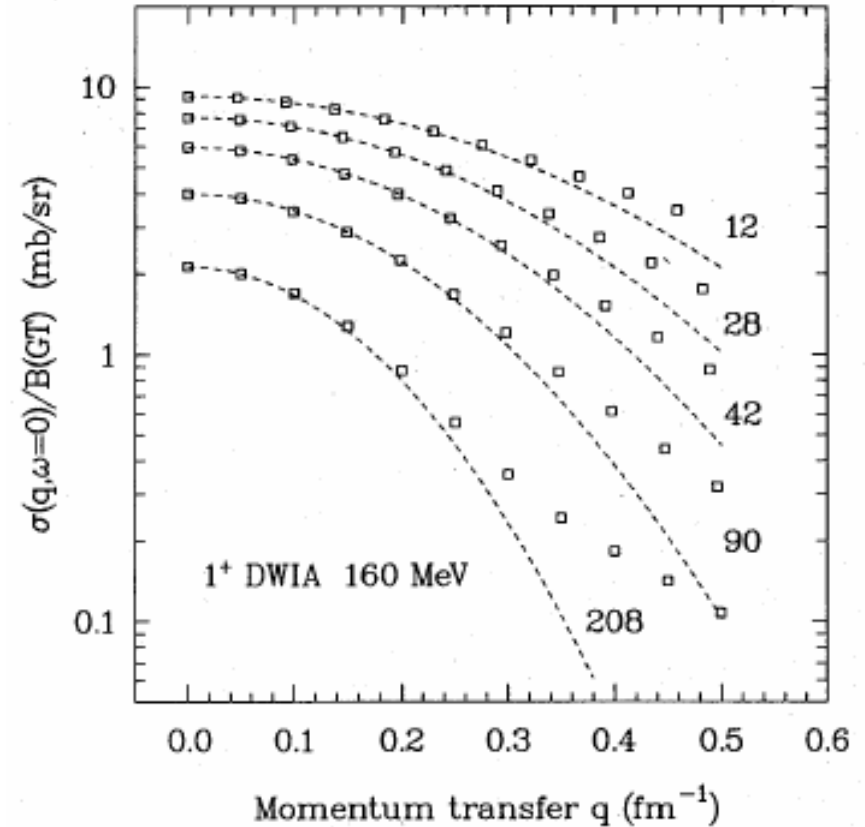
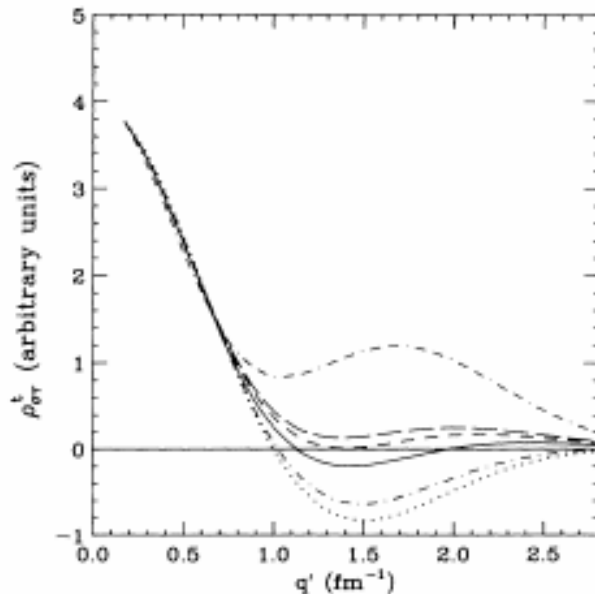
Examples of q -dependences

1) Gamow-Teller excitation

$$\Delta S = 1$$

$$\Delta T = 1$$

$$\Delta L = 0$$



F. Osterfeld et al., Phys. Rev. C 45 (1992) 2854.

T. N. Taddeucci et al.,
Nucl. Phys. A 469 (1987) 125.

Examples of q -dependences (*cont.*)

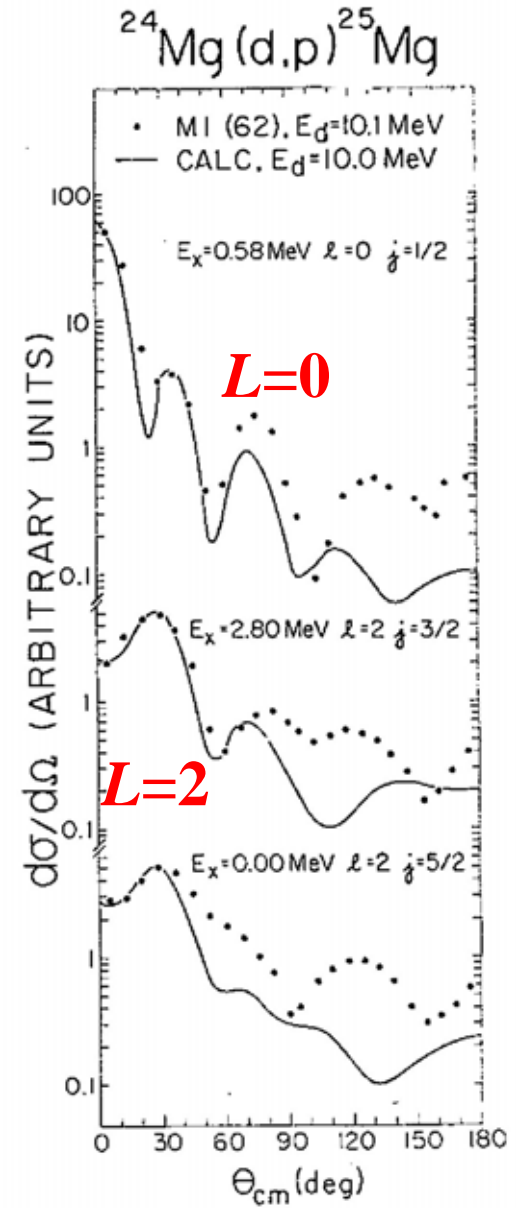
2) (d,p) reaction

$$T^{PW} = \sum F_T(q) F_p(q')$$

$$q = k_p - \frac{A}{A+1} k_d$$

transition density of target part
is w.f. of transferred neutron

$$\tilde{\rho}_{fi}(r) \sim \Psi_n(r) Y_{lm}(\hat{r})$$





What' beyond?

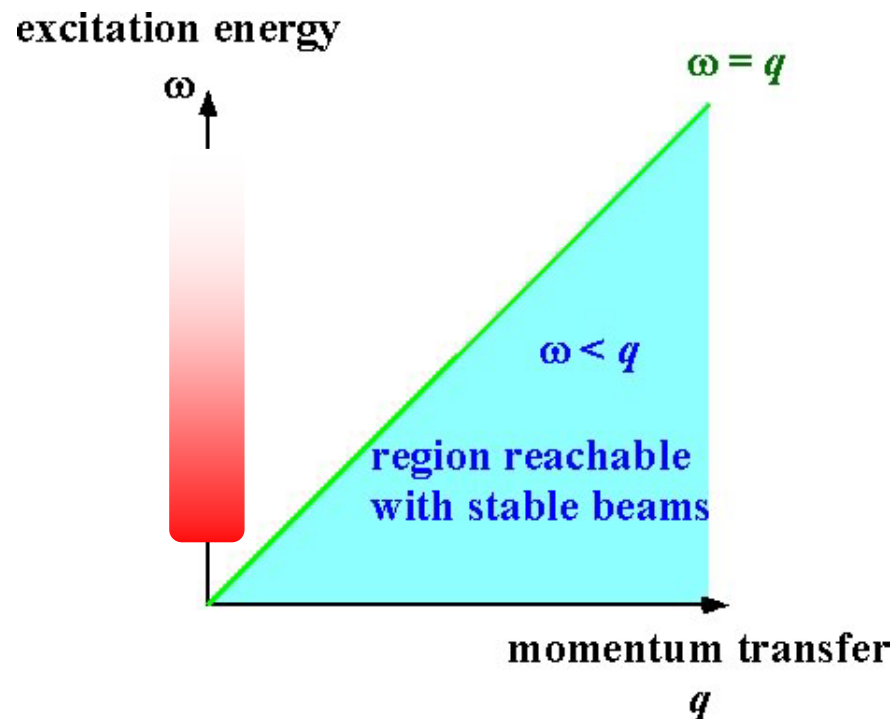
spectroscopy of low excitation energy levels with small L
reactions with stable beams work well.

BUT this is not the case for highly excited states with small L !

WHY limited?

**HOW we can break
the limitation?**

**What we can expect
in the unexplored region**





Excitation energy and momentum transfer

Consider binary reaction at 0° .



Energy Conservation

$$E_1 + m_2 = E_3 + E_4$$

Momentum Conservation

$$p_1 = p_3 + p_4$$

since $q \ll m_4$ in the case considered, $T_4 \sim 0$.

Energy transfer

$$\omega = E_1 - E_3 \sim M_4 - M_2$$

Momentum transfer

$$q = p_1 - p_3$$



ω and q (*cont.*)

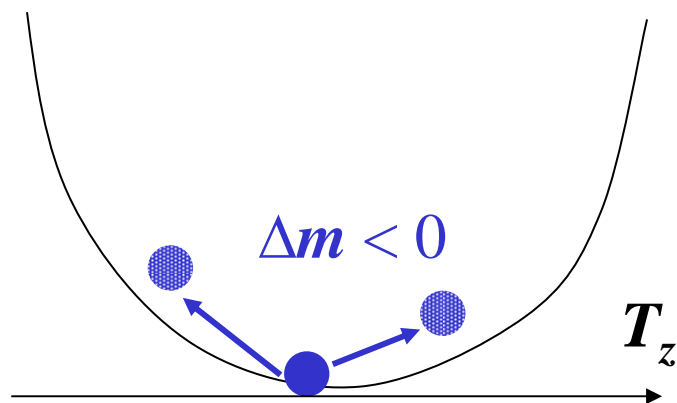
Solving the equations and taking small q approximation,

$$\omega \sim \frac{m_1 - m_3}{\gamma} + \beta q$$

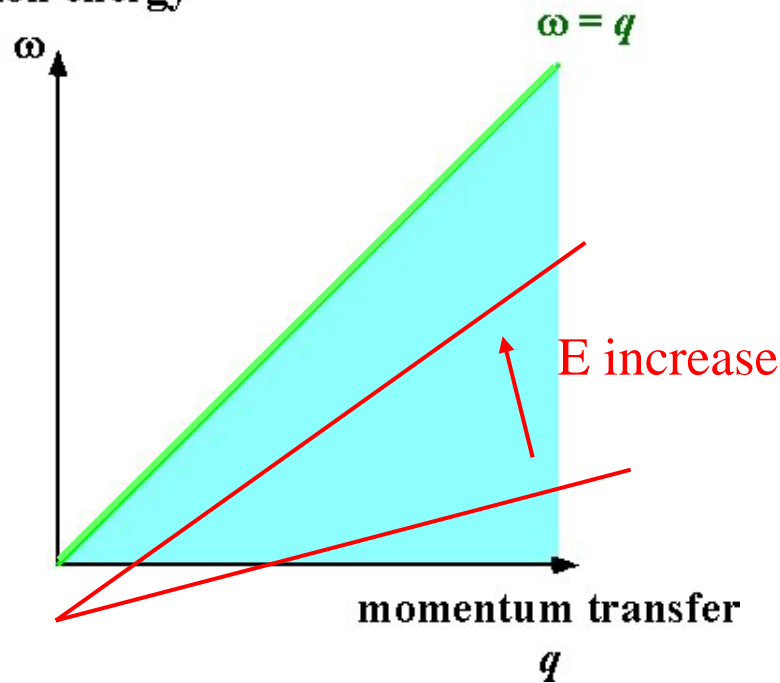
In stable beam induced reactions

$$\Delta m = m_1 - m_3 < 0$$

stable nucleus has the smallest mass among its isobars



excitation energy



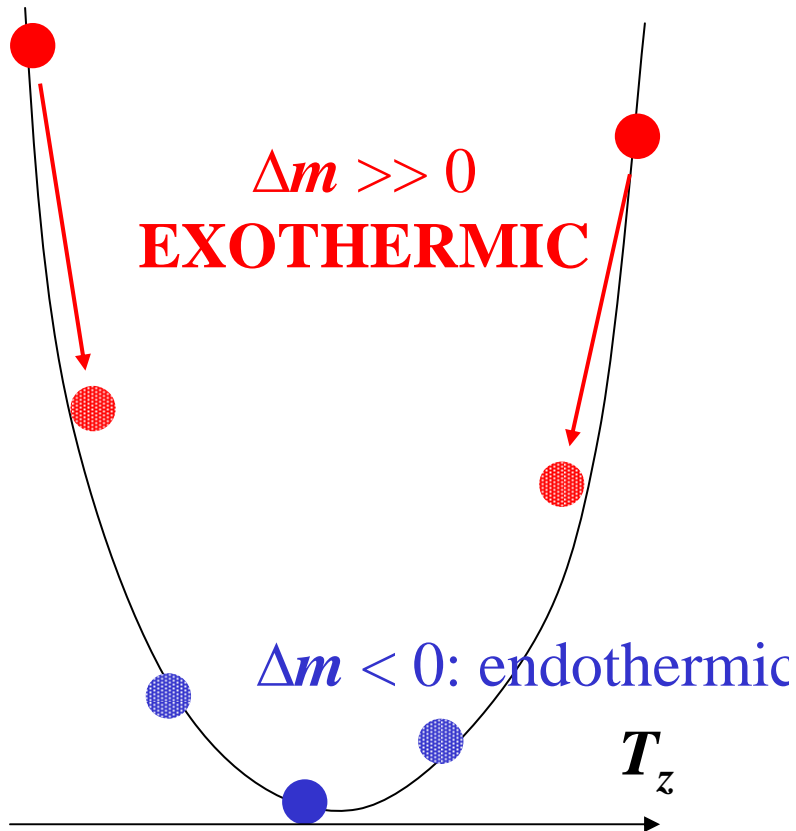


New Idea to use unstable nuclei

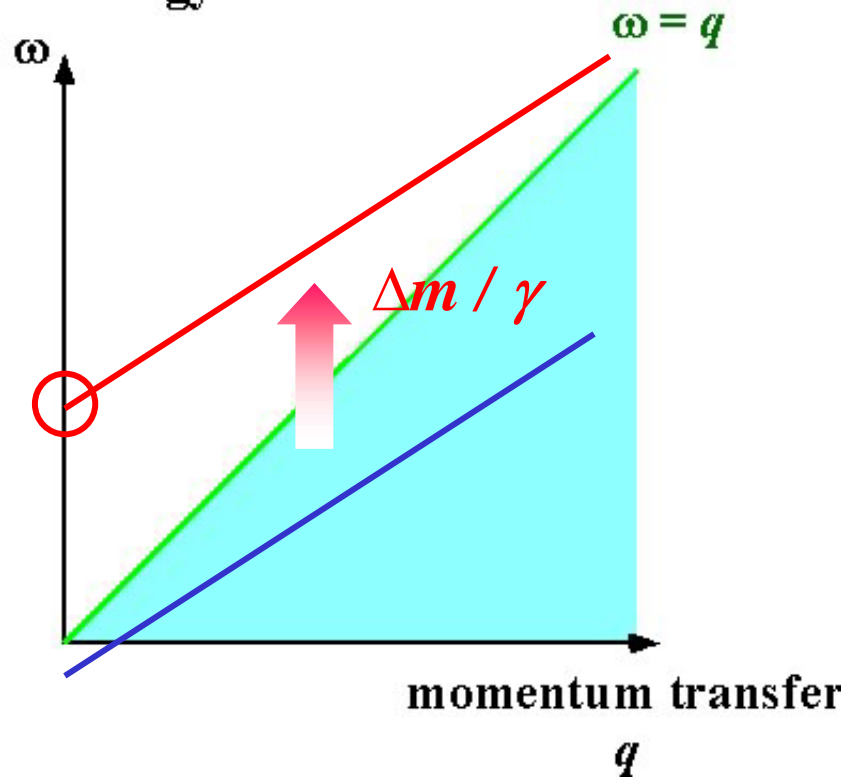
with stable beam

with unstable beam

$$\omega \sim \frac{m_1 - m_3}{\gamma} + \beta q$$



excitation energy





New Excitation modes at large ω & small q

$\Delta L=0$ Excitations

2) **Isovector Spin
Monopole Resonances**

$\omega = 30 - 40$ MeV

1) **Double Gamow-Teller
resonance**

$\omega = 20 - 25$ MeV

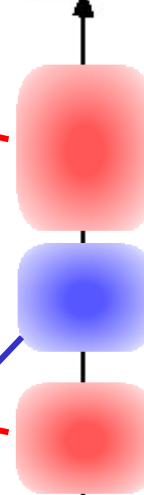
Weakly interacting system

3) **Multi-neutron states**

$\omega \sim 30$ MeV

excitation energy


ω



$\omega = q$

momentum transfer

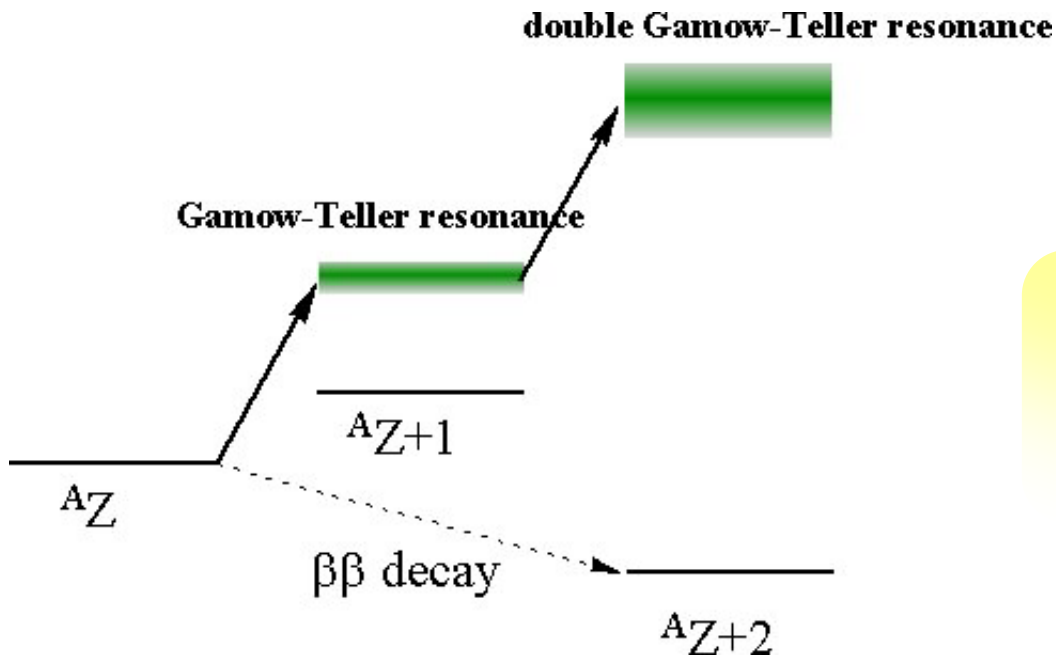
q



Double Gamow-Teller resonance

GT resonance laid on GT resonance

NOT YET DISCOVERED



$$E_{\text{DGTR}} = 2 E_{\text{GTR}} ?$$
$$\Gamma_{\text{DGTR}} = 2 \Gamma_{\text{GTR}} ?$$

irreplaceable "calibration standard" of $\beta\beta$ -decay nuclear matrix element

Heavy-ion double charge exchange reactions

($^{18}\text{O}, ^{18}\text{Ne}$), ($^{11}\text{B}, ^{11}\text{Li}$)

no successful results



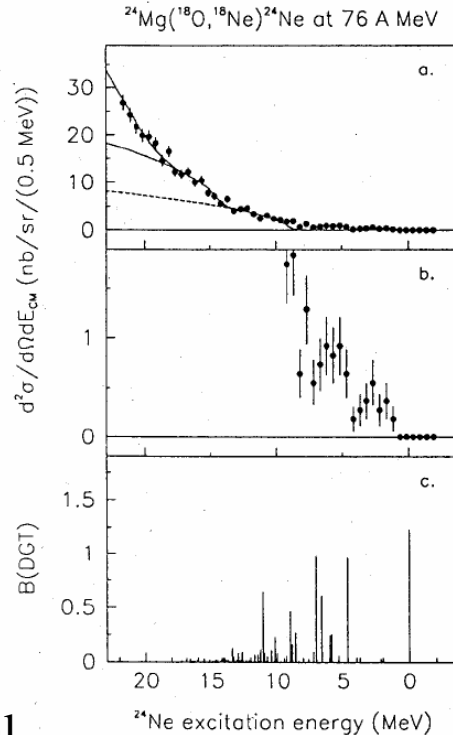
Momentum transfer in candidate reactions

$(^{18}\text{O}, ^{18}\text{Ne})$ @ 76 MeV/A, GANIL

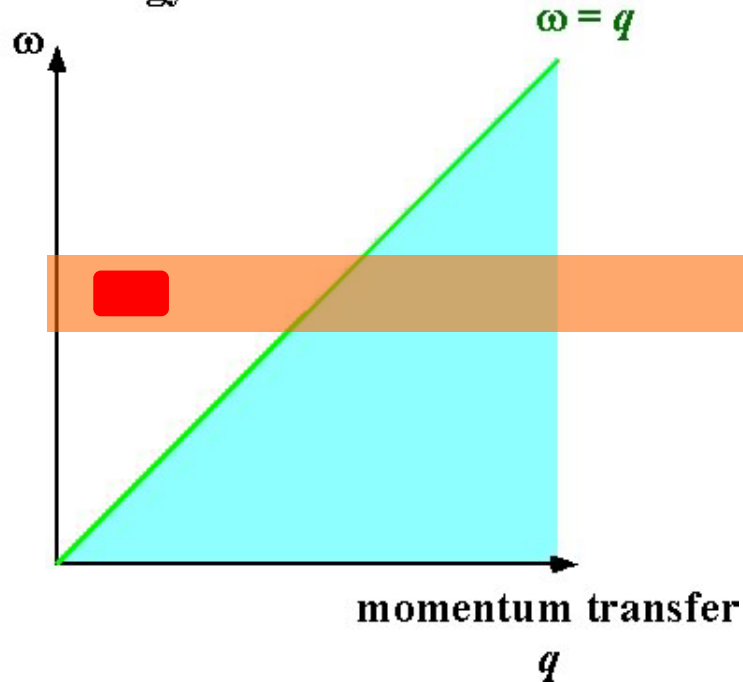
$$q = 90 \text{ MeV}/c$$

$(^{11}\text{B}, ^{11}\text{Li})$ @ 69 MeV/A, RCNP

$$q = 174 \text{ MeV}/c$$



excitation energy



$^{100}\text{Mo}(^{20}\text{Mg}, ^{20}\text{Ne})$ @ 150 MeV/A, RIBF

$$q = 8 \text{ MeV}/c$$

most promising reaction



Isvector Spin Monopole Resonance

Breathing (compressive) mode

spin-isospin density ($\sigma\tau$) oscillates

"spin-isospin compressibility"

propagation velocity of "spin-isospin sound"

$$\mathcal{O}_{IVSMR} = \sum r_i^2 \sigma_i \tau_i$$

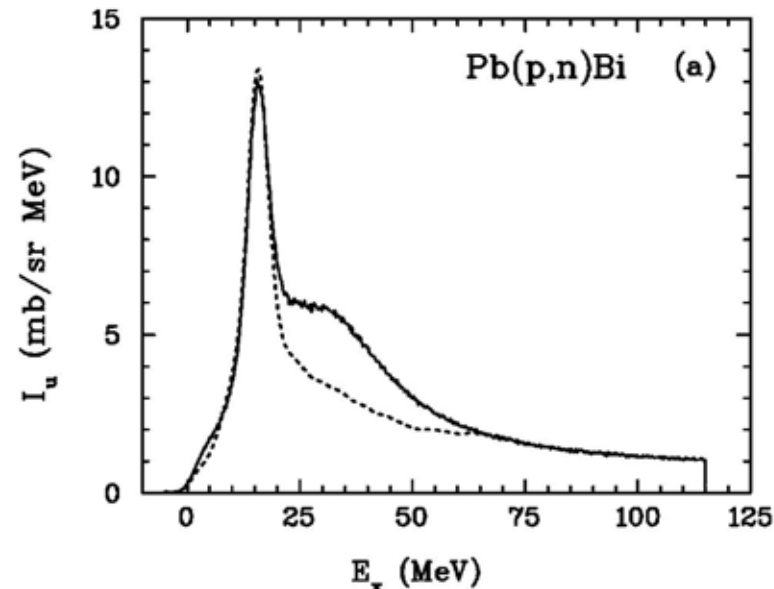
One data indicative of its existence

$^{208}\text{Pb}(p,n)$ @795MeV (LAMPF)

D.L. Prout et al., PRC **63** (2000) 014603.

$(^3\text{He},t)$ data from RCNP

R.G.T.Zegers et al. PRL **90** (2003) 202501.





Probes to IVSMR

L=0 resonance

small q

spin-isospin excitation

150 – 300 MeV/A

surface sensitivity

$$\int \rho_{IVSMR}(r) r^2 dr = 0$$

heavy ion reaction

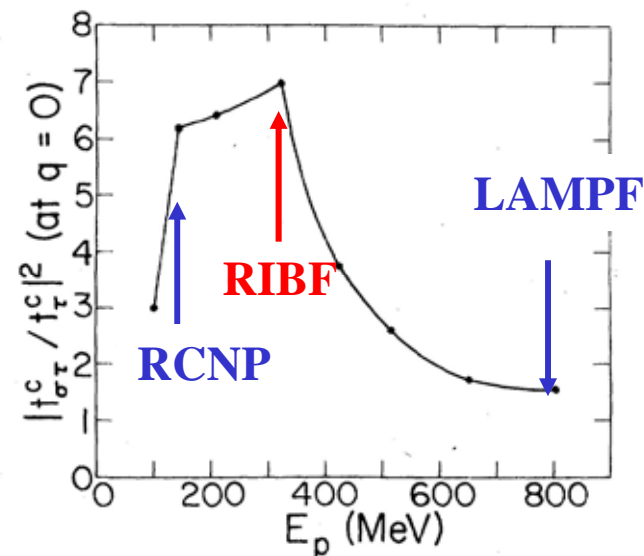
$(^{12}\text{N}, ^{12}\text{C}), (^{12}\text{B}, ^{12}\text{C})$ reaction at RIBF

possible probes to IVSMR

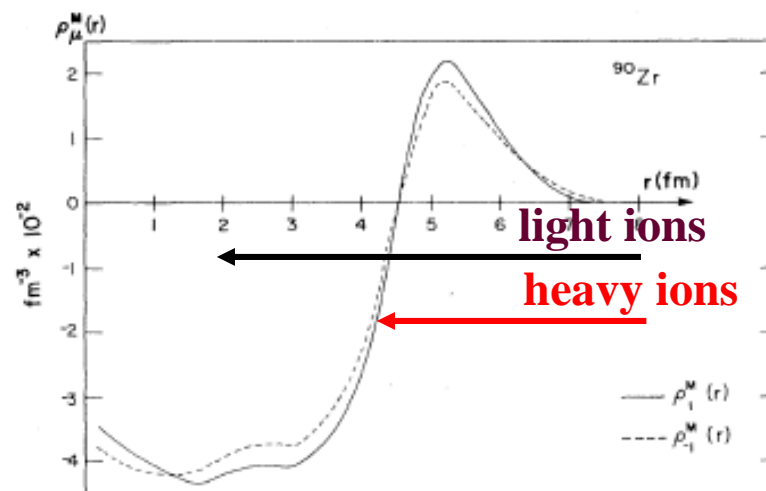
$q \sim 40 \text{ MeV}/c$

$E/A \quad 350 \text{ MeV}/A$

sensitivity to $\sigma\tau$ mode



W.G.Love and M.A.Franey,
Phys. Rev. C **24** (1981) 1073.



N. Auerbach et al.,
Phys. Rev. C **28** (1983) 280.



Multi-neutron states

extreme of neutron-rich, weakly interacting "nuclei"

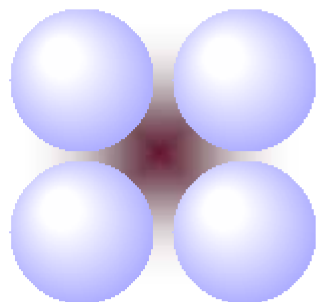
many body correlation in neutron matter

three-, four- nucleon force

4-neutron bound state: "tetra-neutron"

B 1MeV

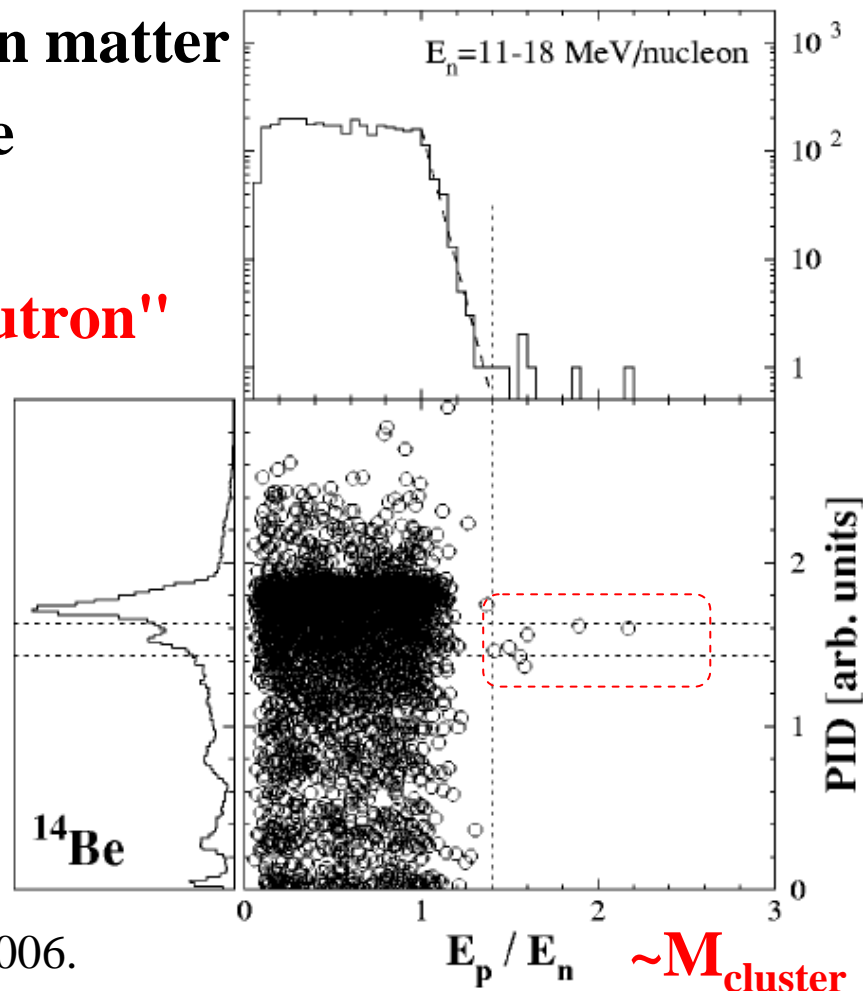
if bound



Candidates?

7 events in ^{14}Be breakup

in coincidence with ^{10}Be





$(^8\text{He}, ^8\text{Be})$ Reaction

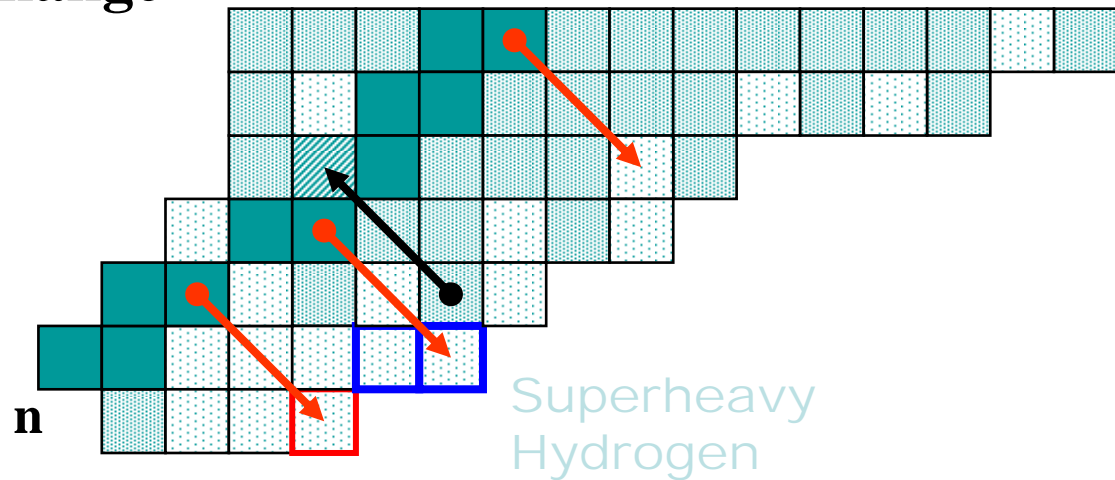
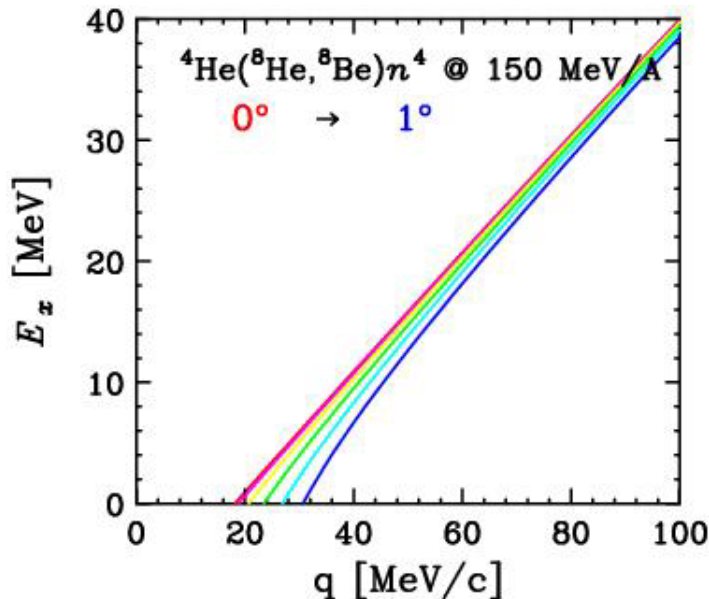
n^4 -state: weakly interacting system

should be softly produced, i.e. with small q

$$\omega \sim 4m_n - m_{^4\text{He}} \sim 30\text{MeV}$$

$(^8\text{He}, ^8\text{Be})$ reaction

double charge exchange



Neutron
"Nugget"

$3,4n: ^3,4\text{He}(^8\text{He}, ^8\text{Be})$

$6,7\text{H}: ^6,7\text{Li}(^8\text{He}, ^8\text{Be})$



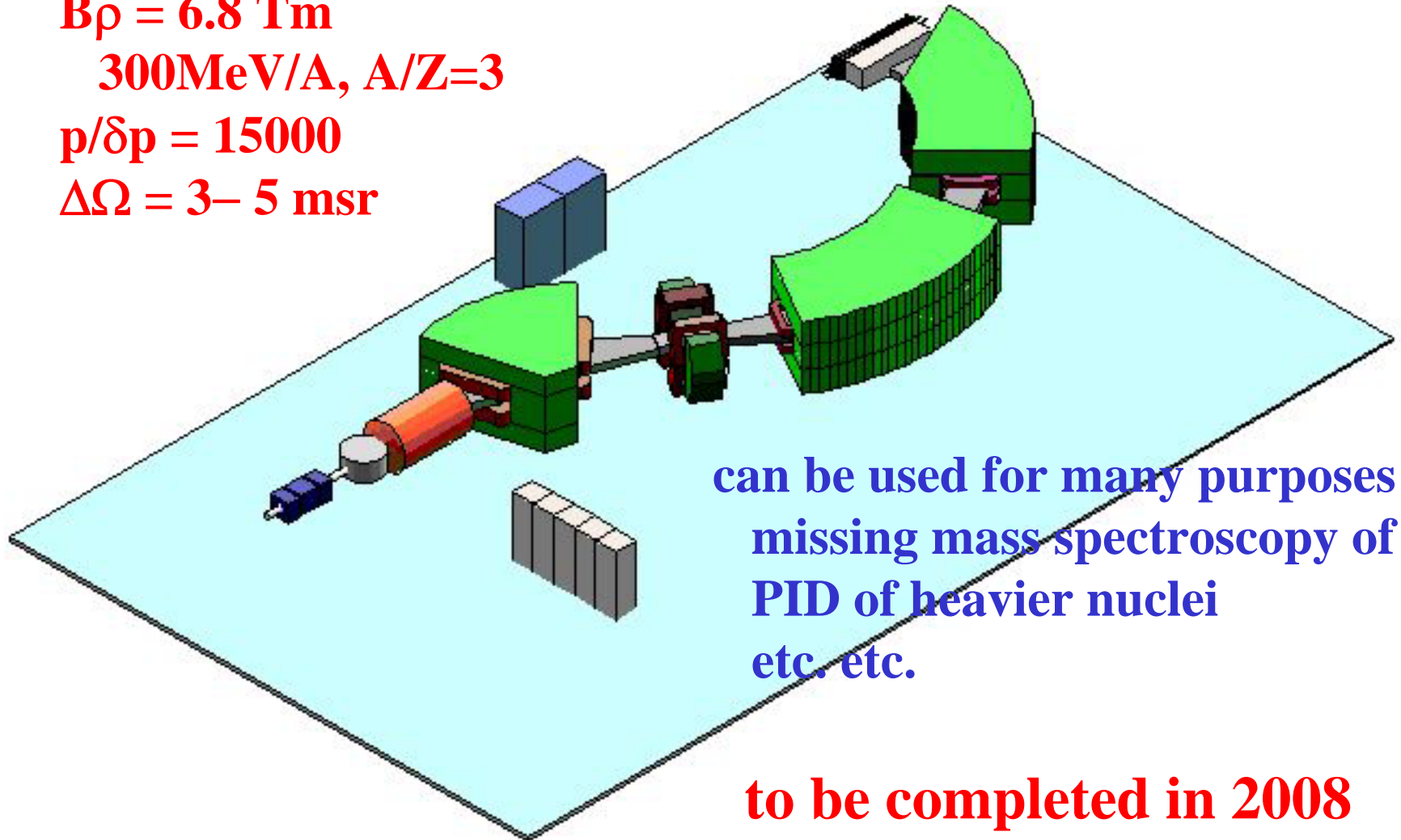
SHARAQ spectrograph at RIBF

$B\rho = 6.8 \text{ Tm}$

$300 \text{ MeV/A}, A/Z=3$

$p/\delta p = 15000$

$\Delta\Omega = 3-5 \text{ msr}$



can be used for many purposes
missing mass spectroscopy of RI
PID of heavier nuclei
etc. etc.

to be completed in 2008



Summary

- 1. momentum transfer** is an important key to understand nuclear reaction.
- 2. stable-beam induced reaction can probe only $q > \omega$ region.**
while several interesting subjects are sitting in $q < \omega$.
- 3. RI beam can provide new experimental approaches to explore the unexplored region in q - ω plane.**
 - double Gamow-Teller resonances**
 - isovector spin monopole resonances**
 - multi-neutron states**
- 4. Combination of RI beams from RIBF and SHARAQ spectrograph can give us much.**

YOUR NEW IDEAS OPEN THE POSSIBILITY!